

Lecture 24 - Intrinsic Limits of Transistor Speed - Outline

- **Announcements**

 - Handouts - Lecture Outline and Summary

 - Problem Set No. 10 - Don't forget, there is one, and it is due Friday!

 - Final - Monday, Dec. 15, 9:00 am -noon, duPont Gymnasium

- **Review - Dealing with shunting feedback capacitances: C and C_{gd}**

 - The Miller effect: any C bridging a gain stage looks bigger at the input

 - The Marvelous cascode: CE/S-CB/G (E/SF-CB/G work, too - see A741)

 - large bandwidth, large output resistance
used in gain stages and in current sources

- **Intrinsic high frequency limits for transistors**

 - General approach

- **Limits for BJTs:**

 - Metrics

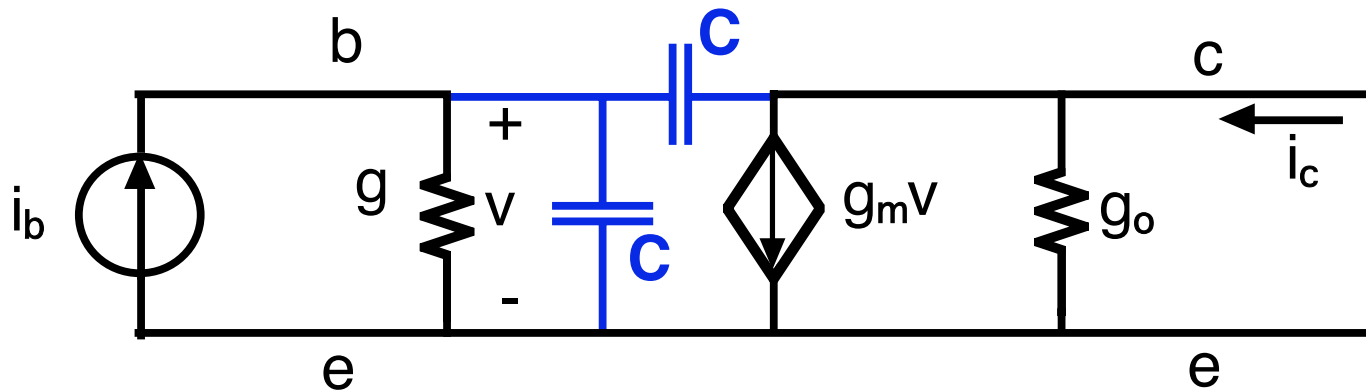
 - Design lessons

- **Limits for MOSFETs:**

 - Metric

 - Design lessons

Intrinsic H_{HI} 's for the BJTs - short-circuit current gain



The common-emitter short-circuit current gain is:

$$i_{sc}(j) \equiv \frac{i_c(j)}{i_b(j)} = \frac{[g_m \quad j \quad C]}{\{g + j [C + C]\}}$$

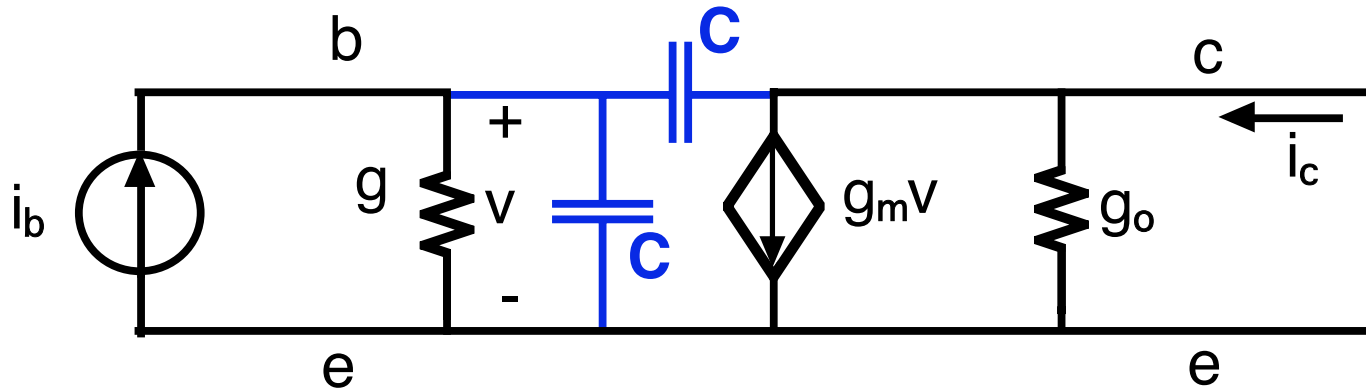
there is one pole, call it p , and one zero, z :

$$p = \frac{g}{[C + C]}, \quad z = \frac{g_m}{C}$$

Of these two, p is much smaller and this is the 3dB point of the common-emitter short-circuit current gain. We give it the name f_{3dB} .

