

2 a) THERE ARE 10 SINGLE PARTICLE STATES INCLUDING SPIN.
 # 3-PARTICLE STATES = # WAYS OF CHOOSING 3 FROM 10
 WHEN ORDER DOES NOT MATTER = $10 \times 9 \times 8 / (3 \times 2 \times 1) = \underline{\underline{120}}$

b) $E = \Delta$: 2 ELECTRONS IN a, 1 IN b OR c \rightarrow 4 STATES
 $E = 1.5\Delta$: 2 ELECTRONS IN a, 1 IN d OR e \rightarrow 4 STATES

$$\underline{\underline{Z = 4e^{-\Delta/kT} + 4e^{-1.5\Delta/kT} + \dots}}$$

c) $E = 4.5\Delta$: 3 ELECTRONS IN d AND e \rightarrow 4 STATES
 $E = 4\Delta$: 2 ELECTRONS IN d AND/OR e \rightarrow 6 WAYS
AND 1 ELECTRON IN b OR c \rightarrow 4 WAYS
 $\Rightarrow 6 \times 4 = 24$ STATES

$$Z = \dots + \underline{\underline{24e^{-4\Delta/kT} + 4e^{-4.5\Delta/kT}}}$$

d) $k \ln 4$

e) $k \ln 120$

f) $C(T) \rightarrow 0$ $T \rightarrow \infty$ SINCE THE TOTAL ENERGY HAS AN UPPER BOUND
 UPPER BOUND

9-b) $E = 0$: ALL 3 BOSONS IN a \rightarrow 1 STATE
 $E = \Delta$: 2 BOSONS IN a, 1 IN b OR c \rightarrow 2 STATES

$$\underline{\underline{Z = 1 + 2e^{-\Delta/kT} + \dots}}$$

g-c) $E = 4.5D$: 3 BOSONS IN d AND/OR e \rightarrow 4 STATES
 $E = 4.0D$: 2 BOSONS IN d AND/OR e \rightarrow 3 WAYS
 AND 1 BOSON IN b OR c \rightarrow 2 WAYS
 $\Rightarrow 3 \times 2 = 6$ STATES
 $Z = \dots + \underline{\underline{6e^{-4D/RT} + 4e^{-4.5D/RT}}}$

g-d) $S(0) \rightarrow k \ln 1 = 0$

g-f) $C(T) \rightarrow 0$ SINCE THE TOTAL ENERGY HAS AN
 $T \rightarrow \infty$ UPPER BOUND

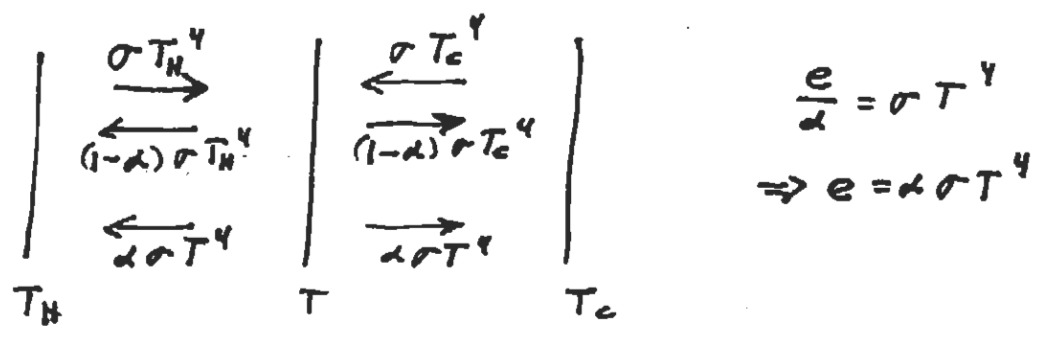
g-a) FOR INFORMATION ONLY!

THE TOTAL NUMBER OF STATES = THE # OF WAYS OF PUTTING 3 SPINLESS BOSONS IN 5 SPATIAL STATES = # WAYS OF PUTTING 3 BALLS IN 5 DIFFERENT BOXES WHEN ORDER DOES NOT MATTER = # WAYS OF ORDERING 3 BALLS AND 4 PARTITIONS WHEN THE ORDER OF THE BALLS DOES NOT COUNT

$$= \frac{7!}{(7-3)!} \times \frac{1}{3!} = \frac{7 \cdot 6 \cdot 5}{3 \cdot 2 \cdot 1} = \underline{\underline{35}}$$

IN PARTICULAR THERE ARE 5 WAYS OF PUTTING ALL 3 BOSONS IN THE SAME STATE, $5 \times 4 = \underline{20}$ WAYS OF PUTTING 2 IN 1 STATE AND 1 IN ANOTHER, AND $5 \times 4 / 2! = \underline{10}$ WAYS OF PUTTING EACH IN A SEPARATE STATE.

3 a)



$$T_H^4 - (1-\alpha)T_H^4 - \alpha T^4 = -T_c^4 + (1-\alpha)T_c^4 + \alpha T^4$$

$$\alpha T_H^4 + \alpha T_c^4 = 2\alpha T^4$$

$$T^4 = \frac{T_H^4 + T_c^4}{2}$$

b) $\sigma \alpha T_H^4 - \sigma \alpha T^4 = \alpha \sigma (T_H^4 - T^4) = \frac{\alpha \sigma}{2} (T_H^4 - T_c^4)$

J IN ABSENCE OF SHEET = $\sigma (T_H^4 - T_c^4) \equiv J_0$

$J_{SHEET} = \frac{\alpha}{2} J_0 = \underbrace{\left(\frac{1-\tau}{2}\right)}_{\sigma_f} J_0$

4 THE ENTROPY OF THE IDEAL PARAMAGNET DEPENDS ON H AND T ONLY THROUGH THE RATIO $\eta = \frac{\text{LEVEL SPACING}}{kT} \propto H/T$

ADIABATIC \Rightarrow CONSTANT S \Rightarrow CONSTANT H/T $\Rightarrow T \propto H$

$\frac{H_f}{H_i} = \frac{20}{8,000} = \frac{1}{400} \Rightarrow T_f = \frac{1}{400} T_i = \frac{1}{400} K = \underline{\underline{2.5 mK}}$

NOTE: SINCE THE SPIN SYSTEM IS USUALLY SATURATED AT THE BEGINNING OF SUCH AN EXPERIMENT, ARGUMENTS BASED ON THE CURIE LAW ARE NOT SUFFICIENT.