

## HOMWORK 2 - 10 pts total

2pts

1.  $V = 1 \text{ m}^3$   
 $S_r = 0.2$  residual saturation  
 $n = 0.25$  porosity

Mass balance: original vol. of TCE in soils  
 $= 1 \text{ m}^2 \times 0.25 \times 0.2 = 0.05 \text{ m}^3$

Density of TCE =  $1.47 \text{ g/cm}^3 = 1470 \text{ Kg/m}^3$

Initial mass TCE =  $1470 \frac{\text{Kg}}{\text{m}^3} \cdot 0.05 \text{ m}^3 = 74 \text{ Kg TCE}$

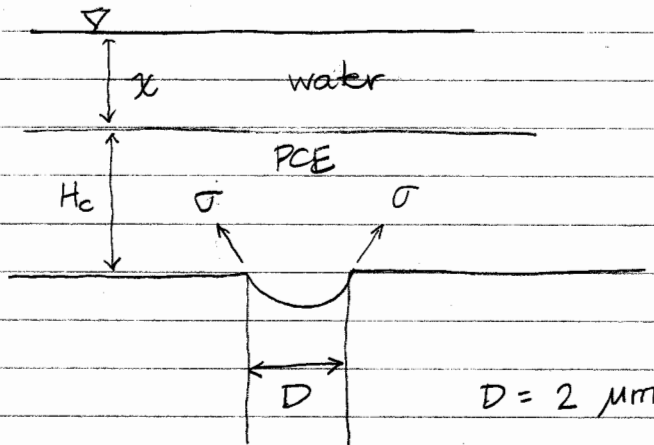
Assume TCE dissolves into rain water to solubility =  $1100 \text{ mg/L}$

Volume of rain =  $1 \text{ m}^2 \times 500 \text{ mm/yr} = 0.5 \text{ m}^3/\text{yr}$

Mass carried by rain =  $0.5 \text{ m}^3/\text{yr} \times 1000 \text{ mg/L} \cdot 10^3 \text{ L/m}^3$   
 $= 0.5 \times 10^6 \text{ mg/yr} = 0.5 \text{ Kg/yr}$

Time to remove TCE =  $\frac{74 \text{ Kg TCE}}{0.5 \text{ Kg TCE/yr}} = 150 \text{ years}$

3 pts  
2.



Properties of PCE

$$\rho_p = 1.63 \text{ g/cm}^3$$

$$\sigma = 44.4 \text{ dyn/cm}$$

$$1 \text{ dyn} = 1 \frac{\text{g cm}}{\text{sec}^2}$$

$$D = 2 \mu\text{m}$$

$$P_{\text{NAPL}} = \rho_w x g + \rho_p H_c g$$

$$P_{\text{WATER}} = \rho_w (x + H_c) g$$

$$a) \quad \Delta P = (\rho_p - \rho_w) H_c g = \frac{2\sigma}{r} \quad \text{for circular fracture}$$

$$0.63 \frac{\text{g}}{\text{cm}^3} H_c 9.8 \frac{\text{m}}{\text{s}^2} = \frac{2 \cdot 44.4 \frac{\text{g}}{\text{sec}^2}}{1 \mu\text{m}}$$

$$H_c = \frac{2 \cdot 44.4}{0.63 \cdot 9.8} \frac{\cancel{\text{g}}/\cancel{\text{sec}^2}}{\mu\text{m} \cancel{\text{g}}/\cancel{\text{cm}^3} \cancel{\text{m}}/\cancel{\text{s}^2}}$$

$$\frac{1}{10^{-6} \text{ m} / (10^{-2})^3 \text{ m}^3 \cdot \text{m}} = \text{m}$$

$$= 14 \text{ m}$$

b) For linear fracture,  $\sigma$  is exerted on both sides of fracture of length  $L$

Hydrostatic pressure is exerted on opening  $DL$

$$\Delta P DL = \sigma 2L$$

$$\Delta P = \Delta P H_c g = (\rho_p - \rho_w) H_c g$$

$$H_c = \frac{2\sigma}{\Delta \rho g D} = 7.2 \text{ m} \quad (\text{one half value for circular fracture})$$

3 pts

3.  $i = 0.005$        $t = 10$  years

As first approximation, consider only advective travel. Thus, downstream wells need to extend to distance  $L$ :

$$L = ut = \frac{Ki}{n} t$$

For each type soil, use literature values of  $K$  and  $n^*$

soil	$K$ (cm/s)	$n_e$	$L$
a. coarse sand	$9 \times 10^{-5} - 6 \times 10^{-1}$	0.2 - 0.35	48 km
b. fine sand	$2 \times 10^{-5} - 2 \times 10^{-2}$	0.1 - 0.3	1600 m
c. silt	$1 \times 10^{-7} - 2 \times 10^{-3}$	0.34 - 0.61	94 m
d. clay	$1 \times 10^{-9} - 5 \times 10^{-7}$	0.34 - 0.60	2 cm

To be conservative, I used high value of  $K$  and low value of  $n$  from range in Daniel.  $L$  is computed to one-digit accuracy commensurate with accuracy of  $K$ .

