

Lecture 8 - Chemical Removal - Lime-Soda Ash Softening

Often necessary to remove certain chemicals from water and wastewater:

Water = iron and manganese
arsenic
hardness
nitrate
radionuclides
organic chemicals

Industrial wastewater = virtually any chemical, but especially
metals
organic chemicals

Hardness

A water is "hard" if:

1. soap does not easily form a foam or lather
2. the water leaves scale in hot-water pipes, boilers, etc.

Hardness arises from divalent metal ions in the water:

Ca^{++}
 Mg^{++}
 Sr^{++}
 Fe^{++}
 Mn^{++}

} come from natural rocks
in source area,
especially = limestones:
calcite - CaCO_3
dolomite $\text{CaMg}(\text{CO}_3)_2$

Prevalence of hard water nationwide reflects
geology - see Figure 19-8 from MWH, 2005

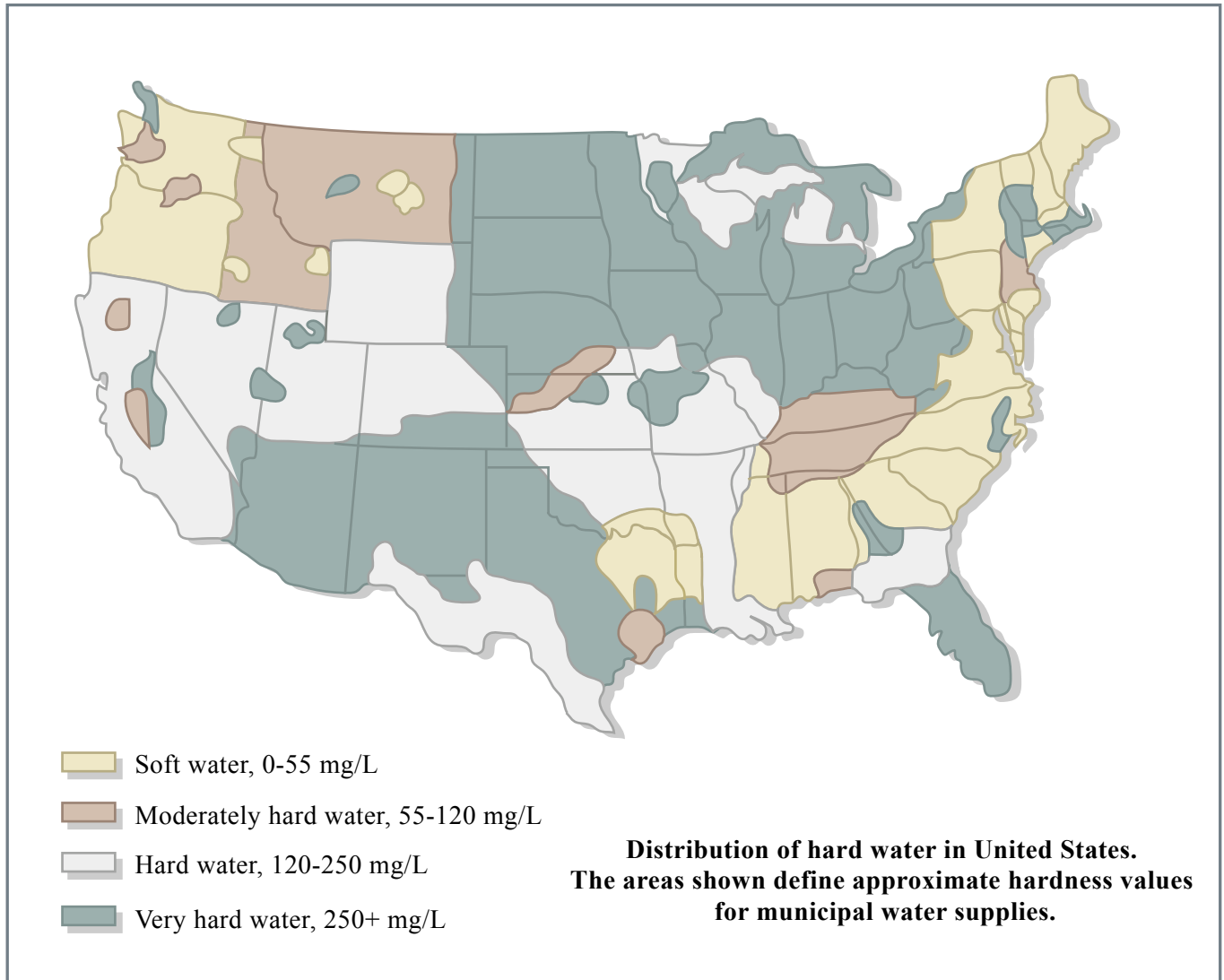


Figure by MIT OCW.

