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IID INFLUENCE OF TIME ON STRESS-STRAIN-STRENGTH BEHAVIOR OF CLAYS DURING UNDRAINED SHEAR

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Sheet A1,2 } Data from Sheahan et al. (1996) from CK_0 UC vs $\dot{\epsilon}$ vs $f(OCR)$
 Sheet B } for resedimented BBC

22-141 50 SHEETS
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5. Undrained Creep

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Sheet C1, 2 Data on creep rupture and unique $\log \dot{\epsilon}_m$ vs $\log t_m$

" D Data on Correspondence

" E1, 2 Data on relaxation

IID: INFLUENCE OF TIME ON STRESS-STRAIN-STRENGTH BEHAVIOR OF CLAYS DURING UNDRAINED SHEAR

1. INTRODUCTION

1.1 Definitions

a) Prior to shear

a) at constant w (UU): thixotropy

b) At constant σ' (CU, CD): "aging" \equiv secondary compression

2) During shear (undrained)

a) Rate of strain, $\dot{\epsilon}$, as increase q

b) Time after applying constant q = creep

c) " " " " ϵ = relaxation

1.2 Comments on Drained Behavior

• For drained shear, $\dot{\epsilon}$ (or t_s) believed to have little effect on c' , ϕ' for "ordinary" clays.

• But NOT for Highly Structured Cemented clays - see Section 4.4

2. THIXOTROPY (Mitchell, 1960 & 1993; O'Neill, 1985)

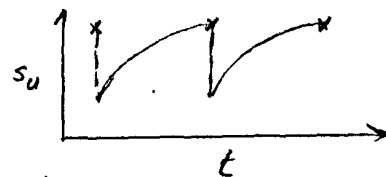
ASCE, JSMIFD 84(3)

Both

MIT SM them

2.1 Definition

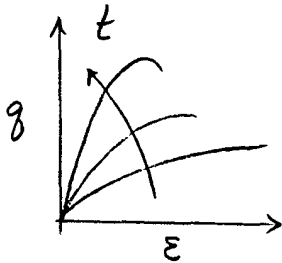
• With some clays, if remold and then store at constant composition \rightarrow incr. stiffness & strength



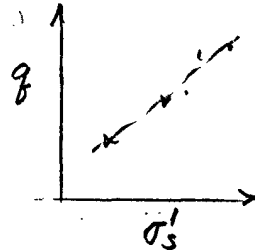
• Thixotropy = isothermal, reversible, time-dependent process occurring under conditions of constant composition & volume whereby a material stiffens while at rest and softens or liquefies upon remolding

2.2 Behavior Measured in UUC Tests

1) Based on limited published data.



plus maybe



- PhD Berkeley on slurries of clay
- SM MIT UUC -1960 ±
(But not OON, 85)

2) Comments

- Storing disturbed tube samples may → incr. s_u w/ t
- No correlation $TSR = s_u(t) / s_u(R)$ and soil type, but restricted to clays and generally more important with increasing I_L

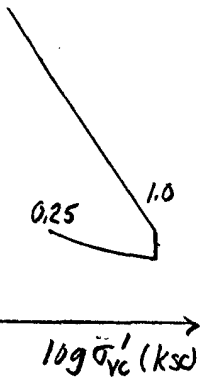
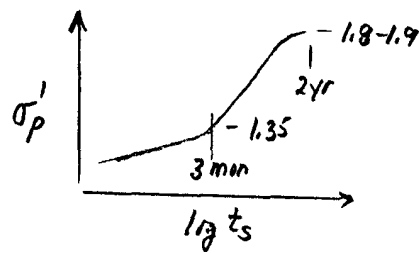
2.3 O'Neill (1985) - Behavior of Block Samples of Resedimented BBC II

Batch $\sigma'_{vm} = 1 \text{ ksc} + t_c/t_p = 1 \text{ cycle}$
 & rebounded to $\sigma'_{vc} = 0.25 \text{ ksc}$

1) See p2a for oedometer:

$\sigma'_p \approx \log t_s$ (t_s = storage time)

- 1 week → $\sigma'_p = 1.1$ (expected)
- 3 mm → $\sigma'_p = 1.35$
- 2 yr. → $\sigma'_p = 1.9$



2) During this period

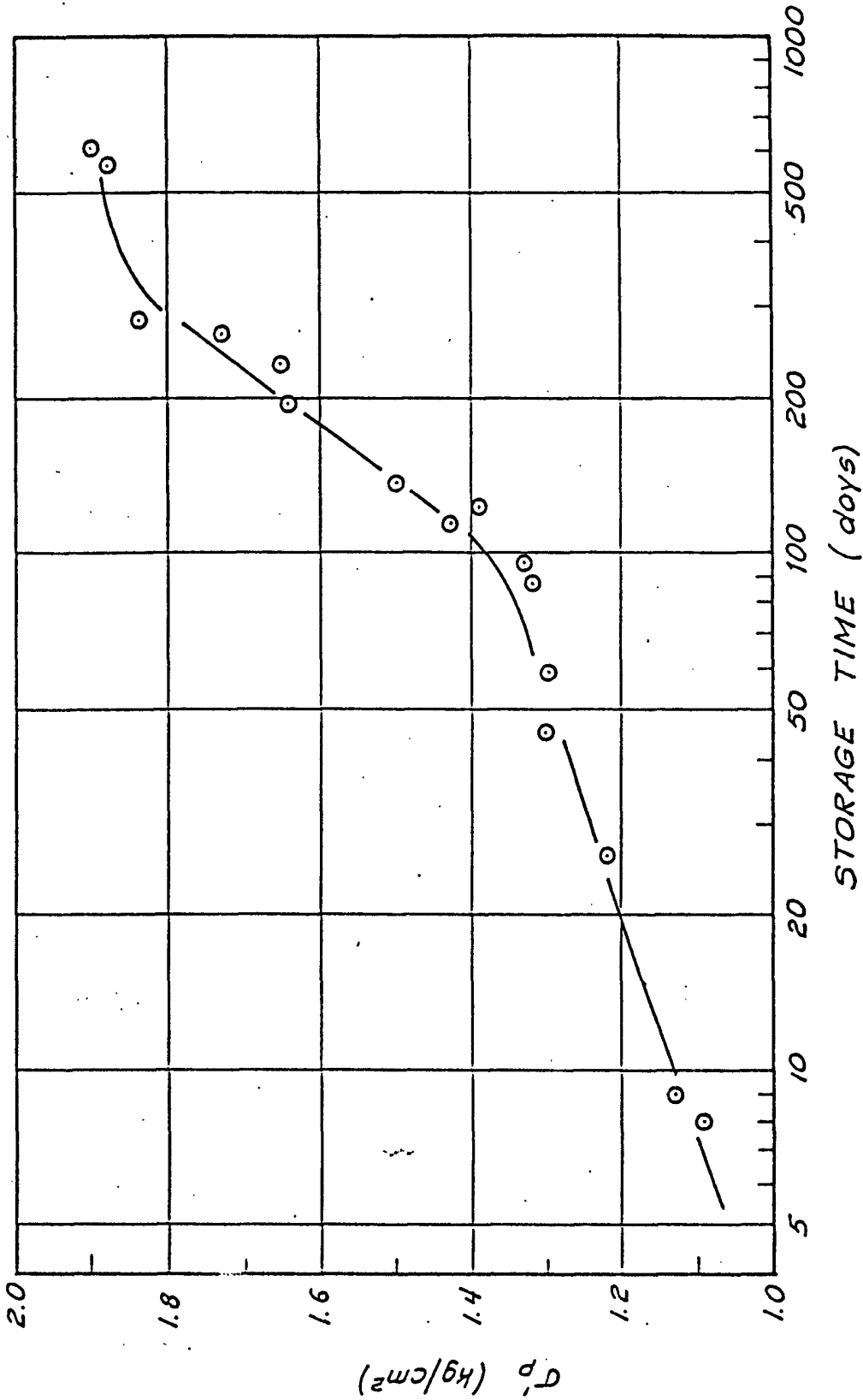
- $D_w \approx 0$
- Very little increase σ_s
- Consistent increase in q_f Recompression $CK_{UC/E}$ of same magnitude & largely due to Δu_s (see p2a)

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p2a



MIT Special Program (1985)
1-605
Figure 6-1 Effect of Thixotropy on Preconsolidation Pressure of Resedimented Boston Blue Clay (after O'Neill, 1985)

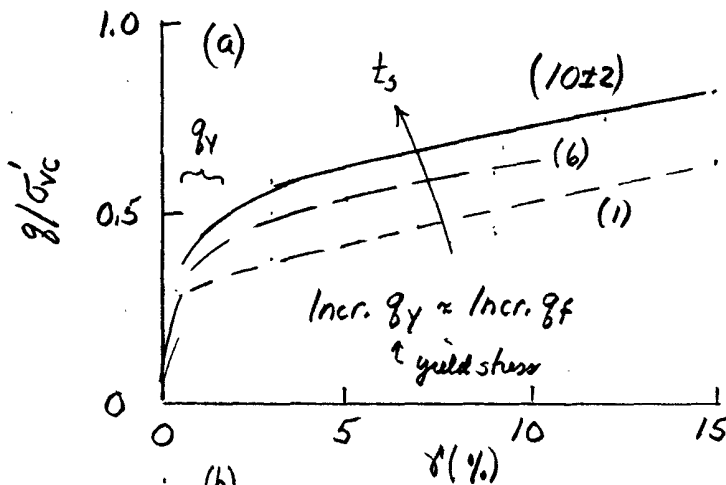
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O'Neill (1985)

Recompression CK_0UC/E Resed. BBC

(OCR = 4 prior to thixotropy)

$\sigma'_{vc} = 0.25 \text{ ksc}$

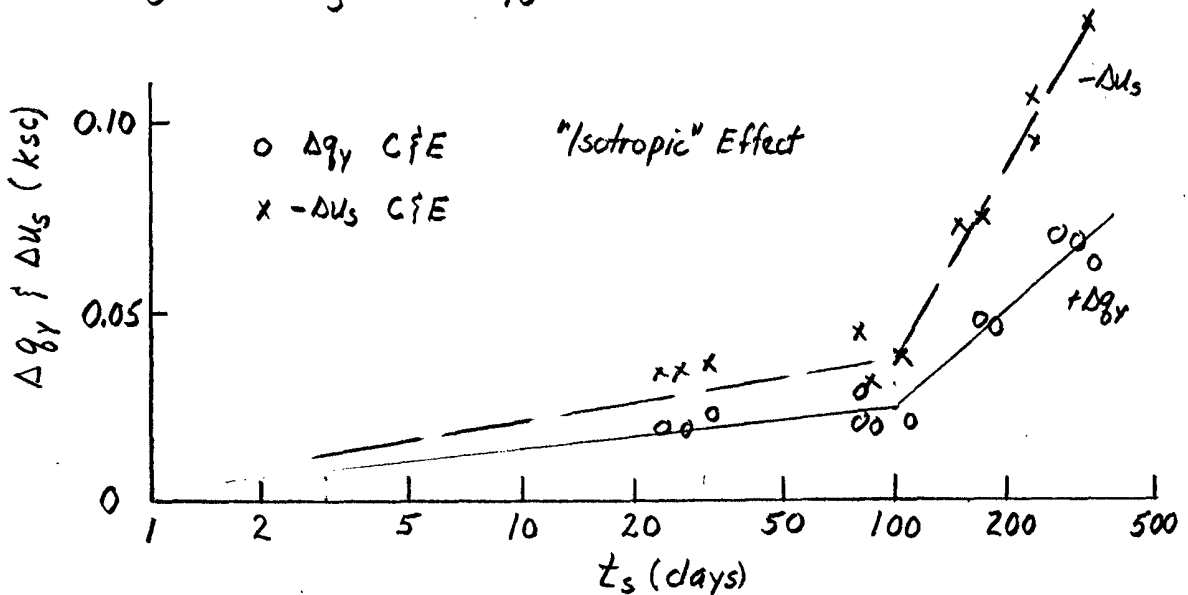
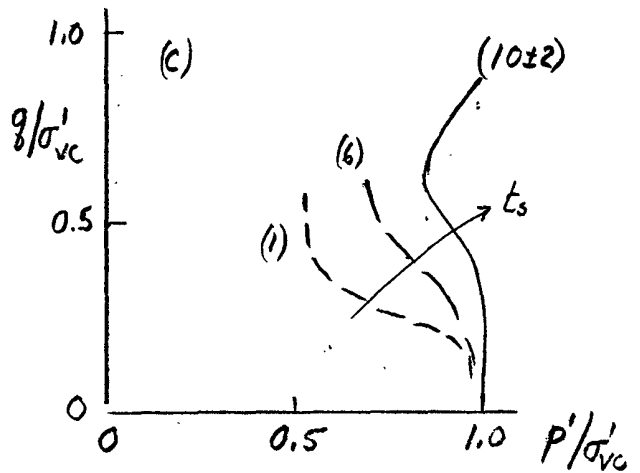
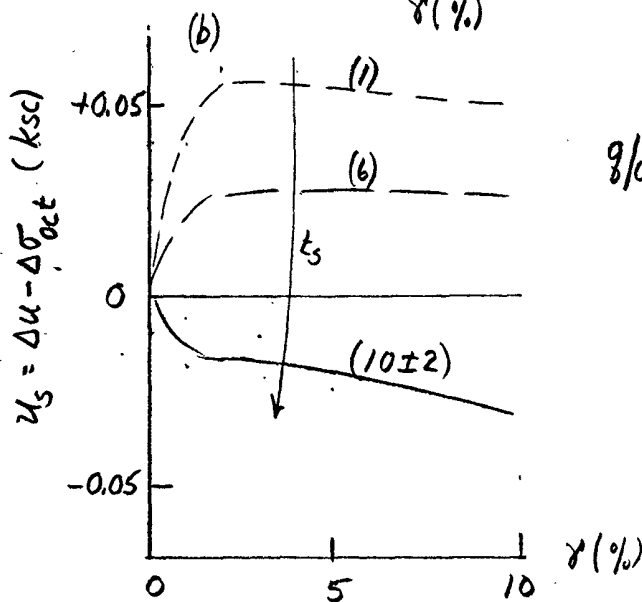


(a) (b) & (c)

CK_0UE

(t_s , mon)

NOTE: Incr. q largely due to reduced $u_s = \Delta u - \Delta \sigma'_{oct}$



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2.4 Possible Mechanisms

1) Reorientation of clay particles (Mitchell, 1976 {1993})
 from "dispersed" → "flocculated". (Δ fabric and interparticle forces)

• Presumably $\bar{A} > \bar{R}$ and/or $\bar{\sigma}_a > \bar{\sigma}_r$

• Berkeley data supposed to show that occurs in compacted clays → large increase in $k' w/t!$

2) Water "structure": Decrease in 'free energy' of adsorbed H₂O → decreasing u → increasing σ'_s

• CCL tested before BBC data became available

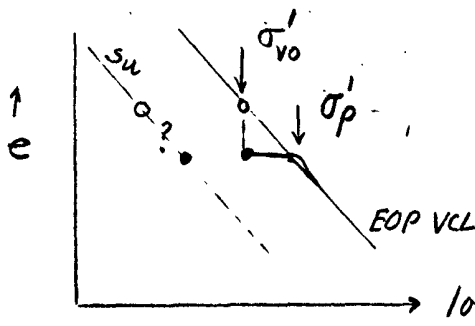
3) "Bugs" (RTM)

4) Conclusions: Mechanism(s) unknown

But some clays (especially at high IL) certainly decrease stiffer with time

3. AGING = SECONDARY COMPRESSION

3.1 Review from Treatment of Consolidation



$$\log \frac{\sigma'_p}{\sigma'_{vo}} = \frac{C_{de}}{C_c} \log(t/t_p)$$

$$\frac{C_{de}}{C_c} = \frac{C_{de}}{C_c} = 0.045 \rightarrow \approx 10\% \text{ increase}$$

in OCR per log cycle secondary compression. Does s_u increase by same amount?

Jevin "fact" (à la Mesri) that $C_{de}/C_c = 0.045 \pm 0.015$ for most cohesive soils (Both OC & NC)

• Only important at low OCR (ie. "high" $C_c \rightarrow$ high C_d)

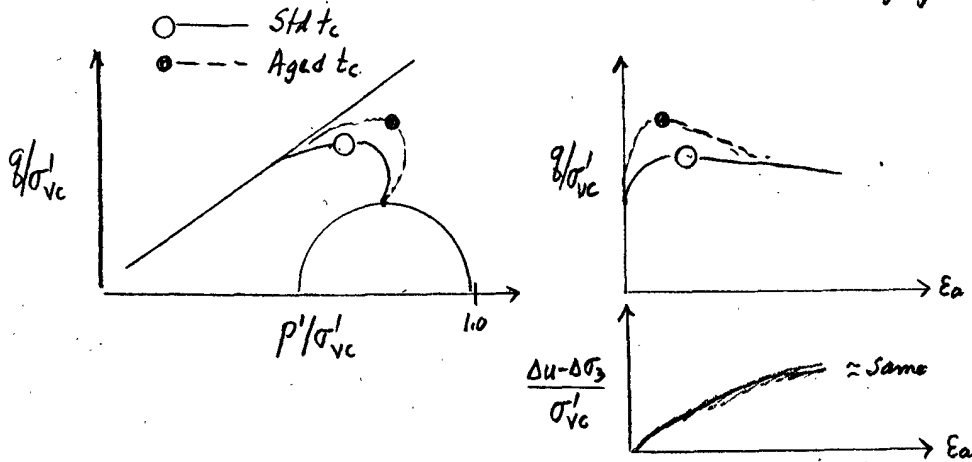
{ Should not vary in consistent fashion }
 with changes in I_p

∴ Tokyo Fig. 39 very suspect

3.2 Influence on CAUC Tests (OCR=1)

(Byerum & Lo 1963; Ladd 1965; Vaid & Campanella 1977)

Note: Aging at constant K_c



1) Aging leads to:

- a) Modest increase in q/σ'_{vc} , say $\approx 5-7\% / \Delta \log t_c$
- b) Large increase in E_u/σ'_{vc} (Ladd 1965 reports $60 \pm 10\% / \Delta \log t_c$ from CIUC tests)
- c) Perhaps decrease in E_f

2) If same Δu vs E_a , then:

- a) Lower shear induced $u_s = \Delta u - \Delta \sigma_{oct}$ (consistent with incr. OCR)
- b) Increased resistance at particle contacts since same Δu vs E_a implies same displacement at contacts

3) Behavior of aged vs. mechanical precompression at same OCR?