$$\equiv \frac{g}{[C + C]}$$

Intrinsic β_{sc} 's for the BJTs - short-circuit current gain, cont.



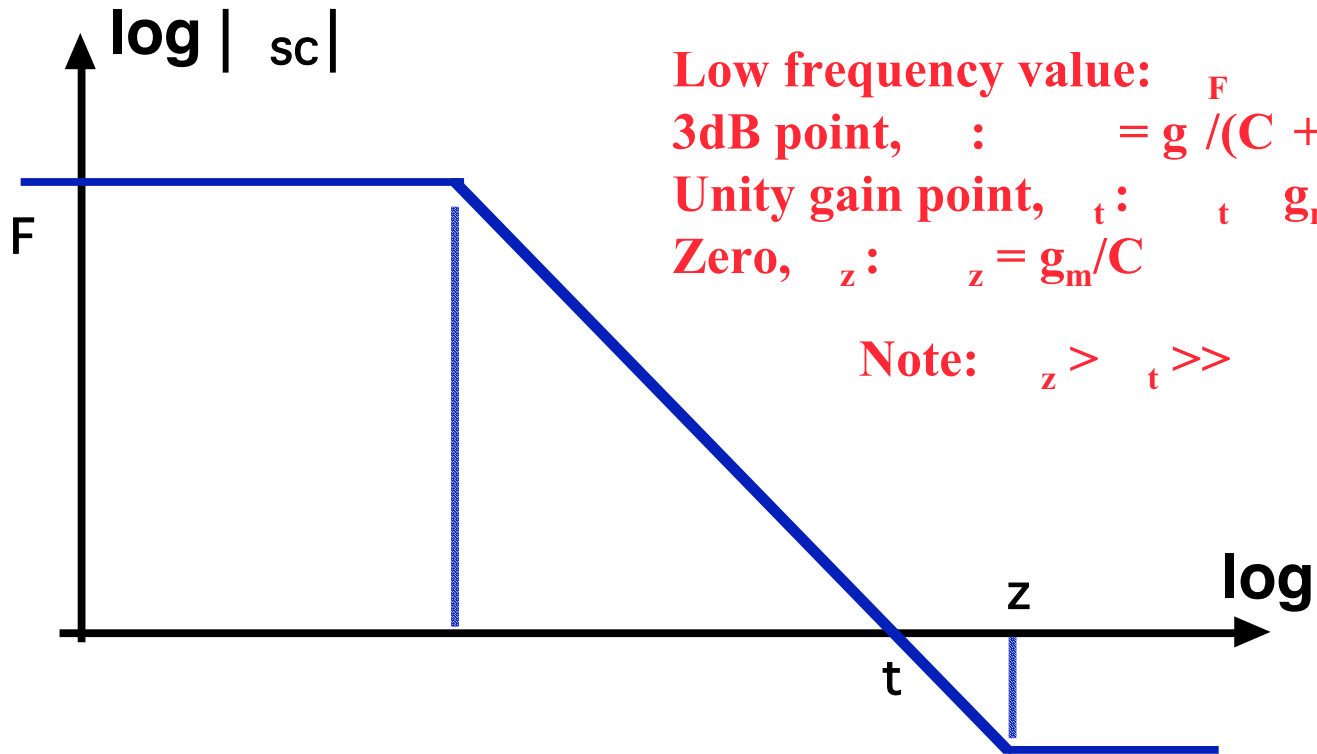
The magnitude of β_{sc} is greater than one at frequencies higher than f_t . The frequency at which it is one is called f_t .

$$|\beta_{sc}(j\omega)| = \sqrt{\frac{[g_m^2 + \omega^2 C^2]}{\{g^2 + \omega^2 [C + C']^2\}}}$$