For finer soils, diffusion could be more important than advection.

$$D_h = D_d^* + \alpha_L u$$

$$D_d^* \approx 10^{-9} \text{ m/s}$$

Based on chart from Gelhar et al. (1992) given in Lecture 2, for 1 to 10 m scale,

$$\alpha_L \approx 1 \text{ m}$$

3. (continued)

Velocities and dispersion coeffs are =

	$u$ (m/yr)	$\alpha_L u$ (m <sup>2</sup> /s)	$D_h$ (m <sup>2</sup> /s)
b. fine sand	7	$2 \times 10^{-7}$	$2 \times 10^{-7}$
c. silt	0.5	$1 \times 10^{-8}$	$1 \times 10^{-8}$
d. clay	0.004	$1 \times 10^{-10}$	$1 \times 10^{-9}$

Evaluate transport with equation given in lecture 3:

$$c = \frac{c_0}{2} \operatorname{erfc} \left( \frac{R_d x - ut}{\sqrt{4R_d D_h t}} \right)$$

Assume  $\frac{c}{c_0} = 0.01$  is threshold

$R_d = 1$  to be conservative

$$\frac{c}{c_0} = 0.01 = \frac{1}{2} \operatorname{erfc} \left( \frac{x - ut}{\sqrt{4D_h t}} \right)$$

$\operatorname{erfc}(z) = 0.02$  at  $z \approx 1.2$

$$\frac{x - ut}{\sqrt{4D_h t}} = 1.2$$

$$x = ut + 2.4 \sqrt{D_h t}$$

Evaluate for different soils:

	$u$ (m/yr)	$D_h$ (m <sup>2</sup> /s)	$D_h$ (m <sup>2</sup> /yr)	$x$
b. fine sand	7	$2 \times 10^{-7}$	7	90 m
c. silt	0.5	$1 \times 10^{-8}$	0.5	10 m
d. clay	0.004	$1 \times 10^{-9}$	0.004	0.5 m

Note: diffusion dominates advection in clay, is about equal to advection in silt

Problem 3

$i = 0.005$   
 $t = 10 \text{ years}$   
 $\alpha_L = 1 \text{ m}$   
 $D_d^* = 1.00E-09 \text{ m/s}$

	Soil	K (cm/s)	$n_e$	u (m/s)	u (m/yr)	L (m)	$D_h$ (m <sup>2</sup> /s)	$D_h$ (m <sup>2</sup> /yr)	x (m)
a.	coarse sand	1.00E-02	0.24	2.08E-06	6.57E+01	657.00	2.08E-06	6.57E+01	657
b.	fine sand	1.00E-05	0.24	2.08E-09	6.57E-02	0.66	3.08E-09	9.72E-02	0.7
c.	silt	1.00E-06	0.35	1.43E-10	4.51E-03	0.05	1.14E-09	3.60E-02	0.05
d.	clay	1.00E-08	0.4	1.25E-12	3.94E-05	0.0004	1.00E-09	3.16E-02	0.0006

$$L = ut = (K/n_e) t$$

$$D_h = D_d^* + \alpha_L u$$

3. (continued)

Benzene computation:

$$K_{oc} = 83 \text{ mg/l}$$

$f_{oc}$  - check Technical Protocol  
can assume a value of  $f_{oc} \approx 0.001$  for all

$$\rho_b = 1.65 \text{ g/cm}^3$$

$$n = 0.3$$

$$R_d = 1 + \frac{\rho_b f_{oc} K_{oc}}{n} \approx 1.5$$

Monitoring for benzene would only need to be about  $\frac{2}{3}$  the distance of monitoring for MTBE.

2 pts  
4.

$$K = 1.6 \times 10^{-4} \text{ cm/s} = 0.45 \text{ ft/day}$$

$$\bar{i} = 0.035$$

$$L = 400 \text{ ft}$$

$$u = \frac{K \bar{i}}{n}$$

assume  $n$  for clay-silt = 0.3  $\therefore u = 0.05 \frac{\text{ft}}{\text{day}}$

$$\text{Ground-water travel time} = \frac{L}{u} = \frac{400 \text{ ft}}{0.05 \text{ ft/d}}$$

$$= 8000 \text{ days} = 22 \text{ years}$$

Need to find retardation factors for PCE, TCA, xylene

From Table C.3.3 of Technical Protocol for Evaluating Natural Attenuation of Chlorinated Solvents in Ground Water

$$f_{oc} \cong 0.002 \text{ for glacial till}$$

From Table A-1\*  $K_{oc}$  values are:

$$\text{PCE } K_{oc} = 364 \text{ L/kg}$$

$$\text{TCA } 152$$

$$\text{X } 240$$

$$\text{TCE } 126$$

$$\text{Bulk density, } \rho_b = 1.65 \frac{\text{g}}{\text{cm}^3} \text{ (typical value)} = 1.65 \frac{\text{kg}}{\text{L}}$$

$$\text{Porosity, } n = 0.3$$

Compound	$K_{oc}$ (L/kg)	$R_d = 1 + \frac{\rho_b K_d}{n} = 1 + \frac{\rho_b K_{oc} f_{oc}}{n}$	Travel time (yrs)
PCE	364	3.0	66
TCA	152	1.8	40
X	240	2.3	51
TCE	126	1.7	37

$$\text{Travel time} = \frac{L}{u/R_d} = R_d \frac{L}{u}$$

\* From Chemical reference information in course reader

4. (cont)

Whether compounds reach brook depends on chemistry  
PCE and TCE/A will degrade if conditions  
are anaerobic  
Xylene will degrade in aerobic

Given mix of chemicals at site, both anaerobic  
and aerobic zones are possible - I would  
expect chemicals to degrade over these long  
travel times, but not necessarily from  
areas of the site nearer the brook.