Aging probably \rightarrow stiffer initial response (i.e., higher E_u)

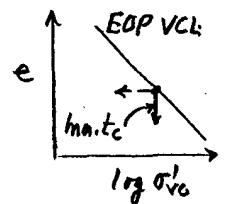
3.3 MIT Standard Practice for SHANSEP Testing

Perform CK₀U tests after $t_c \approx 1$ day ($\log t_c / t_p \approx 1 \rightarrow \approx 1$ log cycle)

- 1) Minimize Δu due to "stopping" secondary compression \rightarrow
- 2) Standard $t_c \rightarrow$ more consistent data

3) To instill some "structure" in the clay (i.e., make stiffer) that was destroyed by consolidation beyond in situ σ'_p

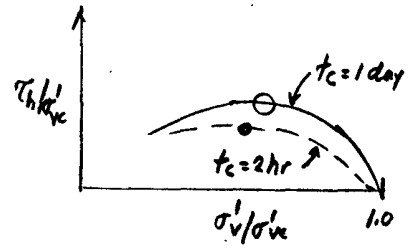
NOTE: Empirical aspect of SHANSEP. Also actual OCR is slightly higher than reported (since aging increases σ'_{vm})



3.4 Influence of Consolidation Time on C_{k0} UOSS Data

- 1) As per 3.3, SHANSEP C_{k0} U tests typically use $t_c = 1$ day at test σ'_{vc} (i.e. test σ'_{vm}) when attempting to predict in situ undrained shear behavior of naturally OC clays.
- 2) However, during staged construction, foundation clay is still undergoing consolidation, i.e., presumably lies on t_p (EOP) compression curve. Therefore there will not be any "aging" (secondary compression).
- 3) Following compares $t_c = 1$ day vs $t_c = 2$ hr ("EOP") for two plastic soils at Peak strength (each average of 2 tests) at $\dot{\epsilon} = 5\%/hr$

Soil	t_c	$\gamma_f(\%)$	Z_h/σ'_{vc}
Fresh Kills, NY Organic Silt ($I_p = 60\%$)	1 day	11.5 ± 0.5	0.296 ± 0.018
	2 hr	14.1 ± 4.9	0.257 ± 0.020
Sergipe, Brazil offshore CH ($w_n = 65\%$)	1 day	9.4 ± 0.2	0.2385 ± 0.0035
	2 hr	$\approx 7.6^3$ ± 0.9	0.2163 ± 0.0667



→ -13%

} Avg. = -10.5%

NOTE: For $\dot{\epsilon} = 0.5\%/hr$, reduction → -11.8%

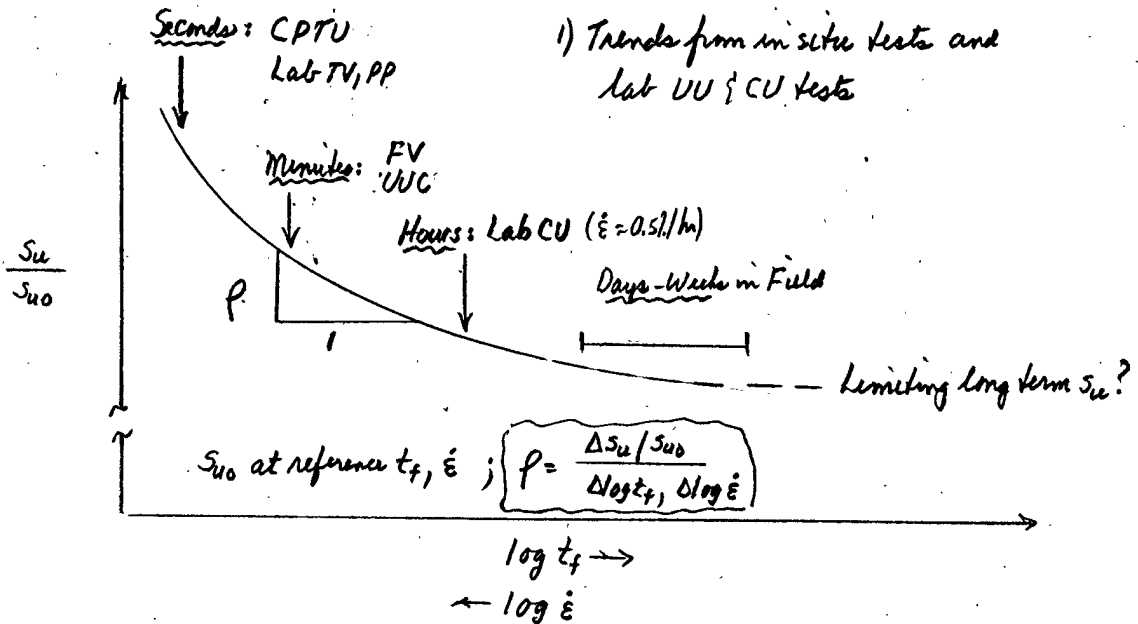
- 4) Effect is significant: Therefore should use $t_c = t_p$ (EOP) to obtain s_u/σ'_{vc} for $OCR=1$ "underconsolidated" soil.



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4. EFFECT OF STRAIN RATE

4.1 OVERVIEW



1) Trends from in situ tests and lab UU & CU tests

2) Reported values of p and comments [also see Sheahan et al. 1996, JGE, 122(2)]

a) Most of the early (<1970) data came from UUC tests \rightarrow unknown OCR

b) Most CU data with known OCR from CIUC tests

NC Typical $p \approx 10 \pm 5\%$; $t_f \approx 1 \text{ min} \rightarrow 1 \text{ week}$

High OCR " " $\approx 15\%$; $t_f \approx 5 \text{ min} \rightarrow 1 \text{ week}$

[Note: Undisturbed CL-ML Hays Clay, $C_{k0}UC$ at OCR = 10-40 $\rightarrow p \approx 30-35\%$!
(Andersen & Stenhamar, 7/82, JGE)]

3) Implications when comparing S_u data having different $t_f / \dot{\epsilon}$

a) Compare UUC at $\dot{\epsilon} = 1\%/min$ vs $C_{k0}UC$ at $\dot{\epsilon} = 0.51/h \rightarrow 2 \log$ cycles

b) $\Delta q_f \approx 20 \pm 10\%$ for $p = 10 \pm 5\%$ at low OCR

" $\approx 30-60\%$ for $p = 15-30\%$ at high OCR

4) Extreme case: Offshore Alaska at Smith Bay; CL-CH Pleistocene clay

S_u (UUC, FV & CPTU) = $3 \times S_u$ (DSS)

from SHANSEP with well defined

σ'_{v0} & σ'_p profiles

$H_k = 15$
 $I_p = 25\%$, $T = -1^\circ C$

$z = 1-5.5 \text{ m}$

OCR = 40-8

Young (1986), MIT
SM thesis

22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS

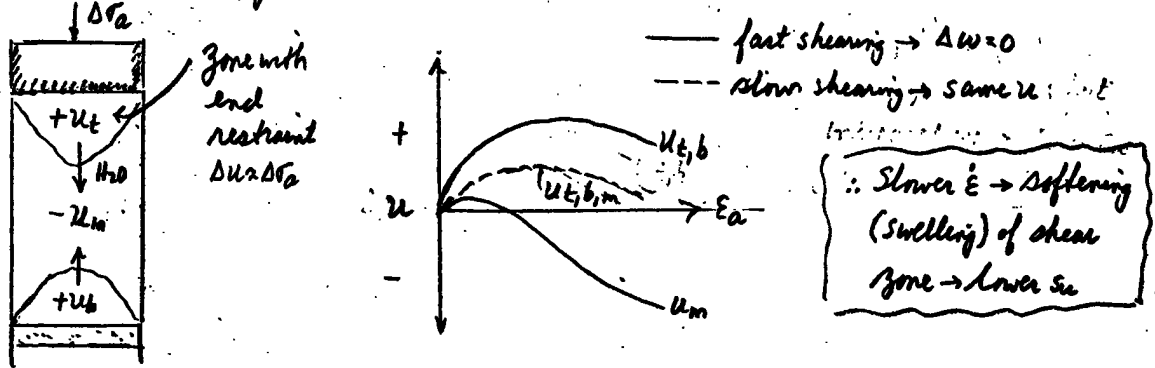


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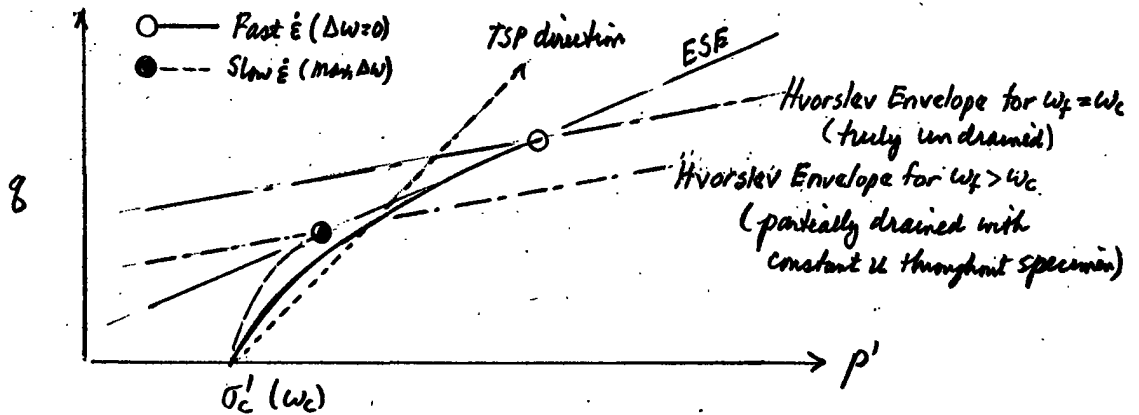
4.2 Results from CIUC Tests at High OCR: Fixed End Caps

NOTE: Also applies to UUC testing at varying $\dot{\epsilon}$

1) Overview of problem (also see Notes on measurement of c' & ϕ' , IB)



2) Results on OCR=16 CH clay [Richardson & Whitman 1963, test 13(4)] → CCL reinterpretation
 CIUC with u_m (at middle → correct ESP)



3) Conclusions:

a) Regular UC/CU tests at varying $\dot{\epsilon}$ on high OCR clay are partially drained; hence dec. in s_u at slower rates due in part to softening of shear zone

b) Need lubricated end caps to measure correct Δs_u vs $\Delta \epsilon$

c) Will in situ shearing of high OCR clay also → softening of potential shear zone, and hence lower s_u ?

CCL doesn't know, but probably possible (need to study literature)

22-141 50 SHEETS
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4.3 Results from CK_0UC Test on RBBG at $OCR=1, 2, 4, 8$:

Lubricated End Caps and Mid-Specimen U Data

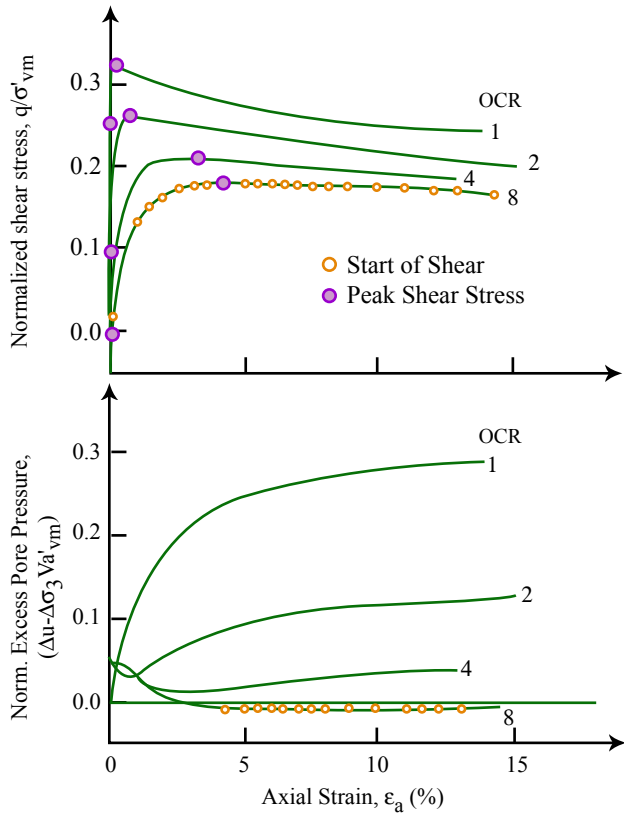
[Sheahan 1991 MIT ScD thesis; Sheahan et al. 1996, JGE, 122(2)]

1) Test Program

- 1st MIT automated TX cells, $\dot{\epsilon} = 0.05, 0.5, 5 \text{ \& } 50\%/hr$
- $P_{0.5} = (\Delta\sigma_u / \sigma_{u0}) / \Delta \log \dot{\epsilon}$, where σ_{u0} at $\dot{\epsilon} = 0.5\%/hr$.

• Cell fluid = oil to prevent membrane leakage

22-141 50 SHEETS
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Typical normalized shear stress and excess pore pressure versus strain for CK_0UC tests on resedimented BBC at reference strain rate ($\epsilon_a = 0.5\%/h$)

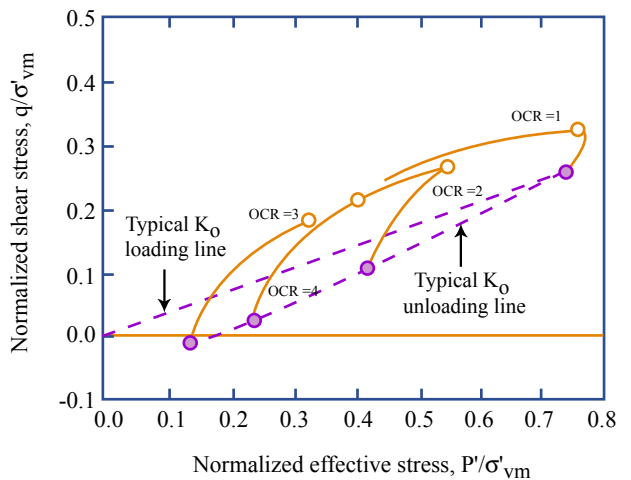
• Measured α both at base & ϵ probe

2) Behavior at reference $\dot{\epsilon} = 0.5\%/h$

• See Fig. 152

• Note that data normalized to σ'_{vm}

OCR	q/σ'_{vm}	P/σ'_{vm}	$E_f(\%)$
1	0.322	0.761	0.15
2	0.2615	0.552	0.7
4	0.2135	0.448	3.0
8	0.180	0.3285	4.2



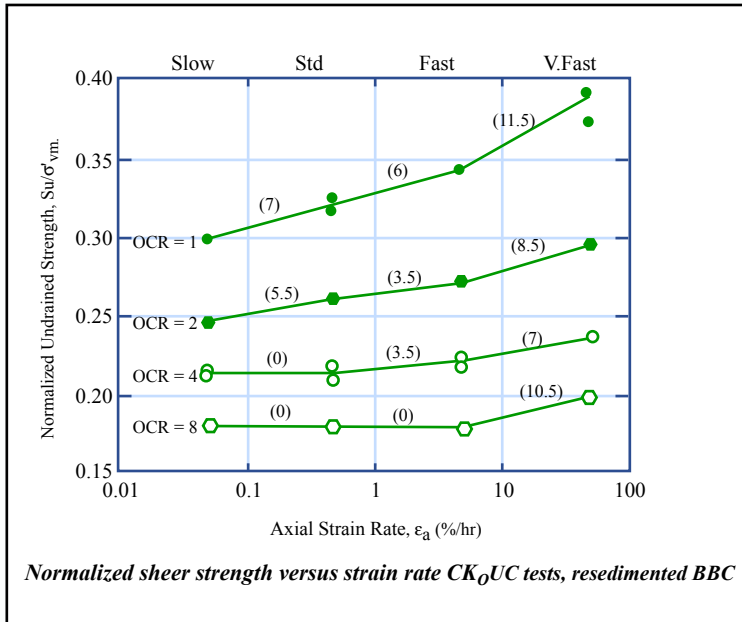
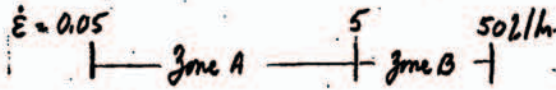
Typical normalized effective stress paths for CK_0UC tests on resedimented BBC at reference strain rate ($\epsilon_a = 0.5\%/h$)

- Peak shear stress
- Start of Shear

4.3 Cont

3) Overview of effects on s_u

a) $s_u/\sigma'_{vm} \approx \log \dot{\epsilon}$ as f(OCR): Fig 11



Normalized shear strength versus strain rate CK₀UC tests, resedimented BBC

Figure by MIT OCW.