Adapted from: Dekker, Marcel. *Water and Water Pollution Handbook*. Edited by L. Ciaccio. New York, NY: 1971.

Different definitions of hardness

$$\text{Total hardness} = \sum [M^{++}] \times \frac{50}{\text{eq. wt. of } M^{++}}$$

Hardness is expressed in equivalents of CaCO_3

$$\begin{array}{rclcl} \text{Ca} & - & \text{MW} = 40 & \times 1 & = 40 \\ \text{C} & - & \text{MW} = 12 & \times 1 & = 12 \\ \text{O} & - & \text{MW} = 16 & \times 3 & = 48 \\ & & & & \hline & & & & 100 = \text{MW} \end{array}$$

Since Ca^{++} and CO_3^{--} have valence of 2,
equivalent weight of $\text{CaCO}_3 = 100/2 = 50$

Example water: (Ex 11.4, pg. 445 of V&H):

$$\begin{array}{ll} \text{CO}_2 = 8.8 \text{ mg/L as CO}_2 & \text{Alk (HCO}_3^-) = 115 \text{ mg/L} \\ \text{Ca}^{2+} = 70 \text{ mg/L} & \text{as CaCO}_3 \\ \text{Mg}^{2+} = 9.7 \text{ mg/L} & \text{SO}_4^{2-} = 96 \text{ mg/L} \\ \text{Na}^+ = 6.9 \text{ mg/L} & \text{Cl}^- = 10.6 \text{ mg/L} \end{array}$$

<u>M⁺⁺</u>	<u>conc</u> (mg/L)	<u>MW</u>	<u>eq. wt.</u>	<u>hardness</u>
Ca^{2+}	70	40	20	175
Mg^{2+}	9.7	24.4	12.2	39.8
				<u>214.8</u>

pretty hard
water!

Most hardness is due to Ca and Mg

Ca hardness = that due to Ca

Mg hardness = that due to Mg

Total hardness \cong Ca hardness + Mg hardness

Carbonate hardness = part of total hardness
equivalent to carbonate plus bicarbonate
alkalinity

Refresher on alkalinity [ALK]:

ALK = capacity for solutes to neutralize a strong acid

$$= \Sigma [\text{strong bases}] - \Sigma [\text{strong acids}]$$

in equivalents per liter

Strong acids are those that completely dissociate
in water: HCl, H₂SO₄, HNO₃, HBr, HI, HClO₄

Strong bases completely dissociate = NaOH, KOH,
Ca(OH)₂, Mg(OH)₂, LiOH, RbOH, Sr(OH)₂,
Ba(OH)₂

$$[\text{ALK}] = [\text{Na}^+] + [\text{K}^+] + 2[\text{Ca}^{++}] + 2[\text{Mg}^{++}]$$

$$- [\text{Cl}^-] - 2[\text{SO}_4^{=}] - [\text{NO}_3^-]$$

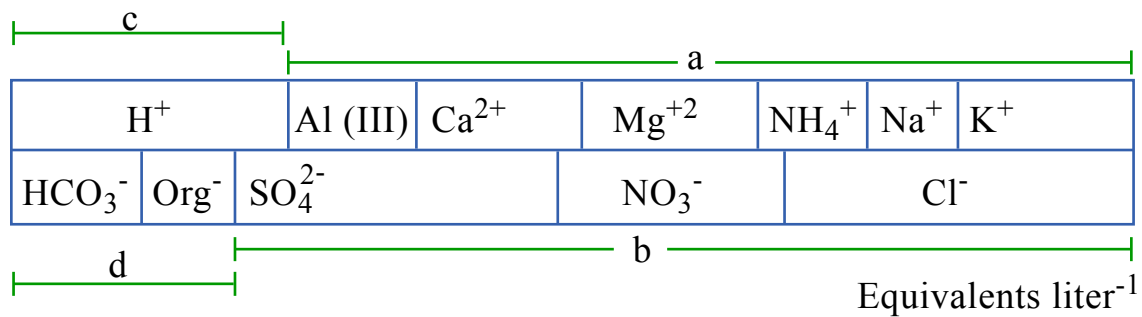
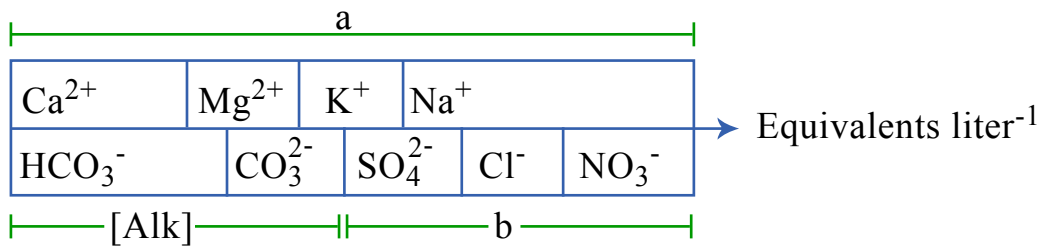
$$= \Sigma[\text{SB}] - \Sigma[\text{SA}]$$