Setting this equal to one and solving for ω we find that f_t is:

$$f_t = \frac{1}{2\pi} \sqrt{\frac{[g^2 + g_m^2]}{\{[C + C']^2 - C^2\}}} \frac{g_m}{[C + C']}$$

BJT short-circuit current gain, $s_c(j)$, and T

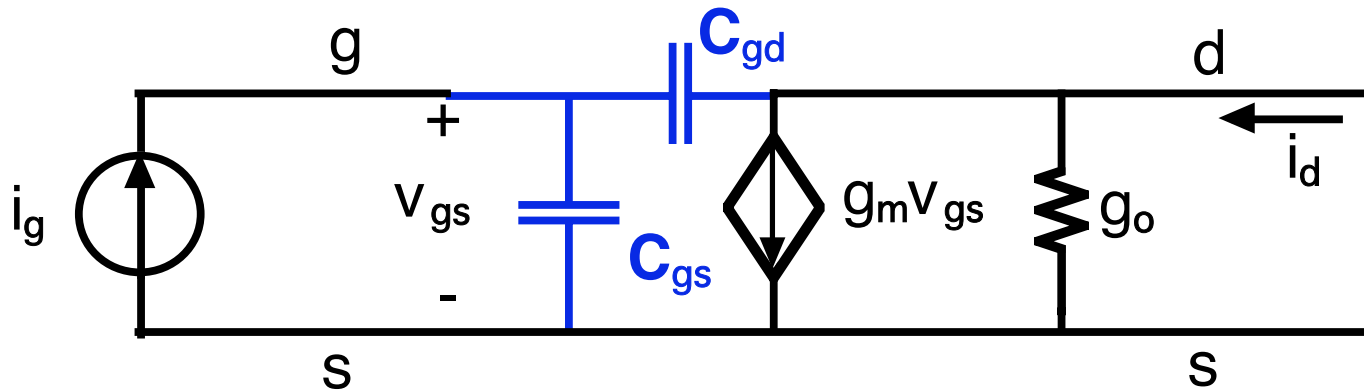


$$t = \frac{g_m}{[C_{eb,dp} + C_{cb,dp}]} = \frac{g_m}{\{g_m \tau_{trB} + C_{eb,dp} + C_{cb,dp}\}} = \frac{qI_C/kT}{\{[qI_C/kT] \tau_{trB} + C_{eb,dp} + C_{cb,dp}\}}$$

In the limit of large I_C :

$$t(BJT) = \frac{1}{\tau_{trB}} = \frac{2D_{eB}}{W_B^2} = \frac{2}{W_B^2} \frac{eV_{thermal}}{e}$$

Intrinsic H_{HI} 's for the MOSFETs - short-circuit current gain



The common-source short-circuit current gain is:

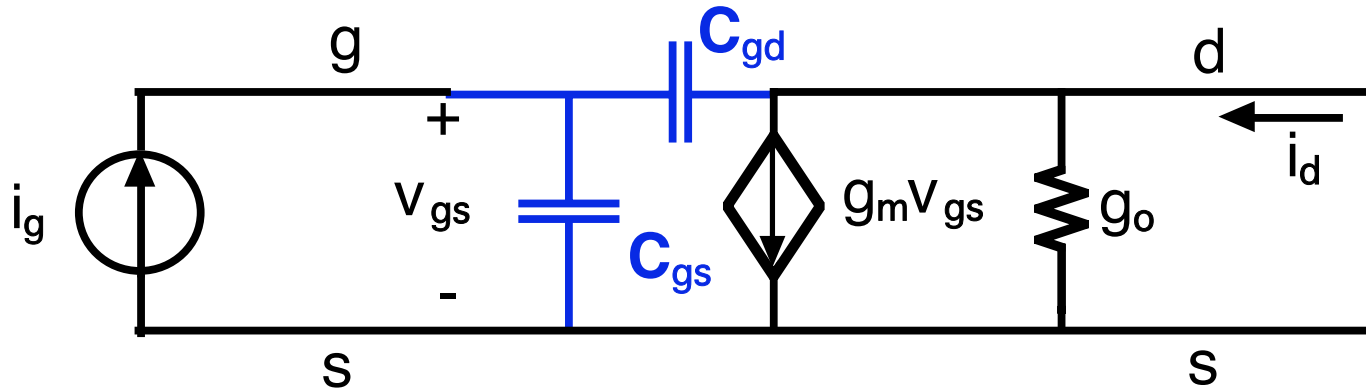
$$A_{sc}(j\omega) \equiv \frac{i_d(j\omega)}{i_g(j\omega)} = \frac{[g_m - j\omega C_{gd}]}{j\omega [C_{gs} + C_{gd}]}$$