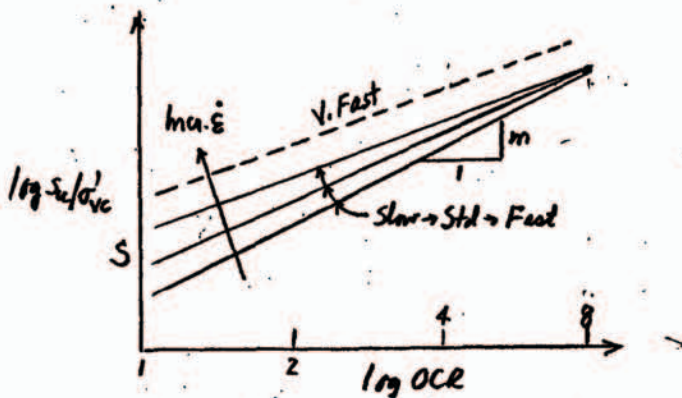
b) $\log s_u/\sigma'_{vc} \approx \log OCR$ as f($\dot{\epsilon}$): Table 4

TABLE 4. SHANSEP Parameters for BBC at Different Strain Rates

Strain rate $\dot{\epsilon}_a$ (%/h) (1)	S^a (2)	m^b (3)	r^2 (4)	Number of observations n (5)
0.05	0.298	0.757	0.9997	6
0.5	0.320	0.714	0.9993	6
5	0.340	0.689	0.9997	5
50	0.373	0.686	0.9984	8

^a S = value of s_u/σ'_{vc} at OCR = 1, based on regression analysis.

^b m = strength increase exponent [refer to Eq. (3)].



Zone B (Fast → Very fast)

• get effect at all OCR that is \approx constant

• $P_{as} = 9.4 \pm 2.0\%$

Zone A (Slow → Fast)

• P_{as} decreases with increasing OCR (1st data to show this!)

• P_{as} goes to zero with increasing OCR more rapidly at lowest $\Delta \log \dot{\epsilon}$ range.

Complex trends

• Slow → Fast $\dot{\epsilon}$ → increasing S / decreasing m

• Fast → Very Fast $\dot{\epsilon}$ → increasing S at constant m

22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS



4.3 Cont.

4) Overview of effects on stress-strain & ESP behavior

a) Shear stress vs ϵ_a

- See Sheet A1 & A2 for q/σ'_{vc} vs $\epsilon_a \rightarrow$ very consistent trends
- Fig. 12 of sheet B shows that normalized D_g/D_{gmax} vs ϵ_a is unique at OCR = 2, 4 & 8 (very important for soil modeling).

Post peak behavior at OCR = 1 is scattered

b) Pore pressure vs ϵ_a

- Look at shear induced: $\Delta u_s = \Delta u - \Delta \sigma'_{oct} = \Delta u - \frac{1}{3} \Delta \sigma'_a \approx \epsilon_a$
- on sheets A1 & A2

• Increases in s_u are always accompanied by lower Δu_s

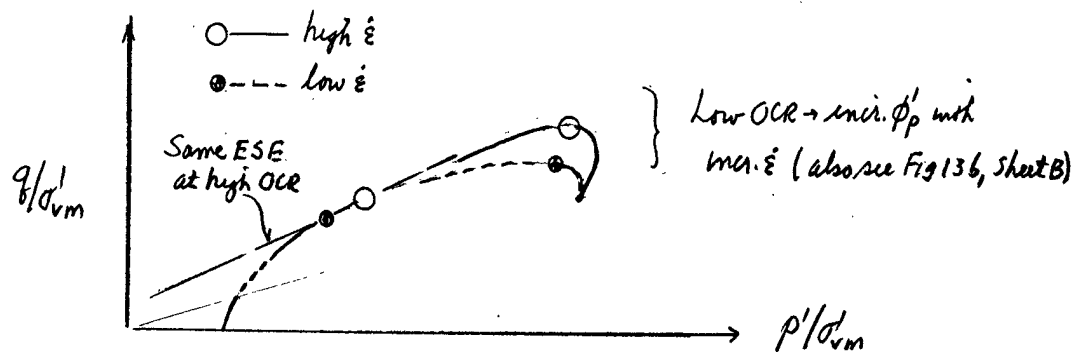
(also see Fig 13a, Sheet B), e.g.

OCR = 1, increasing $\dot{\epsilon} \rightarrow$ incr. s_u & decr. Δu_s

OCR = 8, $\dot{\epsilon} = 0.05$ to 5, $\Delta s_u = 0 \rightarrow$ no change in Δu_s

c) Effective stress paths and failure envelopes

- See Sheets A1 & A2 for ESP \rightarrow consistent trends



OCR = 1 & 2 • Low OCR: Increased s_u due to both lower Δu_s & higher ESE (ϕ'_p)

OCR = 4 & 8 • High OCR: Increased s_u due only to lower Δu_s (same ESE)

4.3 Cont

5) Summary of CK₀UC testing program on RBBC (practical implications for non-structured clays)

a) Very fast shearing \rightarrow increased s_u that is \approx constant at all OCR ($P_{0.5} \approx 10\%$). Applies to in situ testing & lab VUC, TV etc.

b) At slower strain rates, strain rate sensitivity ($P_{0.5} > 0$) decreases with increasing OCR.

Hence for field loading, would not expect design s_u of moderate to high OCR clays to be $<$ measured lab CK₀U testing

c) Strain rate sensitivity (incr. in s_u with incr. $\dot{\epsilon}$) is caused by two mechanisms:

1) Increasing $\dot{\epsilon} \rightarrow$ decreasing Δu_s : Occurs at all OCR

2) Increasing $\dot{\epsilon} \rightarrow$ increase in ESE at peak strength : Occurs only at low OCR

• at OCR ≤ 2 , + $P_{0.5}$ due to both decreased Δu_s & incr. ϕ_p

• at OCR ≥ 4 , + $P_{0.5}$ due only to decreased Δu_s

d) At OCR > 1 , obtain unique $\Delta q / \Delta q_{max} \approx \epsilon_a$ independent of $\dot{\epsilon}$ (simplified modeling)

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4.4 Behavior of Highly Structured (Cemented-Sensitive) vs "Ordinary" Clays

1) Observations from 1-D Consolidation Data

- Hypothesis A
- Unique ϵ vs $\log \sigma'_{vc}$ during primary, (i.e. independent of $\dot{\epsilon}$)
 - Appears reasonable for saturated clays of low-moderate S_t
 - Same mechanisms cause creep as occur during primary, e.g. slippage at particle contacts

- Hypothesis B
- Unique $\epsilon - \dot{\epsilon} - \sigma'_{vc} \rightarrow$ same ϵ vs $\log \sigma'_{vc} / \sigma'_p(\dot{\epsilon})$
 - Better model for high $I_L - S_t$ Canadian clays
 - "Structural Viscosity" due to time dependent strength of cementation bonds (true cohesion) } CCL

2) CU Test Programs at Varying $\dot{\epsilon}$ by Lefebvre & LeBoeuf (1987)

- 5 block samples from 3 sites, $I_p = 10 \pm 3$ to 40% , $I_L = 2.3 \pm 0.6$
- $\sigma'_p = 140 \pm 45 \text{ kPa}$

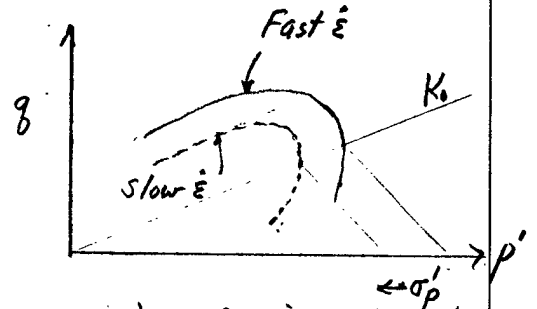
a) CU Tests on INTACT Clay, $\sigma'_{vc} = \sigma'_{v0}$ (see p12a)

- Approx same Δu vs ϵ up to peak S_u at $\epsilon_f < 1\%$, and hence \approx same pre-failure ESP

- Lower S_u with decr. $\dot{\epsilon}$ due to lower yield stress = failure envelope

- Attributed to rate dependent cementation bonds

("structural viscosity" of cohesion component à la Bjerrum, 1973)

b) CU Tests on DESTRUCTURED Clay, $\sigma'_{vc} > \sigma'_p$ (see p12b)

- Decreasing $\dot{\epsilon} \rightarrow$ higher Δu \therefore Lower S_u due to lower p'_f (and also lower ϕ'_p for CAUC tests à la RBBC)

NOTE: Both test series \rightarrow same p' (Fig 1b, p12b), but
due to different mechanisms.

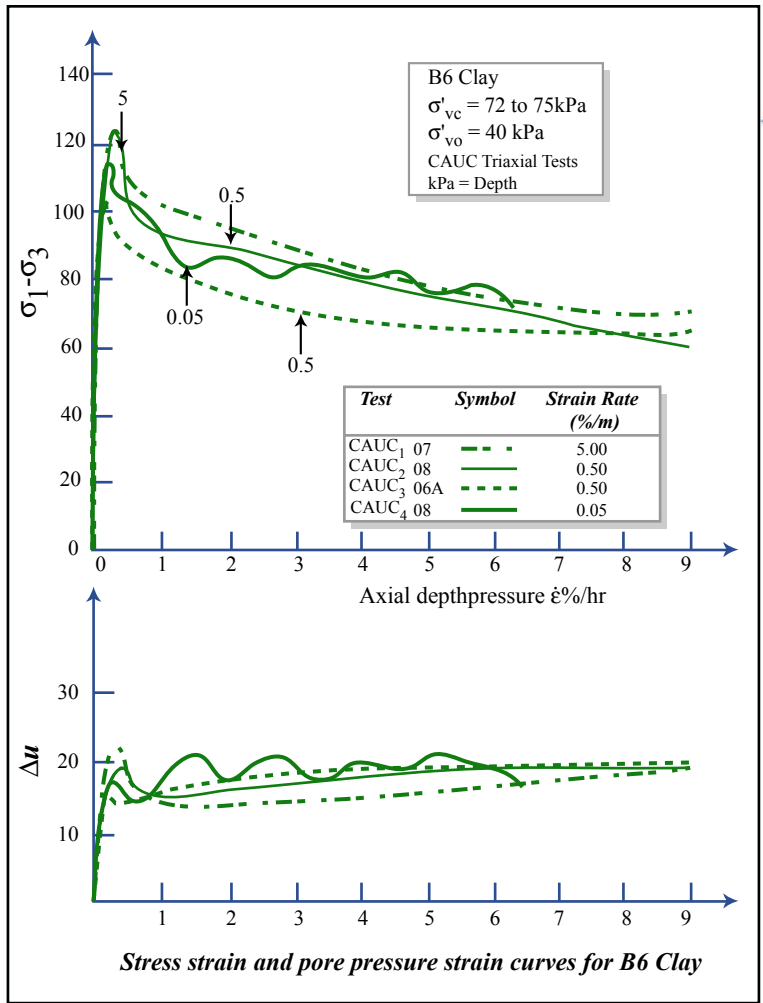
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Lefebvre & LeBoeuf (1987) JGE, ASCE 113(5)

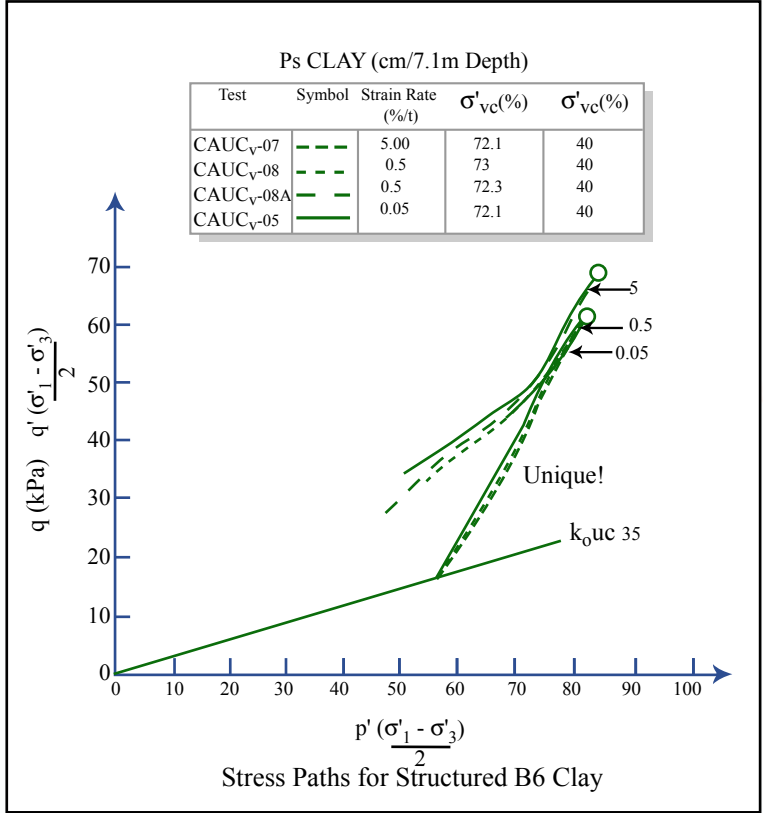
CU Test Data on "Intact" Highly Structured Clay ($\sigma'_{vc} \approx \sigma'_{vo}$)

42 SHEETS 5 SQUARE
42 SHEETS 100 SHEETS 5 SQUARE
42 SHEETS 200 SHEETS 5 SQUARE
NATIONAL
MANUFACTURING U.S.A.

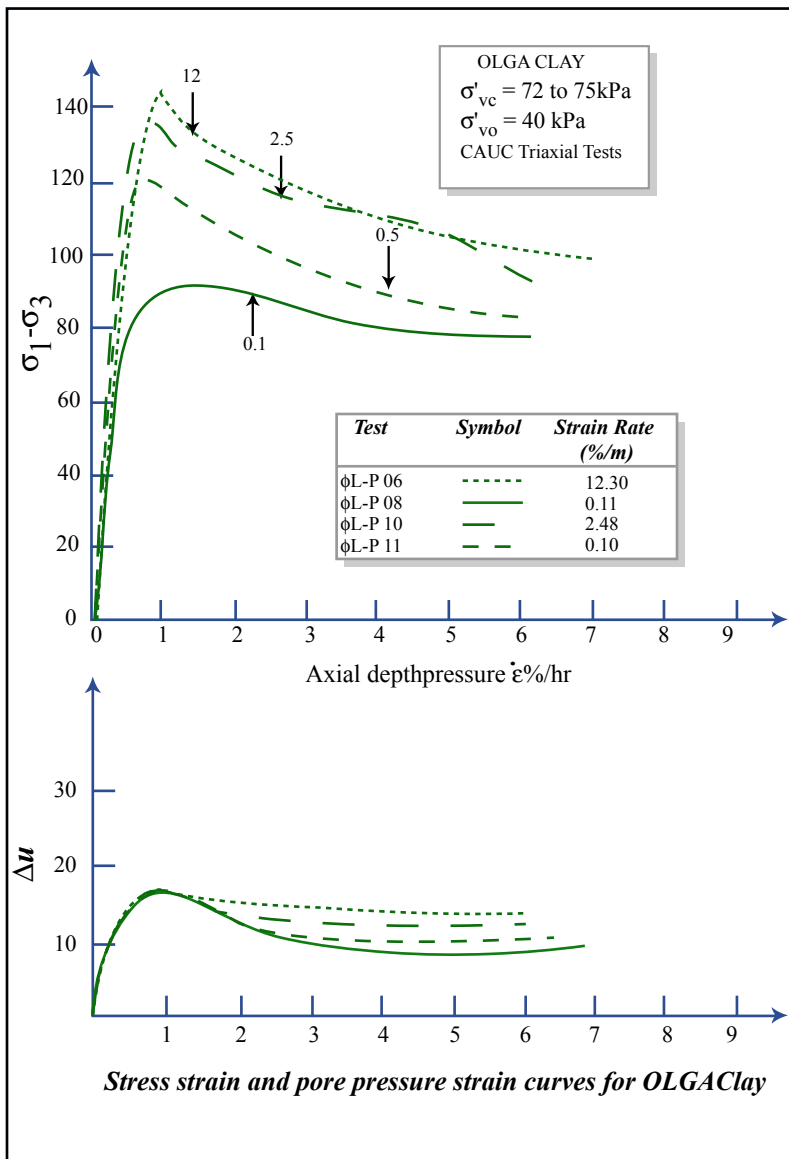
Note: Vaid et al (1979, CGS, 16(1)) observed similar behavior for Canadian Cemented clay: $\sigma'_p = 90 \text{ kPa}$; $I_L = 1.4$, $S_r = 100$; CIVC Hoisting.