Can also find charge balance assuming carbonates
dominate system

$$\Sigma[\text{SB}] + [\text{H}^+] = \Sigma[\text{SA}] + [\text{OH}^-] + 2[\text{CO}_3^{=}] + [\text{HCO}_3^-]$$

$$\Sigma[\text{SB}] - \Sigma[\text{SA}] = [\text{ALK}]$$

$$= [\text{OH}^-] - [\text{H}^+] + 2[\text{CO}_3^{=}] + [\text{HCO}_3^-]$$



Natural water charge balance for an alkaline system (Alk = a-b) and
an acid system (Alk = a-b = d-c).

Figure by MIT OCW.

Adapted from: Schnoor, J. L. *Environmental Modeling: fate and transport of pollutants in water, air, and soil*. New York, NY: John Wiley & Sons. 1996.

Carbonate hardness (for $[Alk]$ in terms of $CaCO_3$)

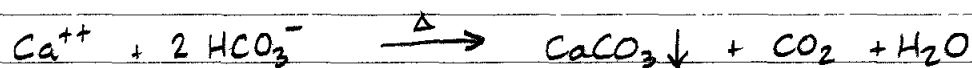
If $[Alk] < \text{total hardness}$,

then carbonate hardness = $[Alk]$

If $[Alk] > \text{total hardness}$,

then carbonate hardness = total hardness

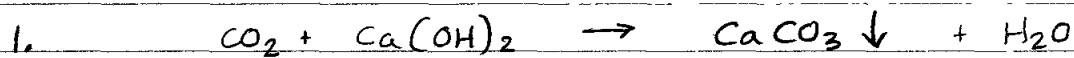
Carbonate hardness causes scaling at high temps:



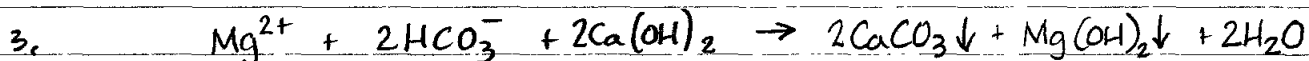
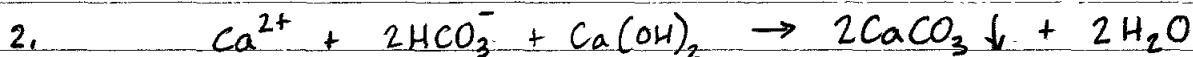
Noncarbonate hardness = total hardness - carbonate hardness

For water treatment, carbonate hardness is removed by adding lime $Ca(OH)_2$:

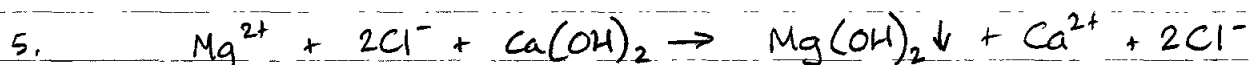
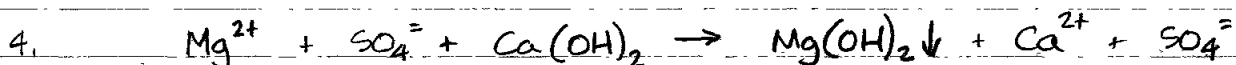
First lime reacts with any CO_2 :



Then lime reacts to remove carbonate hardness



And finally to remove non-carbonate Mg hardness

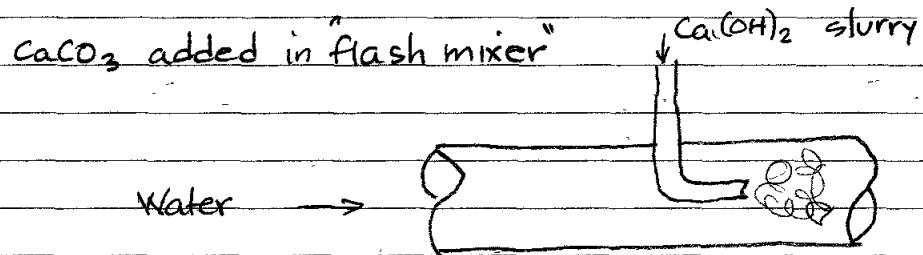


Reactions 4. and 5. simply swap Mg noncarbonate hardness for Ca noncarbonate hardness

Reactions 1-5 remove magnesium hardness and calcium carbonate hardness. Calcium noncarb hardness in original solution plus that created removing Mg hardness remain.

