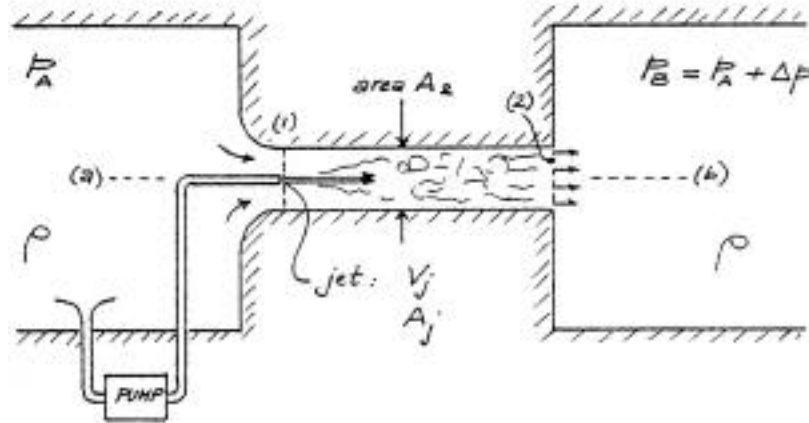


## Problem 5.8

### Jet pump



The device connected between compartments A and B is a simplified version of a jet pump. A jet (or ejector) pump is a device which uses a small, very high-speed jet with relatively low volume flow rate to move fluid at much larger volume flow rates against a pressure differential  $\Delta p$ , as shown in the figure.

The pump in the figure consists of a contoured inlet section leading to a pipe segment of constant area  $A_2$ . A small jet draws fluid from compartment A and ejects it at high velocity  $V_j$  and area  $A_j$  at the entrance plane (1) of the constant-area pipe segment. Between (1) and (2), the jet (the "primary" stream) and the secondary fluid flow which is drawn in from compartment A via the contoured inlet section mix in a viscous, turbulent fashion and eventually, at station (2), emerge as an essentially uniform-velocity stream. The pump operates in steady state.

To simplify the analysis, we make several physical assumptions that are not unreasonable. We assume

- that the flow is incompressible
- that the flow from compartment A to station (1) is inviscid,
- that, although viscous forces cause the turbulent mixing process between (1) and (2), the shear force exerted on the walls between those stations is small compared with  $\Delta p A_2$ ,
- that gravitational effects are negligible, the flow being horizontal.

We also make two assumption about operating conditions that are also reasonable and considerably simplify the mathematics involved in the analysis:

$$A_j \ll A_2 \quad \text{and} \quad V_j A_j \ll V_2 A_2$$

(a) Derive an expression for  $\Delta p$  as a function of the total volume flow rate  $Q$  from compartment A to compartment B. The given quantities are  $A_1$ ,  $A_2$ ,  $\rho$  and  $V_j$ . Indicate the volume flow rate  $Q_0$  when  $\Delta p = 0$  (the "short-circuit" volume flow rate) and the pressure  $p_0$  at which  $Q = 0$ . Write the pressure-volume flow rate relationship in universal dimensionless form as  $p/p_0$  vs  $Q/Q_0$  and sketch it for positive values of pressure. This is the "pump curve" in dimensionless form.

Show that for  $A_j \ll A_2$ ,  $Q_0 \gg V_j A_j$ .

HINT

HINT 2

HINT3

ANSWERS

(c) Sketch the pressure distributions along the line a-b for the cases  $\Delta p = 0$  and  $\Delta p > 0$ .

ANSWER

(d) Is your formulation in (a) valid when  $Q=0$ , i.e. when the total volume flow rate from A to B is zero? Explain. What is the minimum value  $Q_{min}$  of  $Q$  for which your formulation in (a) is valid?

ANSWER