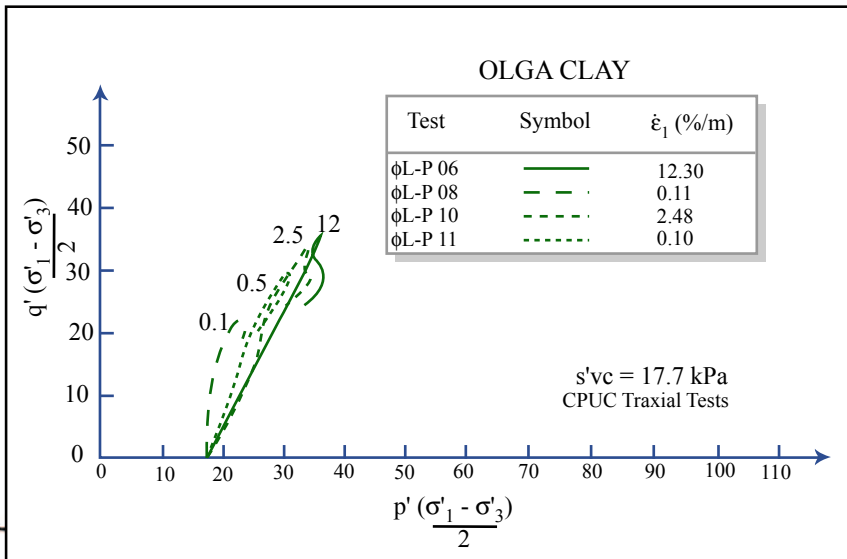
Figures by MIT OCW.



CAUC $I_p = 10\%$ $I_L = 2.5$
 B = Broadback $\sigma'_p = 175 \text{ kPa}$ $\dot{\epsilon} \text{ %/hr}$
 (SEBT NBR Project)



Figures by MIT OCW.

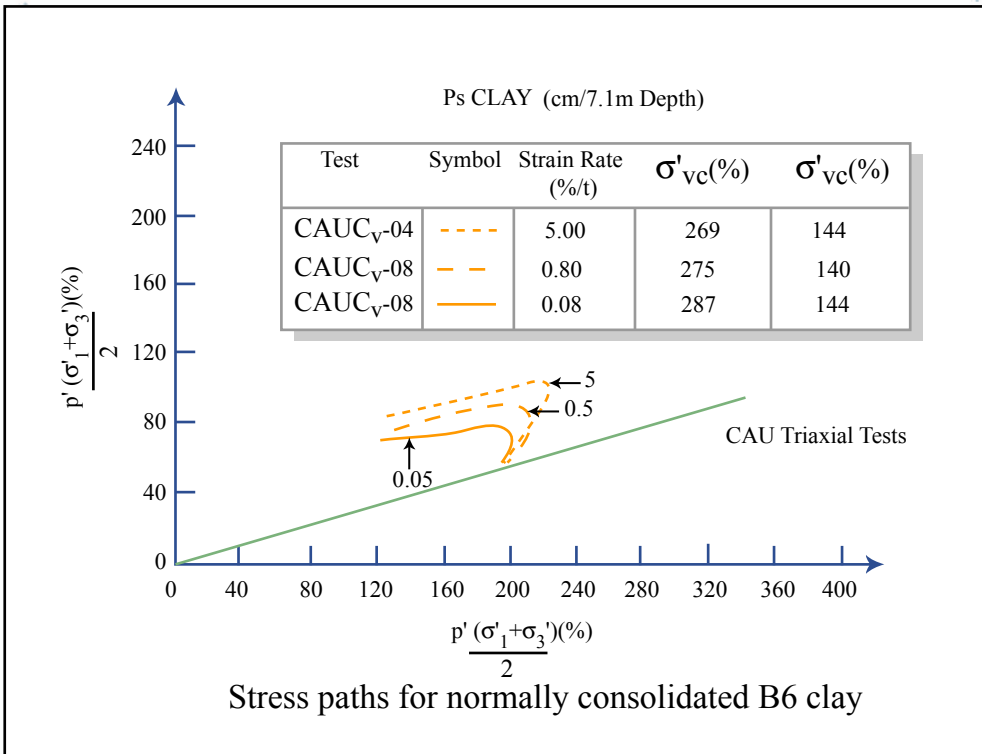
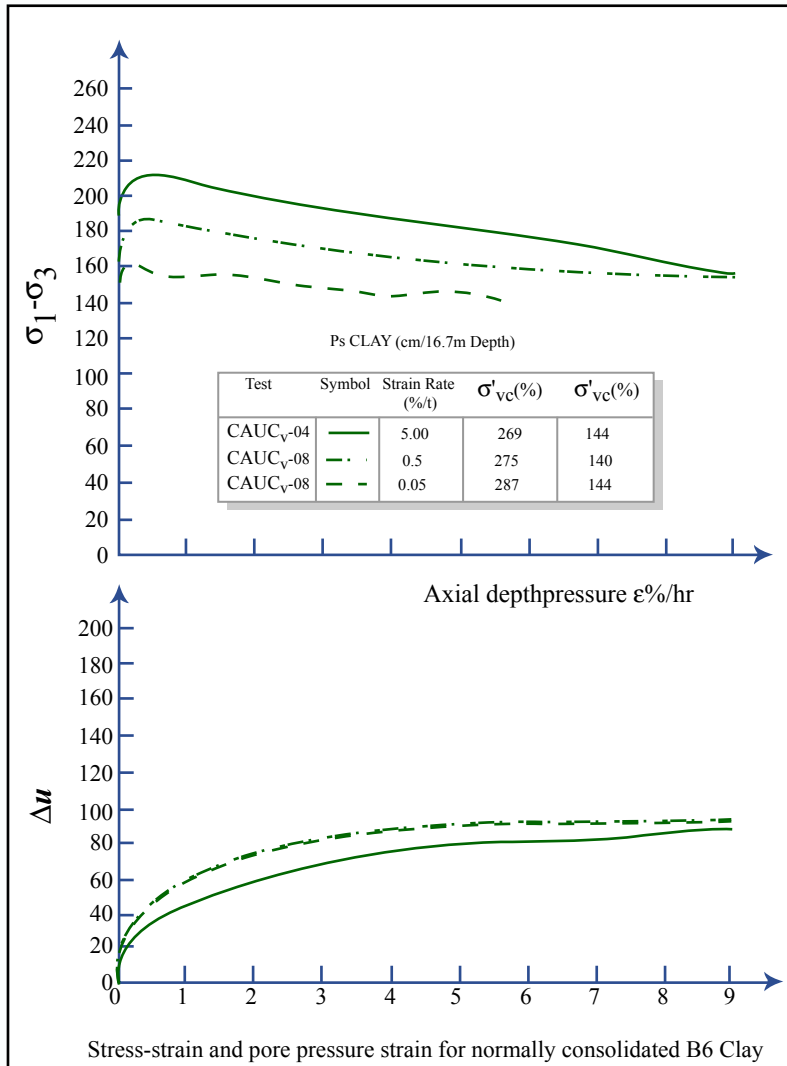


CIUC $I_p = 402$ $I_L = 1.55$
 $\sigma'_p = 78 \text{ kPa}$
 $\dot{\epsilon} \%$ /hr

- Approximately same $\Delta u \approx \epsilon$ up to ϵ_f at peak undrained q_f (especially B6 \rightarrow unique ESP independent of $\dot{\epsilon}$)
- Therefore decrease in s_u due to lowering of failure envelope, i.e., brittle cementation bonds exhibit "structural viscosity"

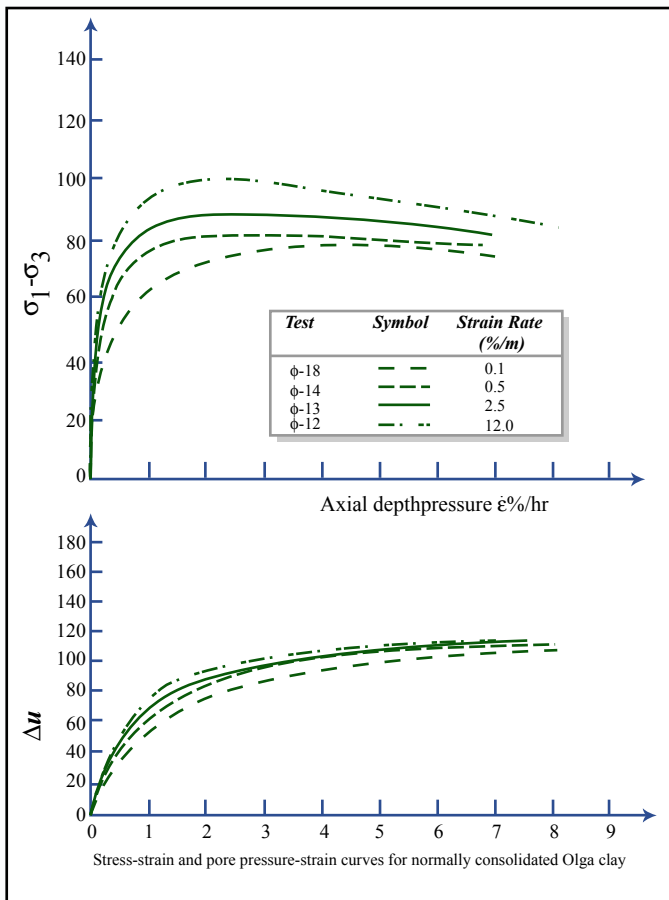
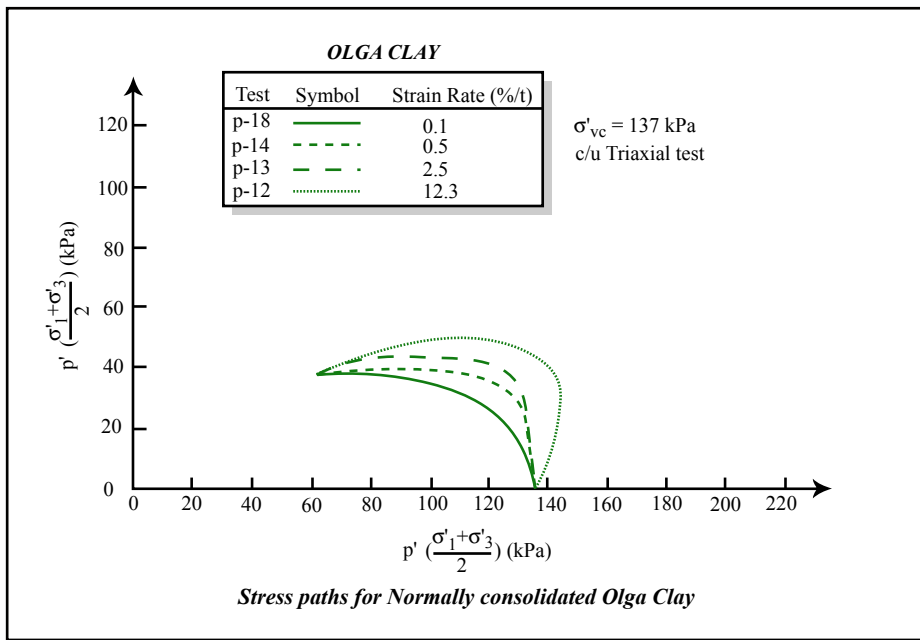
CU Test Data on "Deconstructed" Clay ($\sigma'_{vc} > \sigma'_p$)

42,381 50 SHEETS 5 SQUARE
42,382 100 SHEETS 5 SQUARE
42,383 200 SHEETS 5 SQUARE
NATIONAL ARCHIVE



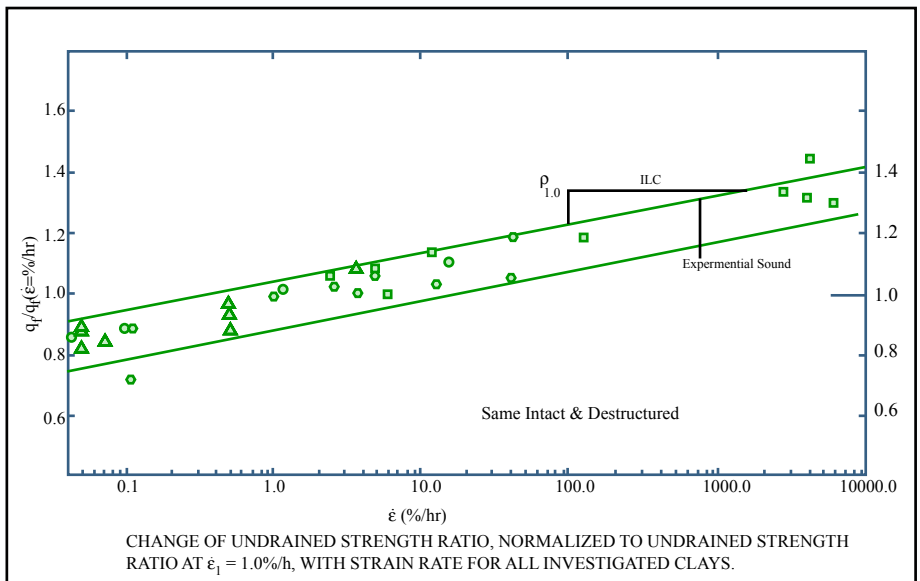
Figures by MIT OCW.

CK₀UC $I_p = 14\%$ $I_L = 1.8$
 $\sigma'_p = 145$ $\sigma'_{vc} = 270$



CIUC $\sigma'_{vc} = 1.7 \sigma'_p$

Figures by MIT OCW.



4.5 Concluding Remarks

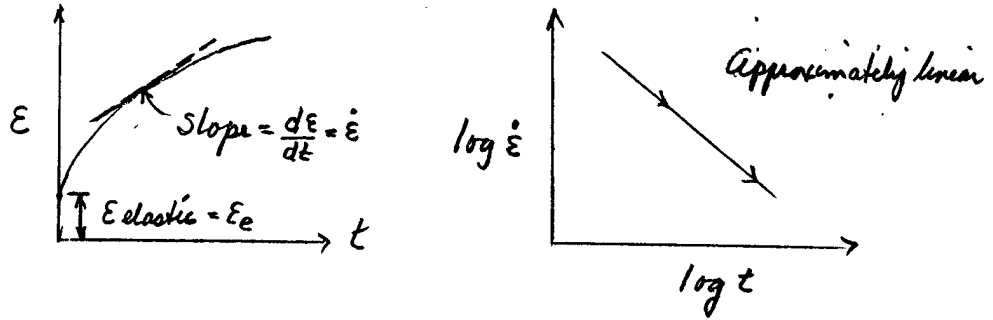
- 1) Be aware of most published data on $\dot{\epsilon}$ effects due to experimental problems
 - a) Membrane leakage \rightarrow incr. $\sigma_u \rightarrow$ decr. S_u
 - b) End restraint at high OCR \rightarrow softening in shear zone \rightarrow decreasing S_u
 - c) If very low t_c , arrested $+OU$ due to secondary compression may \rightarrow
Confusing $\Delta \sigma_u$ vs $\dot{\epsilon}$ (e.g. Holzer et al. 1973 CGJ, OVC tests on SFBM)
- 2) It is likely that all cohesive soils will exhibit strain rate sensitivity at very fast strain rates (say $\dot{\epsilon} > 5-10\%/hr$) that will affect interpretation of in situ tests and lab OVC, TV, etc. tests. Can get very high P_c 10-30%.
- 3) For non-structured clays similar to Resedimented BBC, Sheahan et al. (1996) present the only good CK₀UC vs $\dot{\epsilon}$ data as $f(OCR)$. Principal conclusions are: (for $\dot{\epsilon} \leq 5\%$)
 - a) at low OCR ≈ 1 :
 - $P_{0.5}$ due to both lower σ_{us} and increased ϕ'_p
 - Should expect strain rate effects in field
 - b) at moderate to high OCR:
 - $P_{0.5}$ due mainly or only to lower σ_{us}
 - Strain rate effects in field may be very small since $\phi \rightarrow 0$ w/ incr. OCR at low $\dot{\epsilon}$
- 4) For Canadian cemented clays, expect significant strain rate effects in both lab and field over entire $\dot{\epsilon}$ range (for both consolidation and drained/undrained shear)

4/96

5. UNDRAINED CREEP

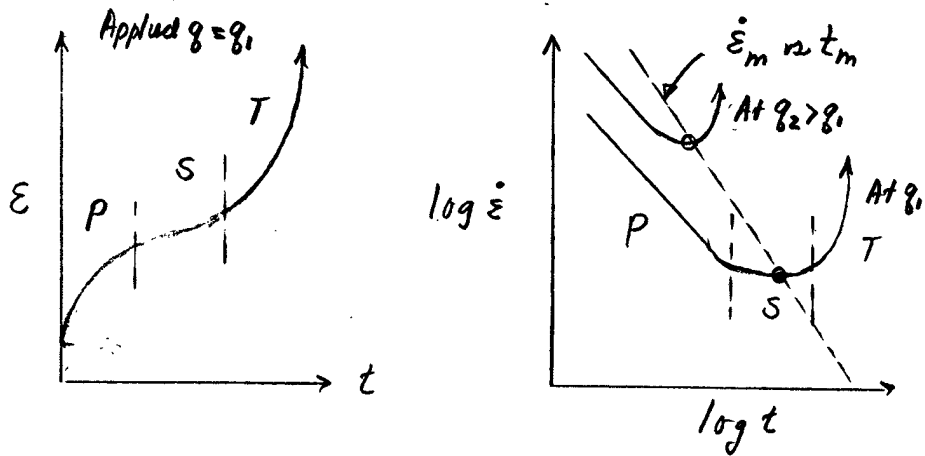
5.1 Introduction (Constant q testing)

1) "Low" stress level (Only "primary")



• Will model w/ Singh-Mitchell 3 parameter eqn.