there is one pole at $\omega = 0$, and one zero, call it ω_z :

$$\omega_z = \frac{g_m}{C_{gd}}$$

The magnitude of A_{sc} is infinity at DC, and it decreases linearly with increasing frequency.

Intrinsic H_{sc} 's for the MOSFETs - short-circuit current gain, cont.



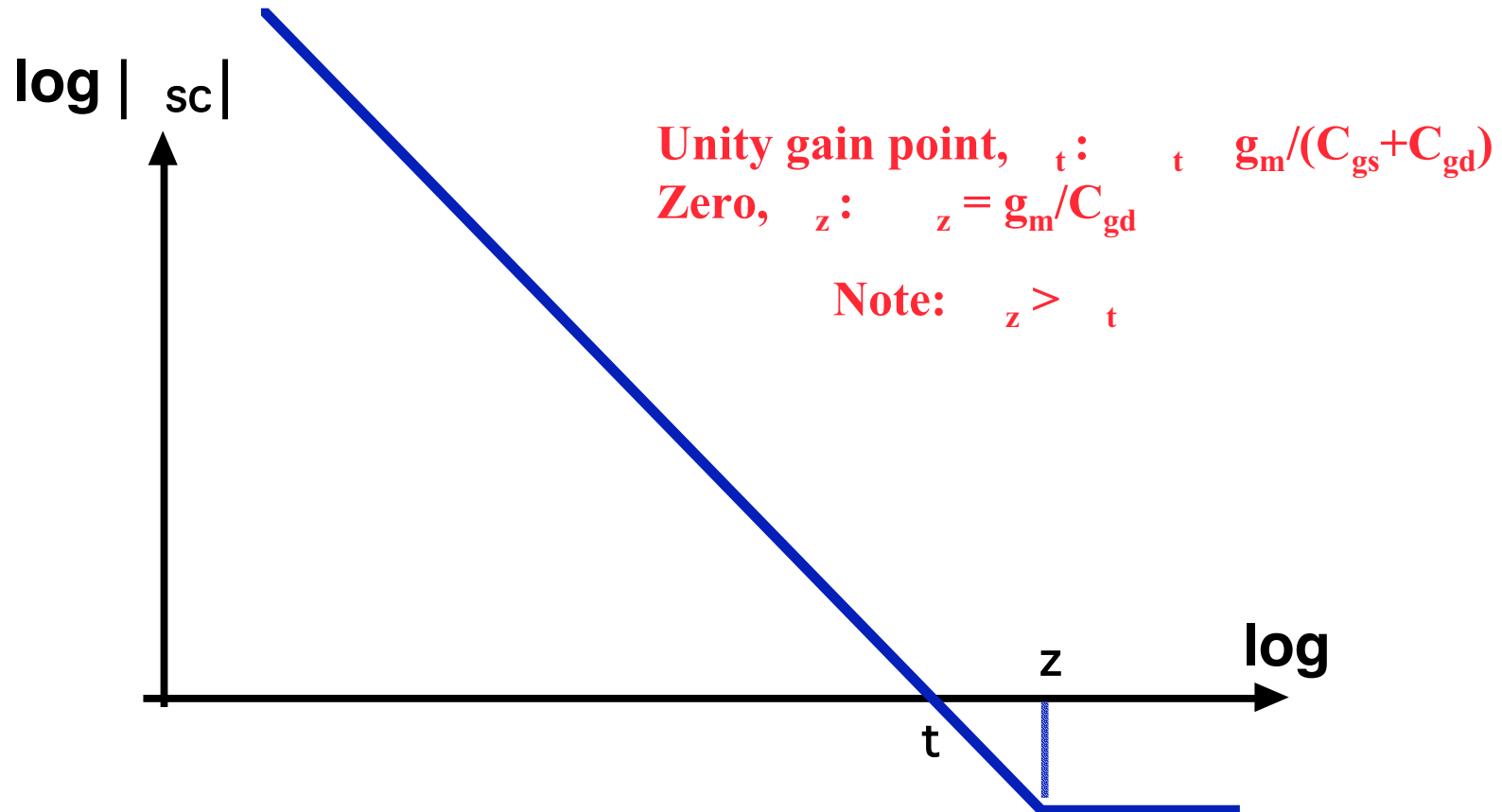
The magnitude of H_{sc} is one at a frequency which is called f_t :

