

## April 8, 2005: Wrap up porous media, Deformation processing

Porous media: calculating  $K_1$  starting with single tube average velocity:

$$u_{av} = \frac{Q}{A_{xs}} = \frac{\Delta P R^2}{8\mu L}. \quad (4.103)$$

Definitions:

- $\omega$  is pore volume fraction (so  $1 - \omega$  is solid volume fraction)
- $S$ =area/vol
- $S_0$ =area/solid vol= $S/(1 - \omega)$
- $R_h$ =hydraulic radius=fluid volume/wetting area  $V_h/A_w = \omega/S_0(1 - \omega)$ .

Then said average fluid velocity in pores (fluid phase) is like tube flow:

$$\bar{V} = K_1 \frac{\Delta P' R_h^2}{L\mu}; \quad V_0 = K_1 \frac{\Delta P' R_h^2 \omega}{L\mu} = K_1 \frac{\nabla P' \omega}{L\mu} \frac{\omega^2}{S_0^2(1 - \omega)^2}. \quad (4.104)$$

So set  $\bar{V}$  equal to  $u_{av}$ :

$$K_1 \frac{\Delta P' R_h^2}{L\mu} = \frac{(P_1 - P_2)R^2}{8\mu L} \quad (4.105)$$

$$K_1 \left(\frac{R}{2}\right)^2 = \frac{R^2}{8} \quad (4.106)$$

$$K_1 = \frac{1}{2}. \quad (4.107)$$

For a packed bed of spheres, around 1/4.2 or 1/5, differences in literature.

This works for Stokes flow (laminar in tubes); how to define Reynolds number?

$$\text{Re} = \frac{\rho \bar{V} R_h}{\mu} = \frac{\rho V_0}{\mu(1 - \omega)S_0}, \quad (4.108)$$

For a friction factor, we get:

$$f_c = \frac{F_d}{KA} = \frac{\Delta P' \cdot A_{xs}\omega}{\rho \bar{V}^2 \cdot A_w} = \frac{\Delta P' V}{L} \frac{\omega^3}{\rho V_0^2 S_0(1 - \omega)V} = \frac{\Delta P' \omega^3}{L\rho V_0^2 S_0(1 - \omega)}. \quad (4.109)$$

For slow flow, substitute  $V_0$  expressions to get  $f_c = 4.2/\text{Re}$ ; higher velocities get Ergun equation whose dimensionless version is:

$$f_c = \frac{4.2}{\text{Re}} + 0.292. \quad (4.110)$$

### Deformation Processing

- Non-Newtonian fluids, Viscoelasticity
- Deformation mechanisms: metals, polymers
- Stress-strain, sheet forming, stability
- Consolidation processes and mechanisms: sintering, HIP, compression molding