2) "High" stress level \rightarrow Creep Rupture



Transient \equiv Primary = $\dot{\epsilon}$ decreasing

Viscous \equiv Steady State \equiv Secondary = $\dot{\epsilon}$ "constant" $\rightarrow \dot{\epsilon}_m$ (inflection point if creep rupture)

Tertiary = $\dot{\epsilon}$ increasing \rightarrow creep rupture

3) Questions

- Physical explanation of behavior (if possible)
- Mathematical models of behavior, at least for primary
- How to estimate q that will not \rightarrow creep rupture (depending long term q_t)
- "Correspondence" between creep & constant $\dot{\epsilon}$ test data

5.2 Singh-Mitchell 3 Parameter Egn. (1968, 1976, 1993 book) ¹⁹⁷⁶
 2 JSNFD 94(1)

1) Egn.

$$\dot{\epsilon} = A e^{\bar{\alpha} \bar{D}} (t_1/t)^m$$

- "Derived" from Rate Process Theory
- Restricted to Primary creep

$t_1 = \text{reference } t$

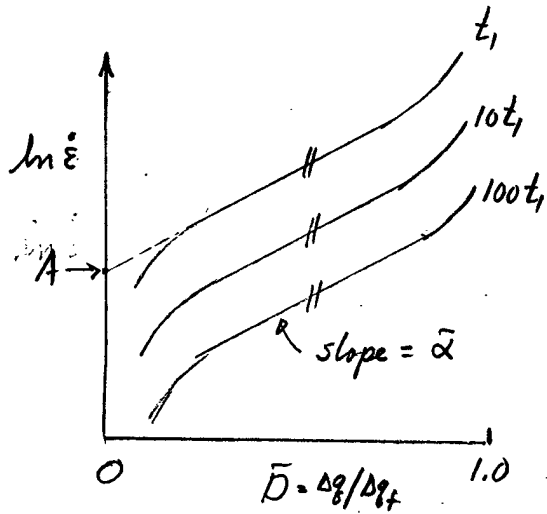
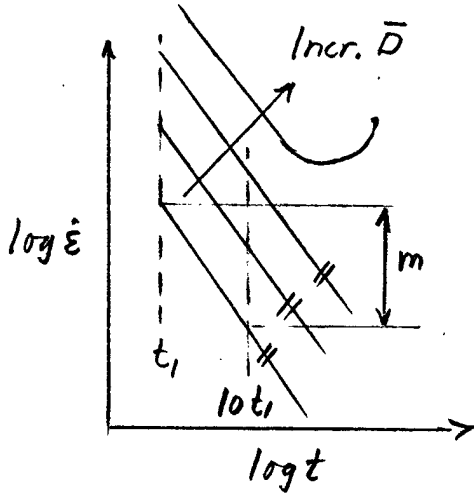
$$\bar{D} = \Delta \sigma / \Delta \sigma_t \quad (\Delta \sigma_t \text{ at reference } \dot{\epsilon})$$

$$m = -d \log \dot{\epsilon} / d \log t$$

$$\bar{\alpha} = d \ln \dot{\epsilon} / d \bar{D} = 2.3 d \log \dot{\epsilon} / d \bar{D}$$

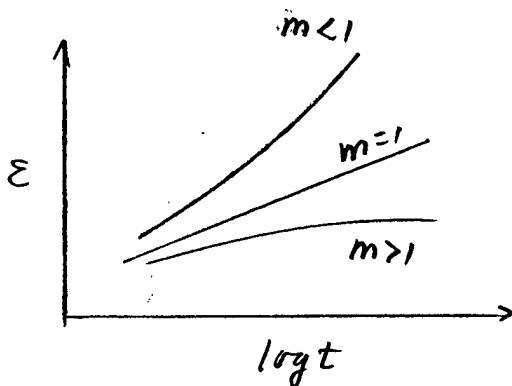
$$A = \dot{\epsilon} \text{ at } t=t_1, \bar{D}=0$$

2) Basic plots



$\bar{\alpha}$ presumed constant
 for $\bar{D} \approx 0.3 - 0.9$

3) Significance of m (Presumed basic soil property, by S-M;
 lower $m \rightarrow$ more creep susceptible)



$m=1 \rightarrow \dot{\epsilon} t = \text{constant}$
 (like constant C_ϵ)

$m < 1$ more "creep susceptible" à la S-M
 w/ $\dot{\epsilon} t$ increasing with t

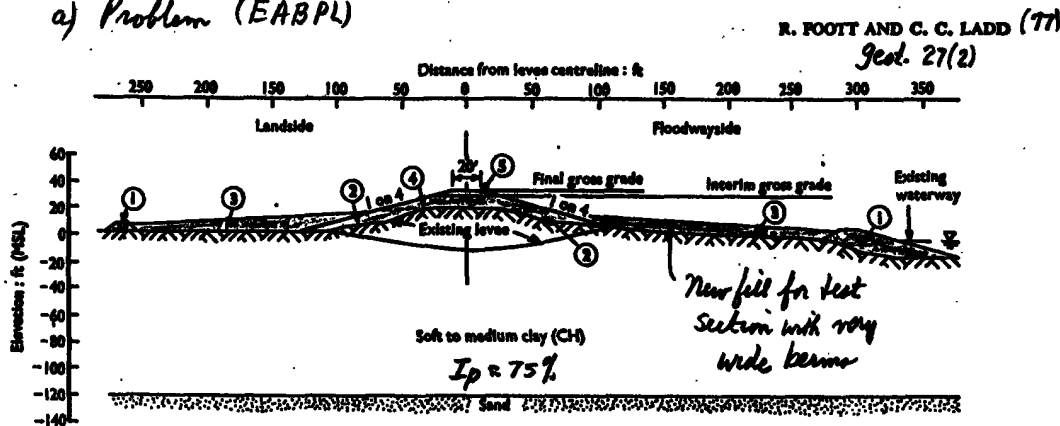
$$\epsilon = \epsilon_1 - \frac{A e^{\bar{\alpha} \bar{D}} t_1}{(1-m)} + \frac{\dot{\epsilon} t}{(1-m)} \quad \left. \vphantom{\frac{A e^{\bar{\alpha} \bar{D}} t_1}{(1-m)}} \right\} m \neq 1$$

Slope = $d\epsilon/dt = \dot{\epsilon} = \frac{0.434 (d\epsilon/d \log t)}{t}$

* Is negative for $m > 1 \rightarrow$ subtraction of
 less neg. no. of $m \cdot t \rightarrow m \cdot \dot{\epsilon}$ w/ time

4) Results from MIT research on flood control levees along Atchafalaya River in Louisiana next to Gulf of Mexico (Edgar et al. 1973; MIT report)

a) Problem (EABPL)



- "Existing" levees: Construction 1930 to 1970 to maintain wet grade of 15 ft
Caused accumulated ϵ of up to 35 ft!
- Very expensive test sections (above) did not perform much better, i.e. excessive lateral deformations (undrained creep) \rightarrow excessive ϵ & settlement

b) Results from creep testing on EABPL clay

	Test	\bar{D}	m	$\bar{\epsilon}$
SP.OC	CUUC	0.75-0.9	0.95	4.7
NC	CK ₀ UC	0.5-0.9	0.55 \pm 0.1	4 \pm 0.2
	CK ₀ UDSS	0.5-0.85	0.85-0.9	4 \pm 0.4

} $m = 0.55$ to 0.95
for this highly creep susceptible clay

5) Campanella & Vaid (1974 CGJ) tests on low I_p NC Honey Clay

- CUUC $\rightarrow m = 0.6$ • CK₀UC $\rightarrow m = 0.35$ • CK₀UPSC $\rightarrow m = 0.5$
- $\therefore m = 0.35 - 0.6$ for clay that is not very creep susceptible

6) Conclusions

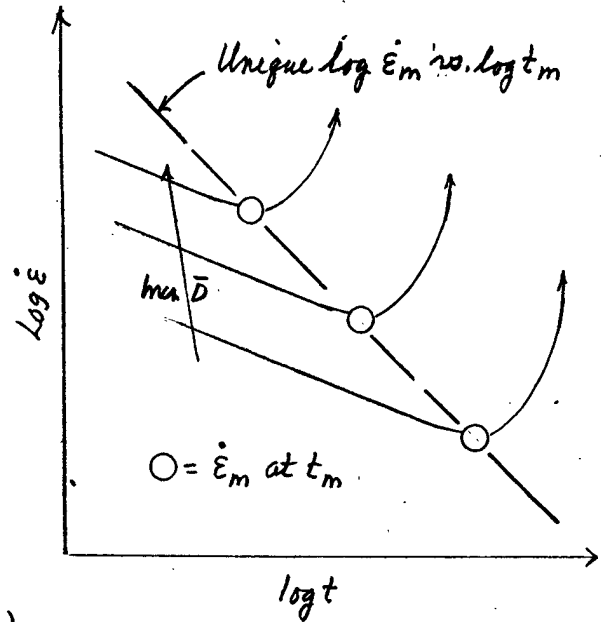
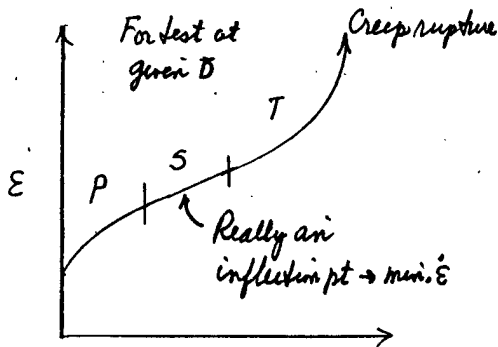
- However, eqn. still useful for modeling given set of primary creep data
- m & $\bar{\epsilon}$ are not material properties since they vary with mode of shearing
- Value of m is not valid criterion for creep susceptibility, i.e. lower m does not mean more highly creep susceptible (see Section 5.6 for new criteria)
- Techniques do NOT exist to predict undrained creep in the field [even though S-Meqn. has been added to "MCC" to do this, e.g. Borja et al. 1990, JGR, 116(9)]

22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS



5.3. Creep Rupture

1) General Behavior: Results from creep tests run at varying $\bar{D} = D_0/\sigma_0$



\therefore Creep tests (of given type) run at varying \bar{D} yield unique relationship between minimum strain rate ($\dot{\epsilon}_m$) and the time (t_m) to reach $\dot{\epsilon}_m$

2) Strain at Minimum Strain Rate (ϵ_m)

- Experimental data show approximately constant strain (ϵ_m) along the $\log \dot{\epsilon}_m$ vs. $\log t_m$ relationship
- $\dot{\epsilon}$ is decreasing before reaching $\dot{\epsilon}_m$, and then accelerates after reaching $\dot{\epsilon}_m$. This suggests that "damage" starts to occur near $\dot{\epsilon}_m$, leading to a weakened material that eventually fails in creep rupture.

3) Creep Rupture Data on Haney Clay (Sheet C1)

- Fig 2 shows $\log \dot{\epsilon}$ vs. $\log t$ data from CIUC, CKoUC and CKoUPSC tests on NC clay \rightarrow 3 different $\log \dot{\epsilon}_m$ vs. $\log t_m$ relationships
- Fig. 3 shows constant ϵ_m for each test series. However, ϵ_m decreases from $\epsilon_m = 2.8\%$ for CIUC tests to $\epsilon_m = 0.3\%$ for CKoUC tests.

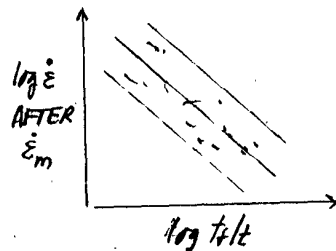
4/99 4/01

5.3 Continued4) Log $\dot{\epsilon}_m$ vs log t_m and ϵ_m Data for Other Materials (Sheet C2)

- Figs. 1 and 3 show log $\dot{\epsilon}$ vs log t data from unconfined compression tests on frozen Manchester Fine Sand (ice saturation $S_i = 40\%$) and polycrystalline ice, respectively, and their unique log $\dot{\epsilon}_m$ vs log t_m relationships.
- Fig. 4 summarizes the unique log $\dot{\epsilon}_m$ vs log t_m relationships for frozen MFS ($S_i = 20\%, 40\% \& 100\%$), ice and CIUC/CK,UC tests on Honey clay.
- Note the shift to the right in log $\dot{\epsilon}_m$ vs. log t_m with increasing ϵ_m (i.e., increasing $\epsilon_m \rightarrow$ longer time to reach critical strain at which "damage" \rightarrow increasing $\dot{\epsilon}$)
- Log $\dot{\epsilon}_m$ vs log t_m can be modeled by $\dot{\epsilon}_m = \beta t_m^\gamma$; data in Fig. 4 show $\gamma = -1.0 \pm 0.2$

5) Summary of Main Points

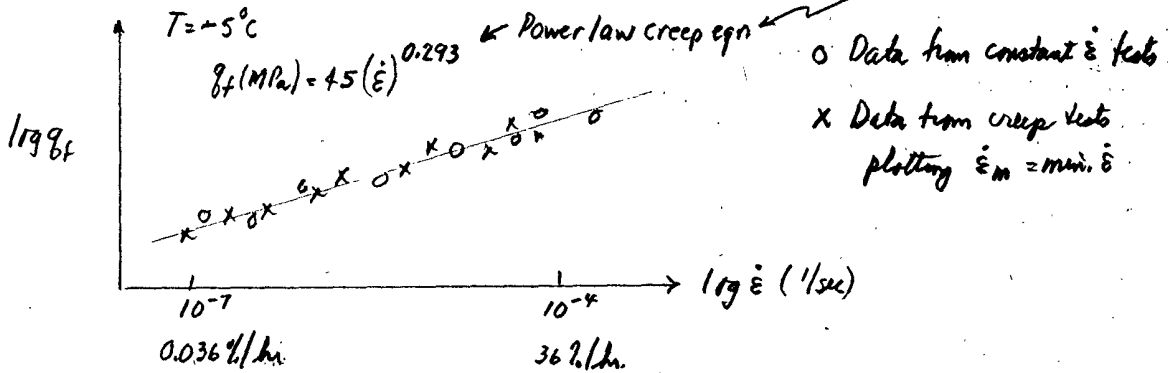
- Should plot log $\dot{\epsilon}$ vs log t from creep tests in order to identify the minimum strain rate ($\dot{\epsilon}_m$) at $t = t_m$
 - Creep data from different types of tests (e.g., UC \rightarrow CIUC \rightarrow CK,UC) and different materials (clay \rightarrow ice) each show unique log $\dot{\epsilon}_m$ vs log t_m (with slope $\gamma = -1.0 \pm 0.2$) relationships having a constant ϵ_m
 - This ϵ_m represents onset of "damage" that \rightarrow increasing $\dot{\epsilon}$ and eventual creep rupture
- 6) Prediction of Creep Rupture
- The literature contains equations & plots to predict when creep rupture will occur.
 - However, the scatter in data for different soils and different types of tests is so large that eqn/plots have little practical significance.



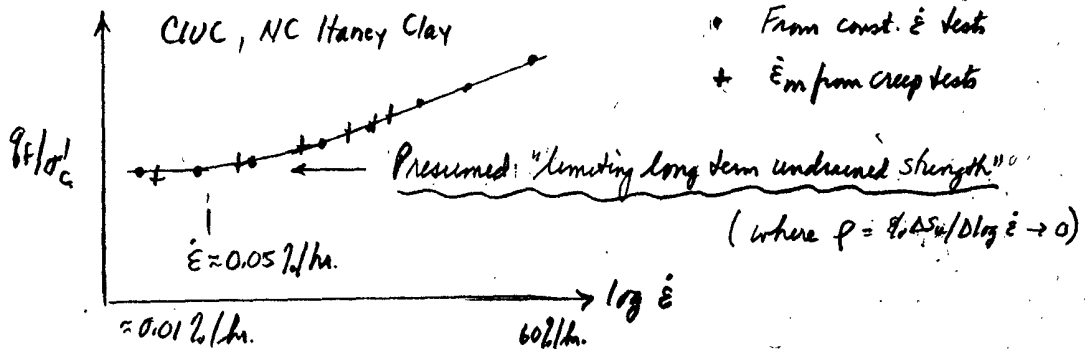
5.4 "Correspondence"

1) This topic addresses the issue between results from constant $\dot{\epsilon}$ tests and from creep tests that eventually rupture.