$$|H_{sc}(j\omega)| = \sqrt{\frac{[g_m^2 + \omega^2 C_{gd}^2]}{\omega^2 [C_{gs} + C_{gd}]^2}}$$

Setting this equal to one and solving for f_t we find:

$$f_t = \sqrt{\frac{g_m^2}{\{[C_{gs} + C_{gd}]^2 - C_{gd}^2\}}} = \frac{g_m}{[C_{gs} + C_{gd}]}$$

MOSFET short-circuit current gain, $|a_{sc}(j\omega)|$, and f_T



$$f_t(\text{MOSFET}) = \frac{g_m}{C_{gs} + C_{gd}} = \frac{g_m}{C_{gs}} = \frac{\frac{W}{L} \mu_n C_{ox}^* [V_{GS} - V_T]}{\frac{2}{3} W L C_{ox}^*} = \frac{3}{2} \frac{\mu_n [V_{GS} - V_T]}{L^2}$$

Looking more at τ_T for BJTs and MOSFETs:

For a MOSFET we have

$$\tau_T(\text{MOSFET}) = \frac{3}{2} \frac{e [V_{GS} - V_T]}{L^2}$$

The average E-field in the channel, E_y , is
So we can also write τ_T as

$$\tau_T(\text{MOSFET}) = \frac{3}{2} \frac{e [V_{GS} - V_T]}{L} \frac{1}{L} \frac{1}{\bar{s}_y} = \frac{1}{\tau_{\text{Channel}}}$$

This is identical to the form we have for τ_T in a BJT

$$\tau_T(\text{BJT}) = \frac{1}{\tau_{trB}} = \frac{2D_{eB}}{w_B^2} = \frac{2}{w_B^2} e V_{thermal}$$

What happens when we have velocity saturation?

$$\tau_T(\text{MOSFET}) = \frac{s_{sat}}{L}, \quad \tau_T(\text{BJT}) = \frac{s_{sat}}{w_B}$$

τ_T still decreases with L and w_B , but not as quickly!

Lecture 24 - Intrinsic Limits of Transistor Speed - Summary

- **Intrinsic high frequency limits for transistors**

General approach: short-circuit current gains

- **Limits for BJTs:**

Metrics - CE short-circuit current gain 3B pt: $A_{T,3B} = g_m / (C_{gs} + C_{gd})$

CE short-circuit current gain unit gain pt: $A_{T,UG} = g_m / (C_{gs} + C_{gd})$

$A_{T,UG}$ approaches $1/\tau_b$ as I_c increases and $\tau_b = W_B^2 / 2D_{min,B}$
 so $A_{T,UG} \approx 2D_{min,B} / W_B^2 = 2 \mu_n V_{th} / W_B^2$

CB short-circuit current gain unit gain pt: $A_{T,UG} = g_m / C_{gs}$

Design lessons - bias at high collector current

minimize W_B (win as W_B^2)

use npn over pnp ($\mu_n \gg \mu_p$)

- **Limits for MOSFETs:**

Metric - CS short-circuit current gain unit gain pt: $A_{T,UG} = g_m / [(C_{gs} + C_{gd})^2 - C_{gd}^2]^{1/2}$

$A_{T,UG}$ is approximately $g_m / C_{gs} = 3 \mu_n (V_{GS} - V_T) / 2L^2$

$g_m = (W/L) \mu_n C_{ox} (V_{GS} - V_T)$ and $C_{gs} = (2/3) WLC_{ox}$

so $A_{T,UG} \approx 3 \mu_n (V_{GS} - V_T) / 2L^2$

Design lessons - bias at large I_D

minimize L (win as L^2)

use n-channel over p-channel ($\mu_n \gg \mu_p$)