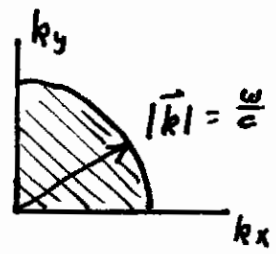


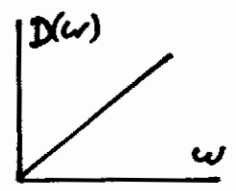
1. a) $\sin k_x L = 0 \Rightarrow k_x = n_x \frac{\pi}{L}$ $n_x = 1, 2, 3, 4 \dots$
 $\sin k_y L = 0 \Rightarrow k_y = n_y \frac{\pi}{L}$ $n_y = 1, 2, 3, 4 \dots$
 $\vec{k} = \frac{\pi}{L} (n_x \hat{x} + n_y \hat{y})$

b) $D(k) = \left(\frac{L}{\pi}\right)^2$ $\omega = c/|\vec{k}|$



$\#(\omega) = \left(\frac{L}{\pi}\right)^2 \frac{1}{4} \pi \left(\frac{\omega}{c}\right)^2$ { ONLY ONE POLARIZATION FOR \vec{E} IN THIS WORLD

$D(\omega) = \frac{d\#}{d\omega} = \frac{1}{2\pi} \left(\frac{L}{c}\right)^2 \omega$



c) $u(\omega, T) = \frac{1}{L^2} D(\omega) \langle \epsilon(\omega) \rangle = \frac{1}{L^2} D(\omega) \hbar \omega \langle n(\omega, T) \rangle$ HARMONIC OSCILLATOR
 $= \frac{\hbar \omega^2}{2\pi c^2} \frac{1}{e^{\hbar \omega/kT} - 1}$

d) $u(T) = \int_0^\infty u(\omega, T) d\omega = \frac{1}{2\pi \hbar^2 c^2} (kT)^3 \int_0^\infty \frac{x^2 dx}{e^x - 1}$ DIMENSIONLESS

$e(T) \propto u(T)$ FOR A BLACK BODY
 $e(T) \propto T^3$ IN THIS WORLD FOR BLACK BODY EMISSION

2. a) $e^{ik_x(x+L)} = e^{ik_x x} \underbrace{e^{ik_x L}}_1 = e^{ik_x x}$
 $\Rightarrow k_x = n_x \frac{2\pi}{L} \quad n_x = 0, \pm 1, \pm 2 \dots$
 SAME FOR k_y

$\vec{k} = \frac{2\pi}{L} (n_x \hat{x} + n_y \hat{y}) \quad n_i = 0, \pm 1, \pm 2 \dots$

b) $D(\vec{k}) = \left(\frac{L}{2\pi}\right)^2$ FOR ALL \vec{k}

c) $\#(\epsilon) = 2 \overset{\text{SPIN}}{D(\vec{k})} \left(\frac{2\epsilon}{\gamma}\right)^2$

$D(\epsilon) = 2 \left(\frac{L}{2\pi}\right)^2 \frac{8}{\gamma^2} \epsilon = \underline{4 \left(\frac{L}{\pi\gamma}\right)^2 \epsilon}$

d) $N = \#(\epsilon_F) = \frac{8L^2}{(2\pi)^2} \left(\frac{\epsilon_F}{\gamma}\right)^2$

$\epsilon_F = \left(\frac{1}{2} \pi^2 \gamma^2 \left(\frac{N}{A}\right)\right)^{1/2}$

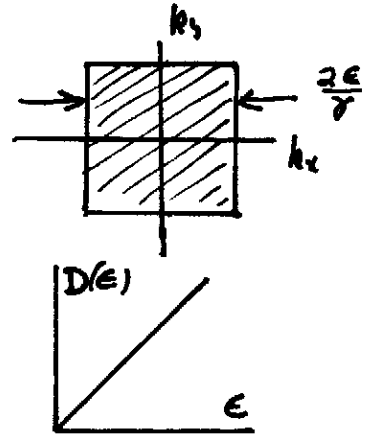
e) $D(\epsilon) = \alpha \epsilon \quad N = \int_0^{\epsilon_F} \alpha \epsilon d\epsilon = \frac{\alpha}{2} \epsilon_F^2$

$E = \int_0^{\epsilon_F} \alpha \epsilon^2 d\epsilon = \frac{\alpha}{3} \epsilon_F^3 = \underline{\frac{2}{3} N \epsilon_F}$

f) STILL T'

g) $dE = T dS + S dA$
 (Note: An arrow points from the text "0 AT T=0" to the T in the equation above.)

$S = \frac{dE}{dA} = \frac{2}{3} N \frac{d\epsilon_F}{dA} = \frac{2}{3} N \left(-\frac{1}{2}\right) \frac{\epsilon_F}{A} = \underline{-\frac{1}{3} \left(\frac{N}{A}\right) \epsilon_F}$



$$3. \quad a) \quad Z_1 = e^{\mu_0 H / RT} + 2 + e^{-\mu_0 H / RT} = \underline{2(1 + \cosh(\mu_0 H / RT))}$$

$$b) \quad E = N \langle \epsilon \rangle = N \frac{-\mu_0 H e^{\mu_0 H / RT} + 0 + \mu_0 H e^{-\mu_0 H / RT}}{Z_1}$$

$$= \underline{-\mu_0 H N \frac{\sinh(\mu_0 H / RT)}{1 + \cosh(\mu_0 H / RT)}}$$

$$c) \quad M = N \langle \mu_z \rangle = N \frac{\mu_0 e^{\mu_0 H / RT} + 0 - \mu_0 e^{-\mu_0 H / RT}}{Z_1}$$

$$= \underline{\mu_0 N \frac{\sinh(\mu_0 H / RT)}{1 + \cosh(\mu_0 H / RT)}}$$