2) Extensive data on polyisobutylene ice* (within so-called ductile region with minimal cracking) show a unique relationship between strength and strain rate using $\dot{\epsilon}_m$ for the creep tests, $q = C(\dot{\epsilon})^{1/N=3.41}$



3) There are little data on clays comparing constant $\dot{\epsilon}$ and creep testing. However, results for Honey clay (see sheet D) also show correspondence when use $\dot{\epsilon}_m$ for creep tests



4) Conclusion:

Use $\dot{\epsilon}_m$ from creep tests for comparison with $\log \dot{\epsilon}$ from constant $\dot{\epsilon}$ tests

* Mellor & Cole (1983) Cold Regions Science & Technology, p 207-230

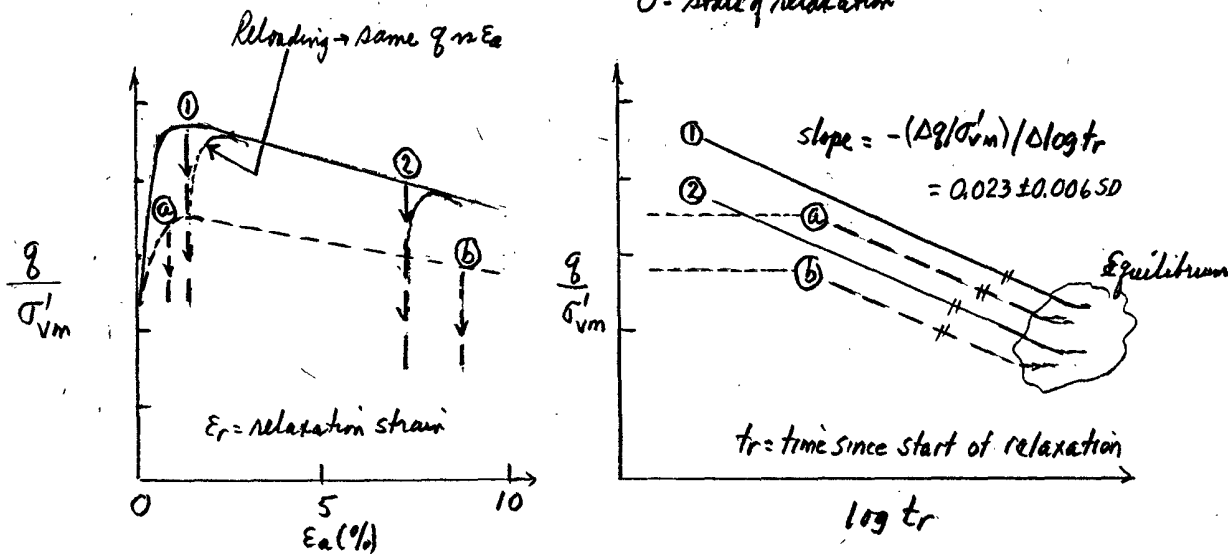
22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS



5.5 Relaxation

- 1) Refers to decrease in q (relaxation) at constant strain after shearing at constant $\dot{\epsilon}$ up to the relaxation strain level (ϵ_r)
- 2) Overview of CKoUC data from Sheahan et al. [1994, ASTM, GTS 17(4)] on reseedimented BBC (part of test program discussed in Section 4.3)

0 = start of relaxation



- For fast shearing to ϵ_r : relaxation starts quickly
 - For slow " " " : start of relaxation is delayed
- } Approx same slope independent of $\dot{\epsilon}$, ϵ_r and OCR
- For relaxation from relatively small strain levels ($\epsilon_a \leq 1.5\%$), equilibrium stresses ended up close to NC K_0 line. Relaxation from larger strain level ($\epsilon_a \geq 2.5\%$ \rightarrow Δ structure of clay) \rightarrow equilibrium at higher K .

3) See sheets E1 & E2 for actual test data (mostly for OCR=1)

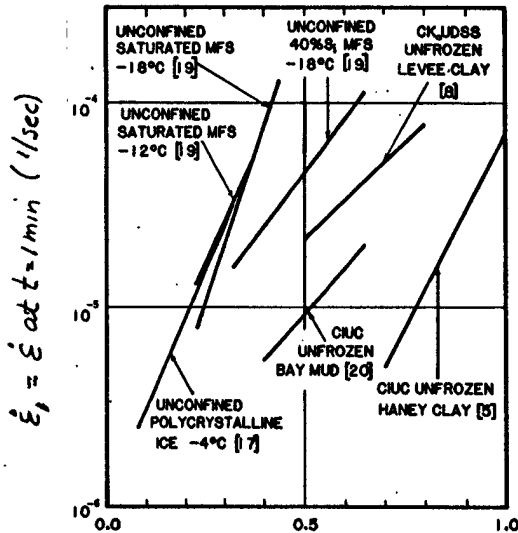
- Fig 1 = $q/\sigma'_{vc} \approx \epsilon_a$
- Fig 2 = ESP data
- Fig 3 = q/σ'_{vc} vs $\log tr$
- Fig 5 = Equilibrium stresses

22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS



5.6 Criteria For High Creep Susceptibility

Fig. 3 Ting et al. (1983) JGE 109(10)



$$\bar{D} = \Delta q / \Delta q_f \quad (q_f \text{ at reference } \dot{\epsilon})$$

3) Therefore, materials with high creep susceptibility have a high initial strain rates at low shear stress levels.

4) However, value of m is still relevant since:

- high $m \rightarrow$ rapid decay in $\dot{\epsilon}$ with time
- low $m \rightarrow$ slow " " " " "

1) m value is not reliable criterion

2) Fig. 3 plots $\dot{\epsilon}$ at $t = 1 \text{ min}$ vs. \bar{D} from creep tests on variety of materials.

- Honey clay of low creep susceptibility plots to lower, right (low $\dot{\epsilon}_1$ at high \bar{D})
- Ice & frozen sand of high creep susceptibility plot to upper left (high $\dot{\epsilon}_1$ at low \bar{D})

22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS



6. SUMMARY AND CONCLUSIONS

6.1 Measurements of S_u

- 1) Strain rate sensitivity of saturated cohesive soils ($\rho = (\Delta S_u / S_{u0}) / \Delta \log \dot{\epsilon}$)
 - All soils have significant ρ at very fast strain rates (say $\dot{\epsilon} > 5-10\%/hr$). ρ may range from $\approx 10\%$ to $> 35\%$ / log cycle.
 - Cemented, sensitive Canadian clays ^{probably} have significant ρ at all strain rates.
 - For "unstructured" clays (like RBBC), value of ρ at slow to moderate $\dot{\epsilon}$ probably decreases with increasing OCR (Section 4.3)
- 2) Must consider $\Delta \dot{\epsilon}$ (or Δt_f) when comparing S_u data from different types of shear tests:
 - For in situ tests, CPTU $t_f \approx$ seconds & FVT $t_f \approx$ minutes
 - Lab UUC, Std $\dot{\epsilon} = 1\%/min \rightarrow t_f \approx$ minutes
 - Lab CK₀UTX, $\dot{\epsilon} = 0.5\%/hr \rightarrow t_f \approx$ hours
- 3) For SHANSEP/Recompression CK₀U testing programs, many major labs use:
 - TX $\dot{\epsilon} \approx 0.5\%/hr$ • DSS $\dot{\epsilon} = 5\%/hr$
 - Should be ok for most clays at OCR > 1
 - May be somewhat unsafe for low OCR clay

6.2 Predictions of Undrained Creep

- 1) The Singh-Mitchell 3 parameter eqn. (Section 5.2) is widely used to model primary creep data from lab tests. However, its use to predict in situ creep is suspect (due to variations in parameters with different modes of shearing), plus problems with its incorporation in an effective stress soil model)
- 2) One probably can assume correspondence between constant $\dot{\epsilon}$ tests and creep rupture tests (using $\dot{\epsilon}_{min}$) when developing S_u vs $\log \dot{\epsilon}$ correlations

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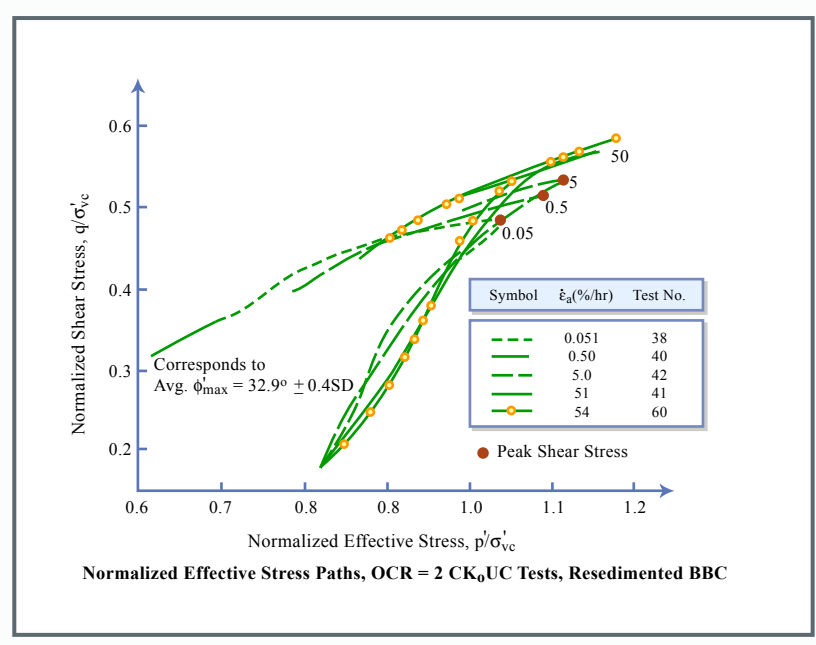
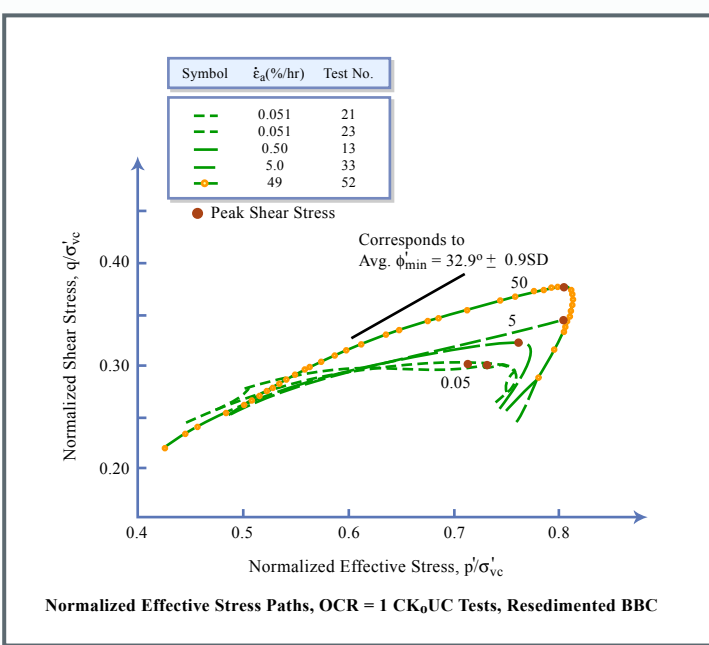
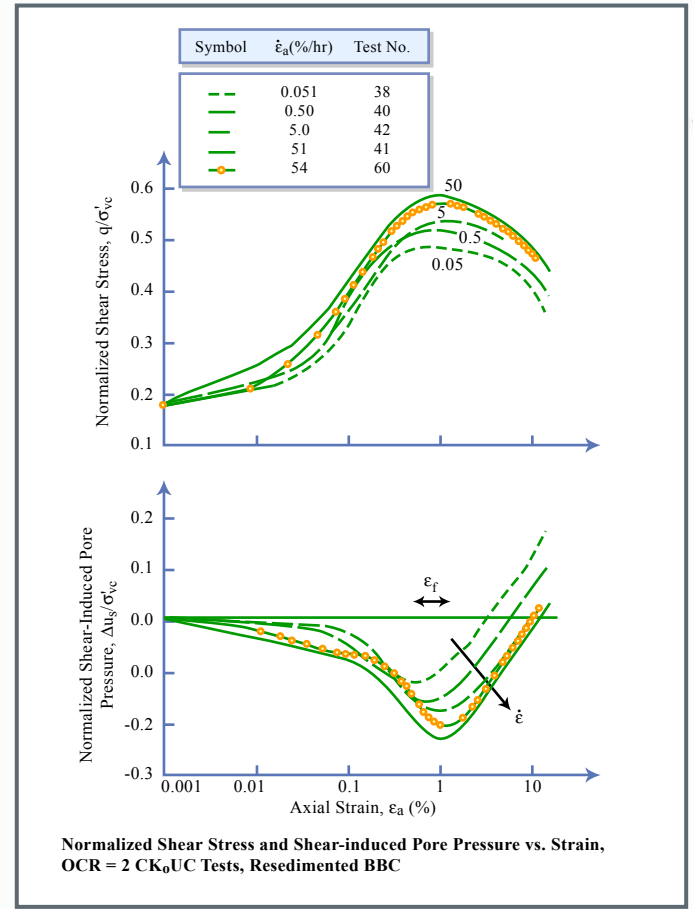
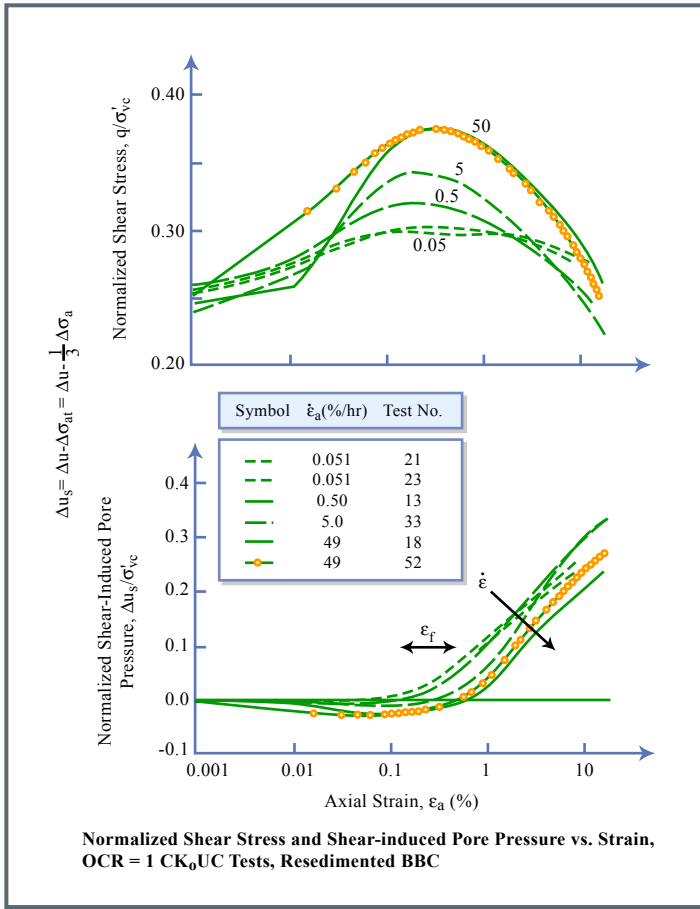


6.2 Cont.

- 3) It is still difficult to predict when undrained creep is likely to cause "excessive" deformations in the field.
- Refer to Forth & Ladd (1981) → loading at low P_f/S of low E_u soil with long consolidation time
 - Might also run some CU creep tests for comparison with data in Fig 3, p 21
- 4) Will a loaded clay undergo undrained creep rupture in the field at a significant time after the end of loading?
- CCL thinks highly unlikely, but many others will disagree

6.3 Miscellaneous

- 1) The importance of thixotropy in situ remains unclear
- 2) For NC clays that are still consolidating, use $t_c = t_p$ (vs. std. $t_c = 1 \text{ day}$) for CKoU testing

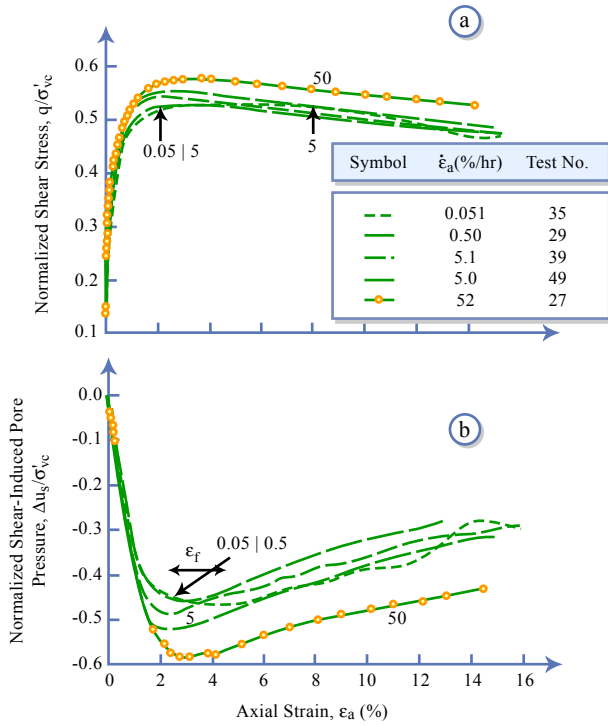


Figures by MIT OCW.

