

Answer 6.1

Station 1: A 50-mg/l solution of tracer is injected at the rate of $Q_i = 100 \text{ cm}^3/\text{s}$.

Station 2: Located 100-m downstream of Station 1.
Dye concentration, $C_{\text{dye}} = 10 \text{ } \mu\text{g/l}$
Lindane concentration, $C_{L2} = 0.5 \text{ } \mu\text{g/l}$

Station 3: Located 200-m downstream of Station 1.
Dye concentration, $C_{\text{dye}} = 8 \text{ } \mu\text{g/l}$
Lindane concentration, $C_{L3} = 0.9 \text{ } \mu\text{g/l}$

If dye is well-mixed and concentration is steady, then the flow at stations 2 and 3 is

$$Q_2 = Q_i C_i / C_{\text{dye}} = (100 \text{ cm}^3 \text{ s}^{-1})(50 \text{ mg l}^{-1}) / (0.01 \text{ mg l}^{-1}) = 0.50 \text{ m}^3 \text{ s}^{-1}$$

$$Q_3 = Q_i C_i / C_{\text{dye}} = (100 \text{ cm}^3 \text{ s}^{-1})(50 \text{ mg l}^{-1}) / (0.008 \text{ mg l}^{-1}) = 0.63 \text{ m}^3 \text{ s}^{-1}$$

If no tributaries or sewer outfalls exist between stations 2 and 3, then we expect the groundwater inflow between these stations to be

$$Q_{\text{GW}} = Q_3 - Q_2 = 0.13 \text{ m}^3 \text{ s}^{-1}.$$

To find the Lindane concentration in the groundwater we evaluate conservation of mass within the river between station 2 and 3. Influxes of Lindane to this control volume are at station 2 and from groundwater. The outflow is at station 3. Such that

$$Q_2 C_{L2} + Q_{\text{GW}} C_{\text{LGW}} = Q_3 C_{L3}$$

Solving for the groundwater concentration

$$C_{\text{LGW}} = \frac{Q_3 C_{L3} - Q_2 C_{L2}}{Q_{\text{GW}}} = 2.4 \text{ } \mu\text{g/l}$$