

18.440 problem set 7, due Wednesday, Nov. 9, 2005

Problems 1-4 from Ross are from the 7th Ed.; problem numbers in the 6th ed. were the same.

1. Chap. 6, Problem 24(a)-(c).
2. Chap. 6, Problem 40.
3. Chap. 6, Problem 41(a), (b).
4. Chap. 6, Problem 45. *Hints:* Show that the event whose probability we want is the union of three disjoint events which each have the same probability. Write  $(X, Y, Z) = (X_1, X_2, X_3)$ . If  $Z > X + Y$ , what must be true of  $X$  and  $Y$ ?
5. Let  $(X, Y)$  be uniformly distributed over the disk  $x^2 + y^2 \leq 1$  in the plane. So, its density function is  $1/\pi$  inside the disk and 0 outside it.
  - (a) What is the conditional density of  $Y$  given  $X = x$ ?
  - (b) What is the marginal density of  $X$ ?