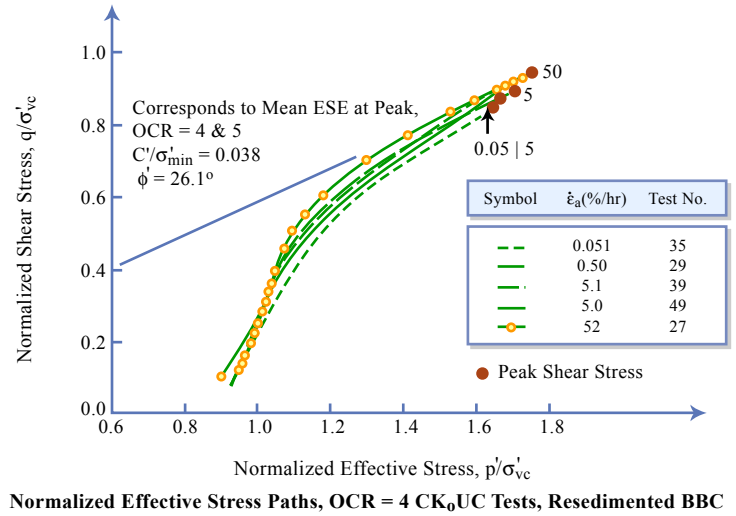
CK₀UC Tests on Resedimented BBC as f(ε̇) : OCR=1 & 2

Adapted from: Sheahan et al. (1996)

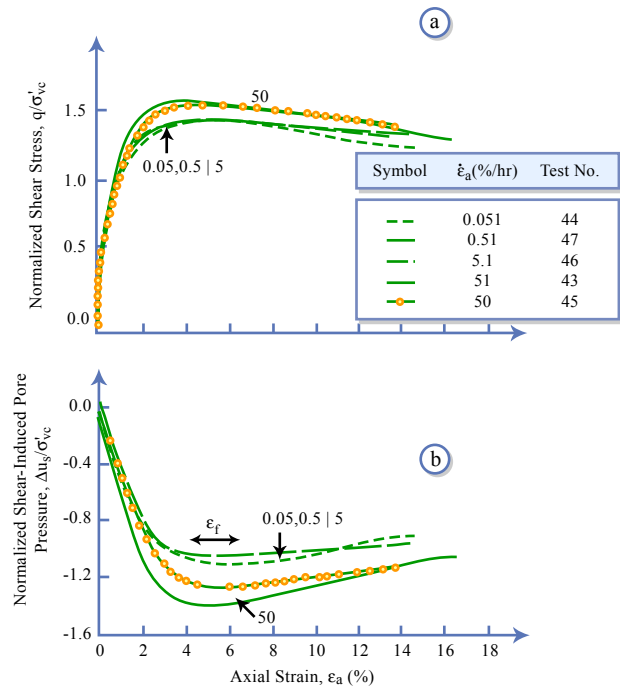




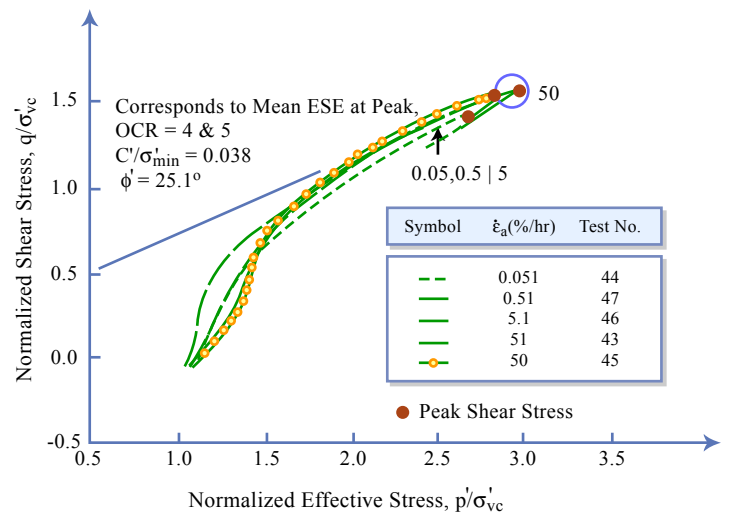
Normalized Shear Stress and Shear-induced Pore Pressure vs. Strain, OCR = 4 CK₀UC Tests, Resedimented BBC



Normalized Effective Stress Paths, OCR = 4 CK₀UC Tests, Resedimented BBC



Normalized Shear Stress and Shear-induced Pore Pressure vs. Strain, OCR = 8 CK₀UC Tests, Resedimented BBC

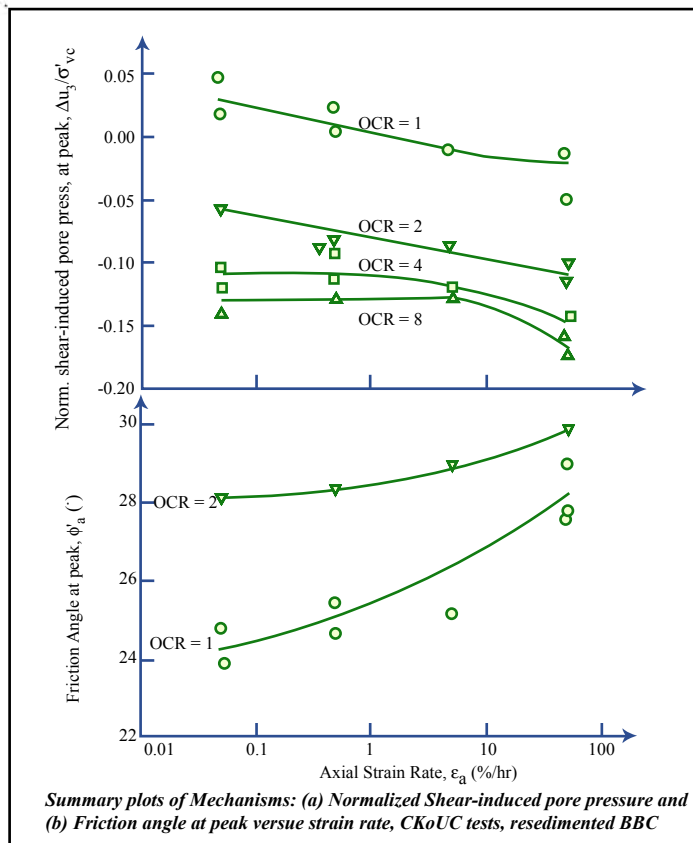
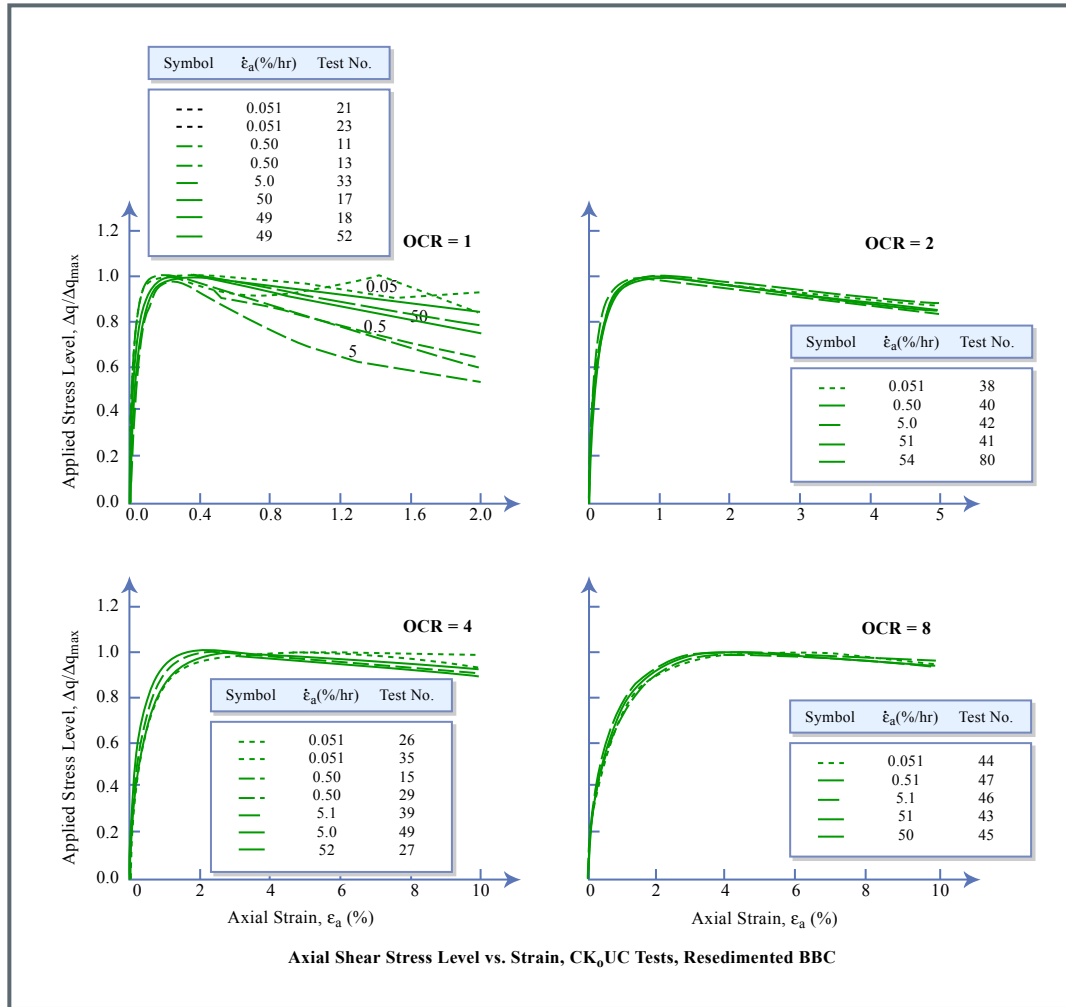


Normalized Effective Stress Paths, OCR = 8 CK₀UC Tests, Resedimented BBC

Figures by MIT OCW.

CK₀UC Tests on Resedimented BBC as f($\dot{\epsilon}$): OCR = 4 to 8

Adapted from: Sheahan et al. (1998)



↑
 Unique NORMALIZED Shear
 Stress ($\Delta u_3 / \Delta q_{max}$) vs ϵ_a
 (especially OCR = 2, 4 & 8)

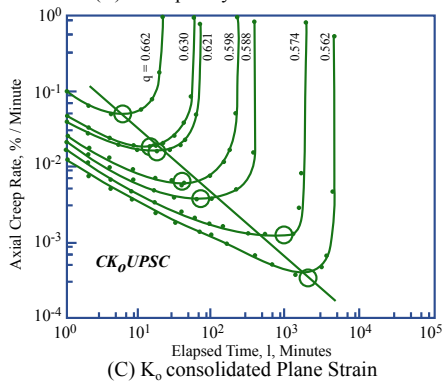
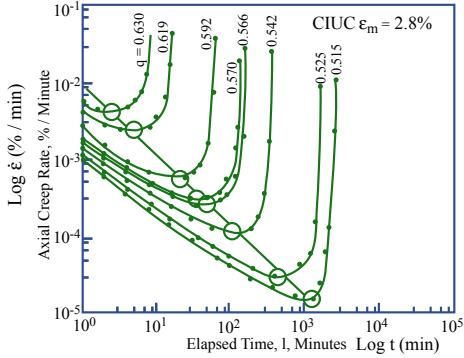
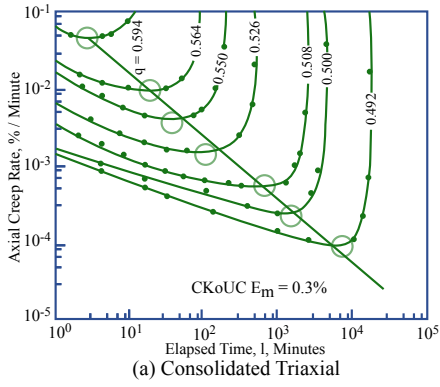
Increasing s_u always
 accompanied by decreasing Δu_3

Increasing s_u at low OCR also
 accompanied by increasing ϕ'_p

Figures by MIT OCW.

Adapted from: Sheahan et al. (1996)

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Creep rate behavior of normally consolidated undisturbed Haney clay.

Figure by MIT OCW.

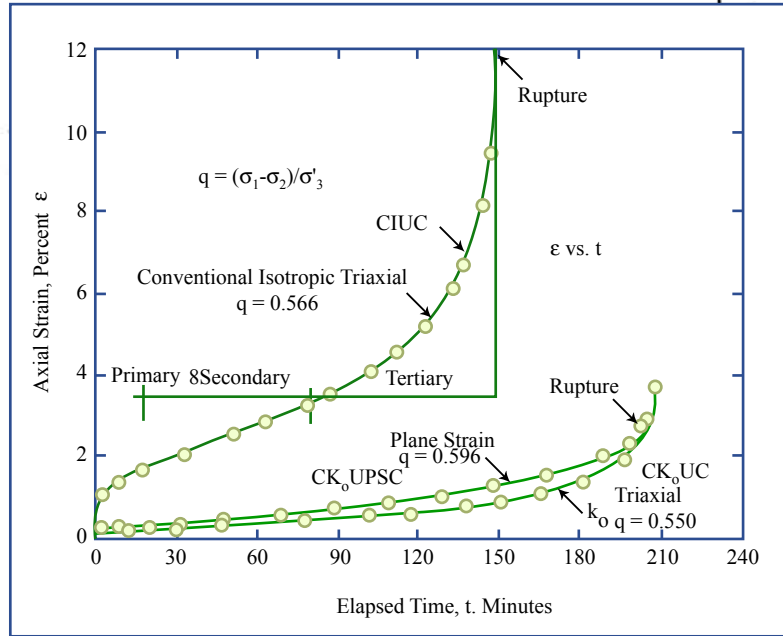


Figure by MIT OCW.

Campanella & Vaid (1974) CGJ, 11(1)

N.C. Haney Clay $w_L = 44, I_p = 18$

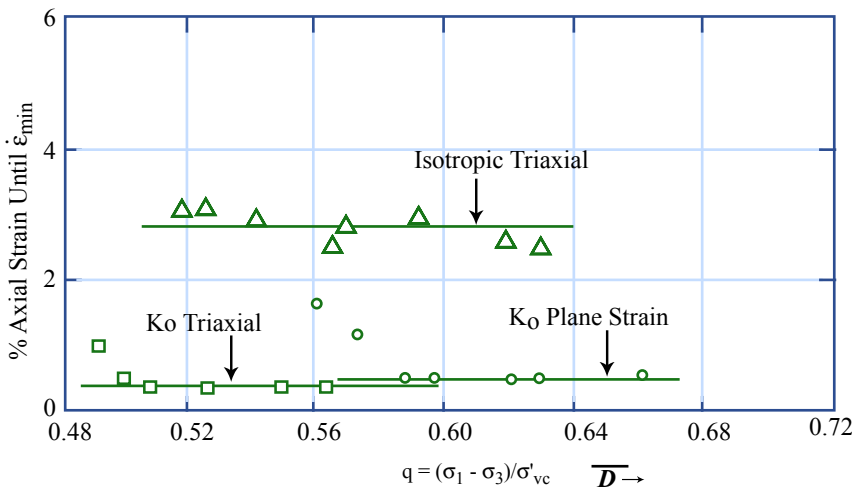
Lab $\sigma'_{vc} / \sigma'_p = 1.5$

• Fig. 2 is $\log \dot{\epsilon} \approx \log t$ at varying \bar{D}

○ = location of $\min \dot{\epsilon} = \dot{\epsilon}_m$
at $t = t_m$

(line through $\dot{\epsilon}_m - t_m$ by CCL)

• Fig. 3 Axial strain at $\dot{\epsilon}_m = \dot{\epsilon}_m$



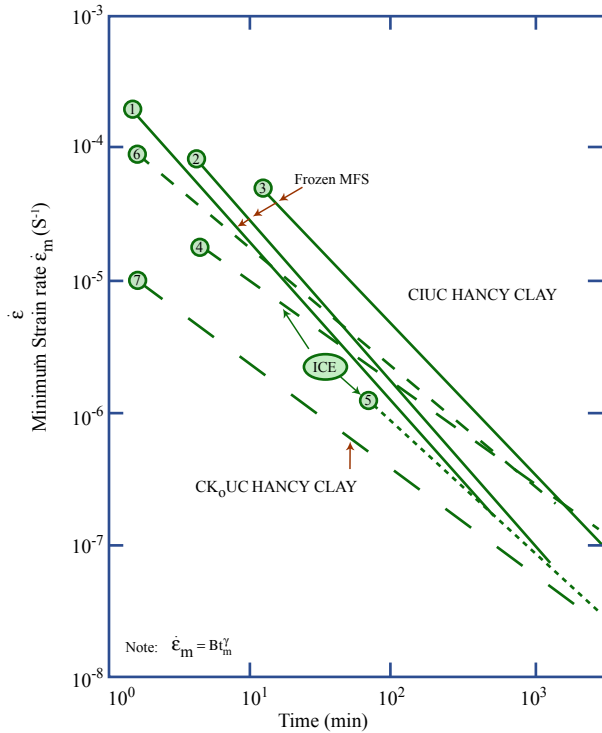
Axial strain until minimum strain rate as a function of creep stress.

Figure by MIT OCW.

Test	ϵ_m (%)
CIUC	2.8
CKoUPSC	0.5
CKoUC	0.3

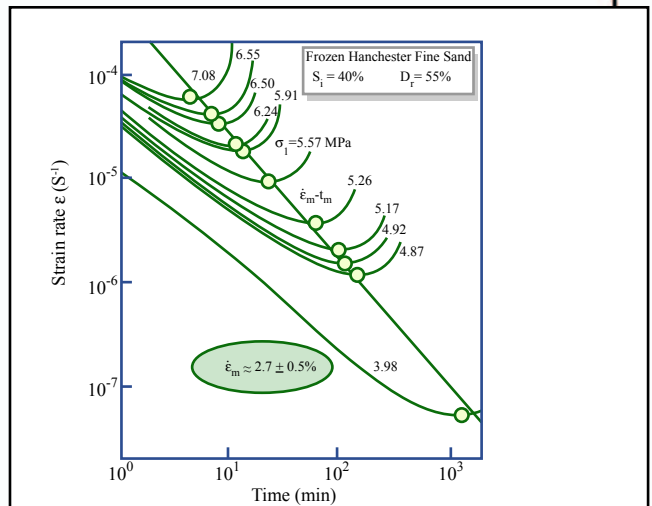
CI

22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS

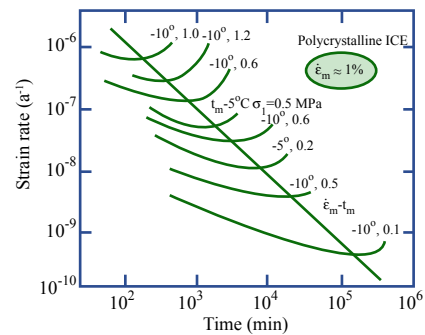


No.	Material	Testing	Reference	B^0	γ^0	r^2	No. Tests	ϵ_m (%)
1	20% S_i MFS	Uniaxial	Martin (1981)	2.8×10^{-4}	-1.2	0.987	7	2.1
2	40% S_i MFS	Uniaxial		4.2×10^{-4}	-1.2	0.993	40	2.7
3	100% S_i MFS	Uniaxial		8.1×10^{-4}	-1.2	0.991	28	4.6
4	Ice	Uniaxial	k_{uo} (1972)	7.9×10^{-5}	-0.8	0.987	7] ≈ 1
5	Ice	Uniaxial	Jacka, in Lue (1979)	6.5×10^{-5}	-1.0	0.996	8	
6	Unfrozen Hanczy Clay	CIUC	Campanella & Void (1974)	1.3×10^{-4}	-0.9	0.997	8	2.8
7	Hanczy Clay	CK ₀ UC		1.5×10^{-5}	-0.8	0.987	7	0.3

Summary of minimum creep rate: Correlations of time to minimum for various materials



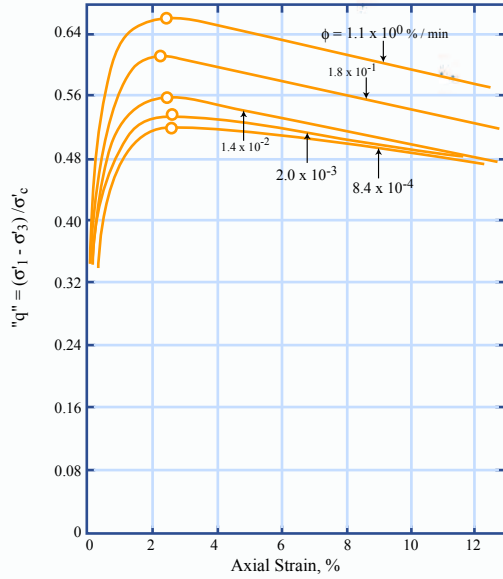
Results of unconfined (uniaxial) compressive creep testing of 40% saturated, 55% relative density Manchester fine sand at $-18.8^\circ C$ (data from Martin et al. 1981)



Results of unconfined (uniaxial) compressive creep testing of polycrystalline ice. (data by Jacka, see Lile 1979).

Figures by MIT OCW.

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Influence of rate strain on undrained stress-strain behavior in constant rate of strain shear.

Figures by MIT OCW.

Adapted from:

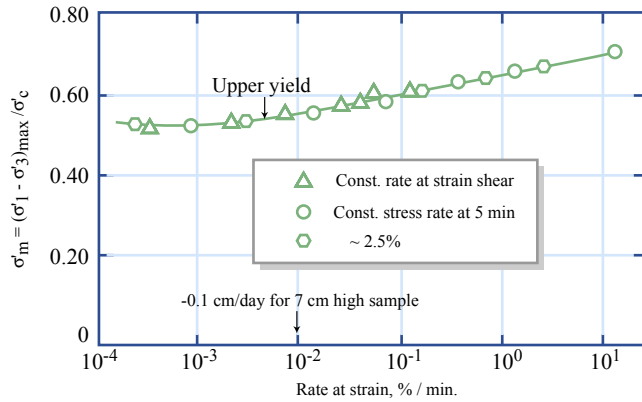
Vaid & Campanella (1977) JGED 103(7)

CIUC OCR=1 Honey Clay

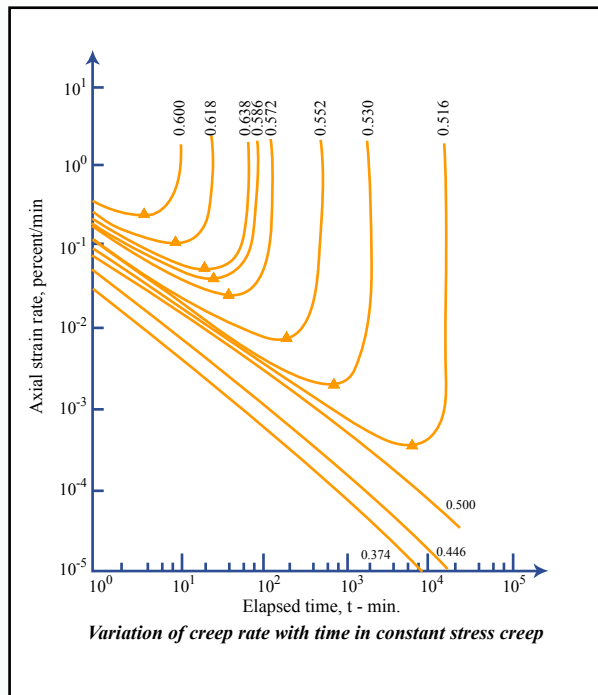
Fig. 2 Constant $\dot{\epsilon}$: take peak •

"5" Constant stress, use $\dot{\epsilon}_m$ +

↓ Fig 3 "Correspondence"



Strain rate dependence of undrained strength in constant rate of strain Shear and constant stress creep



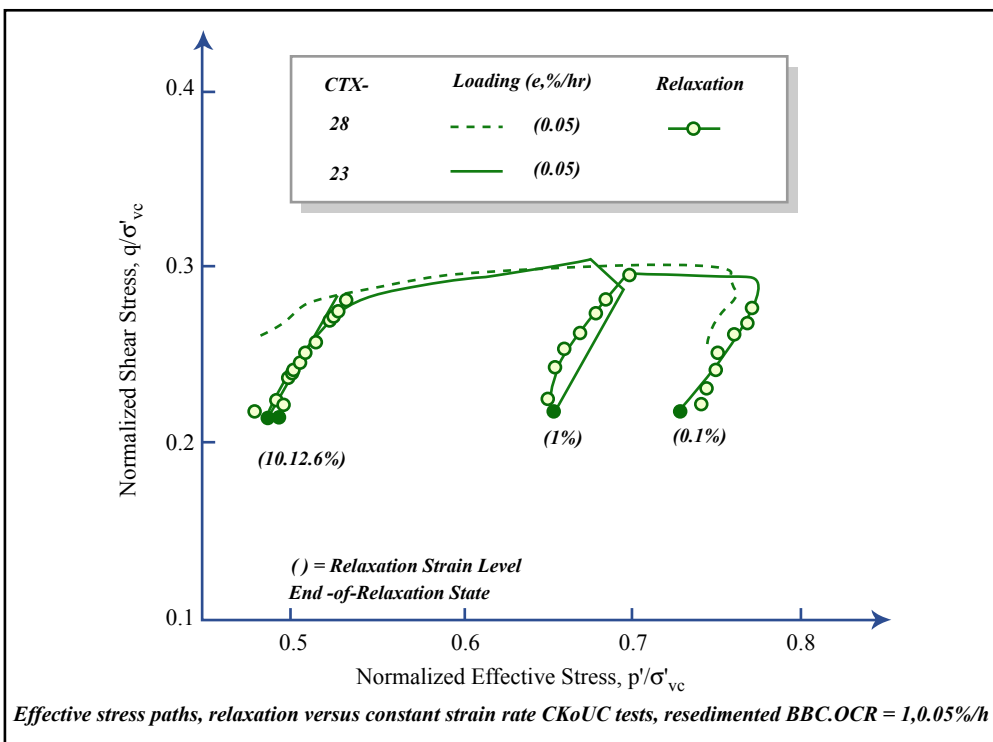
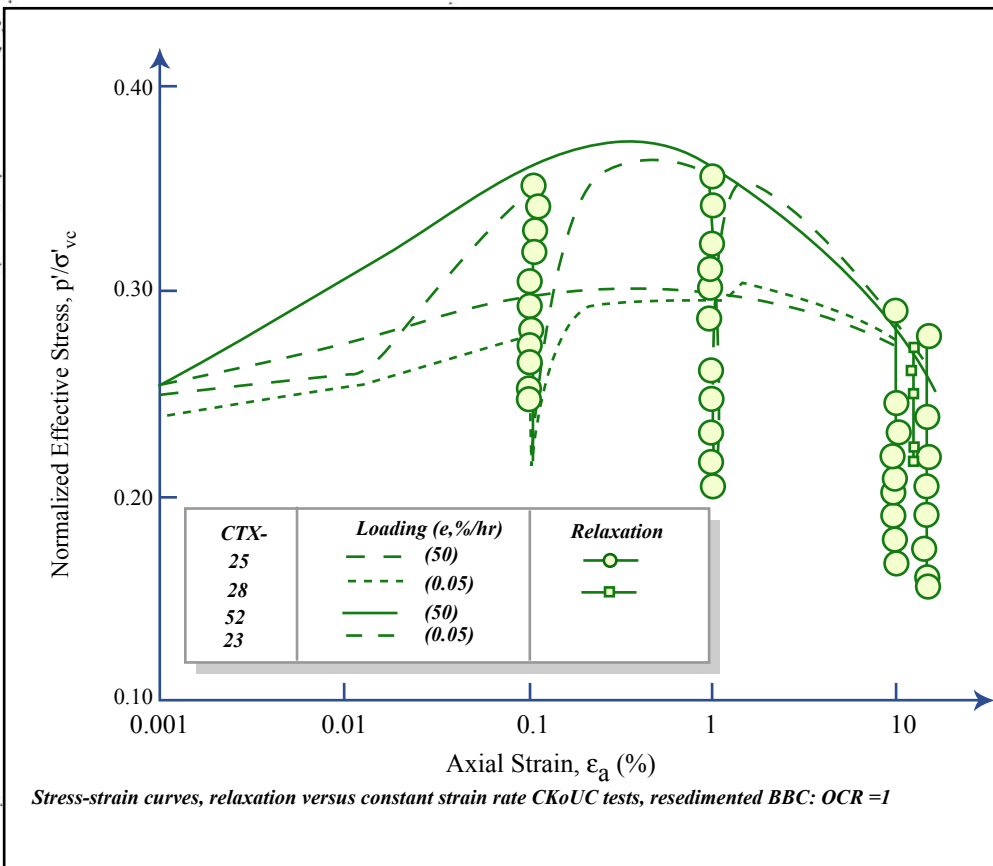
Variation of creep rate with time in constant stress creep

42 381 50 SHEETS 5 SQUARE
42 382 100 SHEETS 3 SQUARE
42 383 200 SHEETS 3 SQUARE
MADE IN U.S.A.



D

22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS



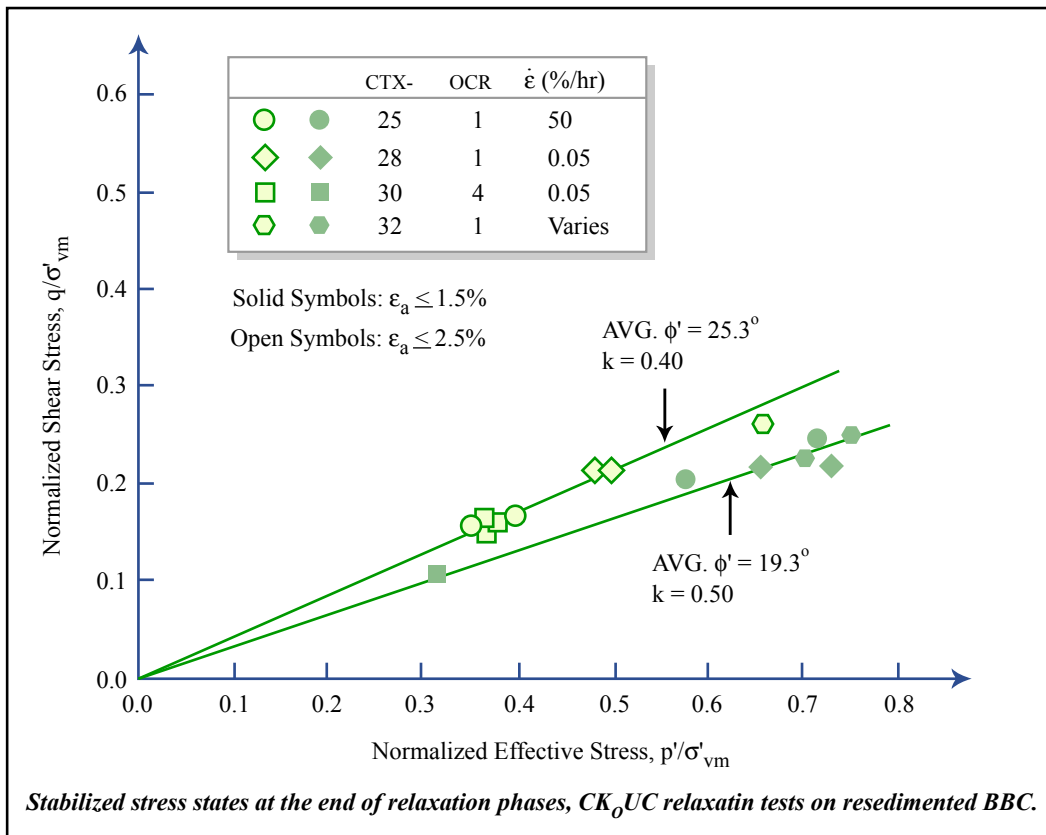
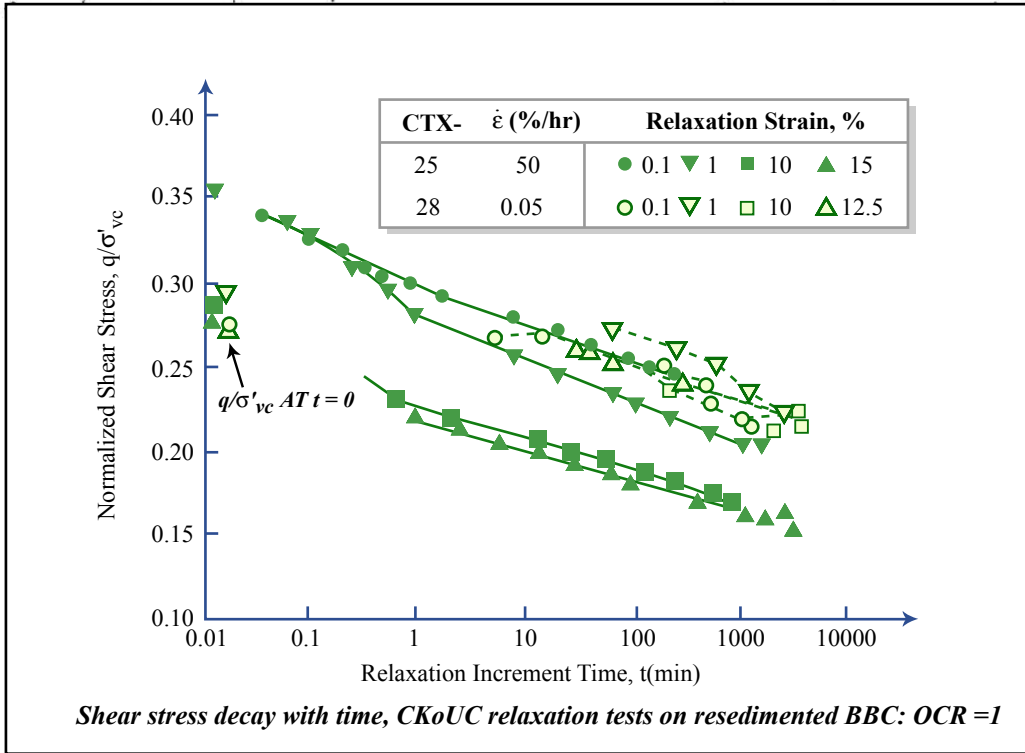
Figures by MIT OCW.

Relaxation data from CKoUC tests on RBBC

Adapted from: Sheahan et al. (1994)



22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS



Figures by MIT OCW.

Relaxation data from CKoUC tests on RBBC

Adapted from: *Sheahan et al. (1994)*