For waters low in Mg and with carbonate Ca hardness, this would be sufficient treatment - called "single-stage lime treatment", "single-stage softening", or "undersoftening"

Typical process in water-treatment plant:

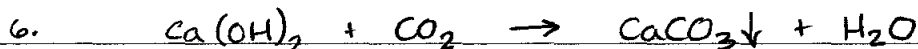


Water/lime mix goes into flocculator, then clarifier to precipitate and remove CaCO_3 ($T_R = 1-2$ hrs)

Water is then "recarbonated"

Recarbonation is needed because addition of Ca(OH)_2 raises pH of water to 10.2 to 10.5

Recarbonation consists of bubbling CO_2 through treated water, lowering pH to 8.7 to 9.0:



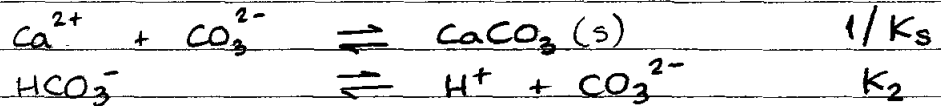
Recarbonation is also done to "stabilize" the water

If water is supersaturated with CaCO_3 , it will precipitate as "scale"

If water is undersaturated, water can be "aggressive" and cause pipe corrosion

Ideal is to keep water slightly oversaturated to maintain thin protective coat of CaCO_3 on inside of pipe

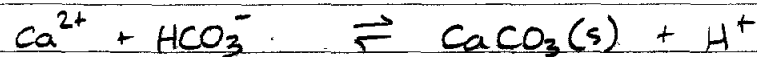
Scale precipitation involves two chemical reactions:



$$K_s = \frac{[\text{Ca}^{2+}][\text{CO}_3^{2-}]}{[\text{CaCO}_3(s)]}$$

$$K_2 = \frac{[\text{CO}_3^{2-}][\text{H}^+]}{[\text{HCO}_3^-]}$$

Overall reaction:



$$K = \frac{[\text{Ca}^{2+}][\text{HCO}_3^-]}{[\text{H}^+]} = \frac{K_s}{K_2}$$

Rearrange to get:

$$[\text{H}^+] = \frac{[\text{Ca}^{2+}][\text{HCO}_3^-]}{K}$$

$$[H^+] = \frac{[Ca^{2+}][HCO_3^-]}{K}$$

$$\log [H^+] = \log [Ca^{2+}] + \log [HCO_3^-] - \log K$$

$$-\log [H^+] = -\log [Ca^{2+}] - \log [HCO_3^-] + \log (K_1/K_2)$$

$$pH_{eq} = pCa + p[HCO_3^-] + \log (K_1/K_2)$$

$$\approx pCa + p[Alk] + \log (K_1/K_2)$$

↑ to denote this is pH at CaCO₃ equilibrium

$$I = pH_{actual} - pH_{eq} \equiv SI$$

Langlier Stability Index

$I > 0 \rightarrow CaCO_3$ precipitates ($pH_{actual} > pH_{eq}$)

$I = 0 \rightarrow$ stable

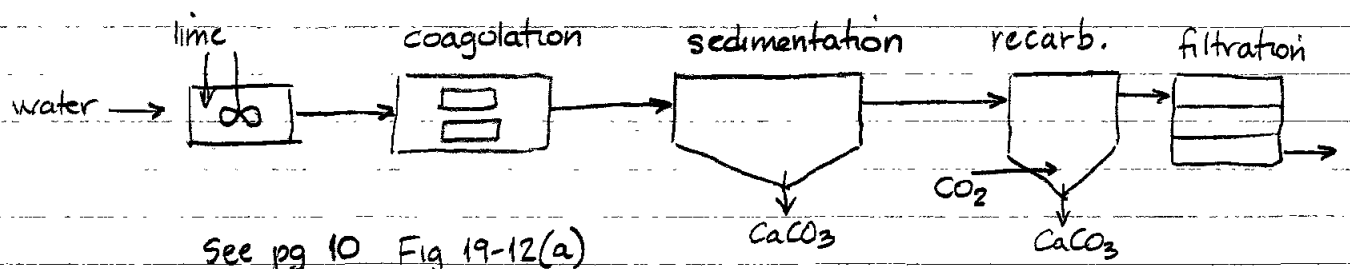
$I < 0 \rightarrow CaCO_3$ dissolves

$I = 0.2$ is desirable - carbonation steps seeks to set $I \approx 0.2$

K_1, K_2 are functions of temp.

$pK_1 = 8.4 \quad pK_2 = 10.4 \quad \text{at } T = 15^\circ C$

conventional lime treatment process looks like:



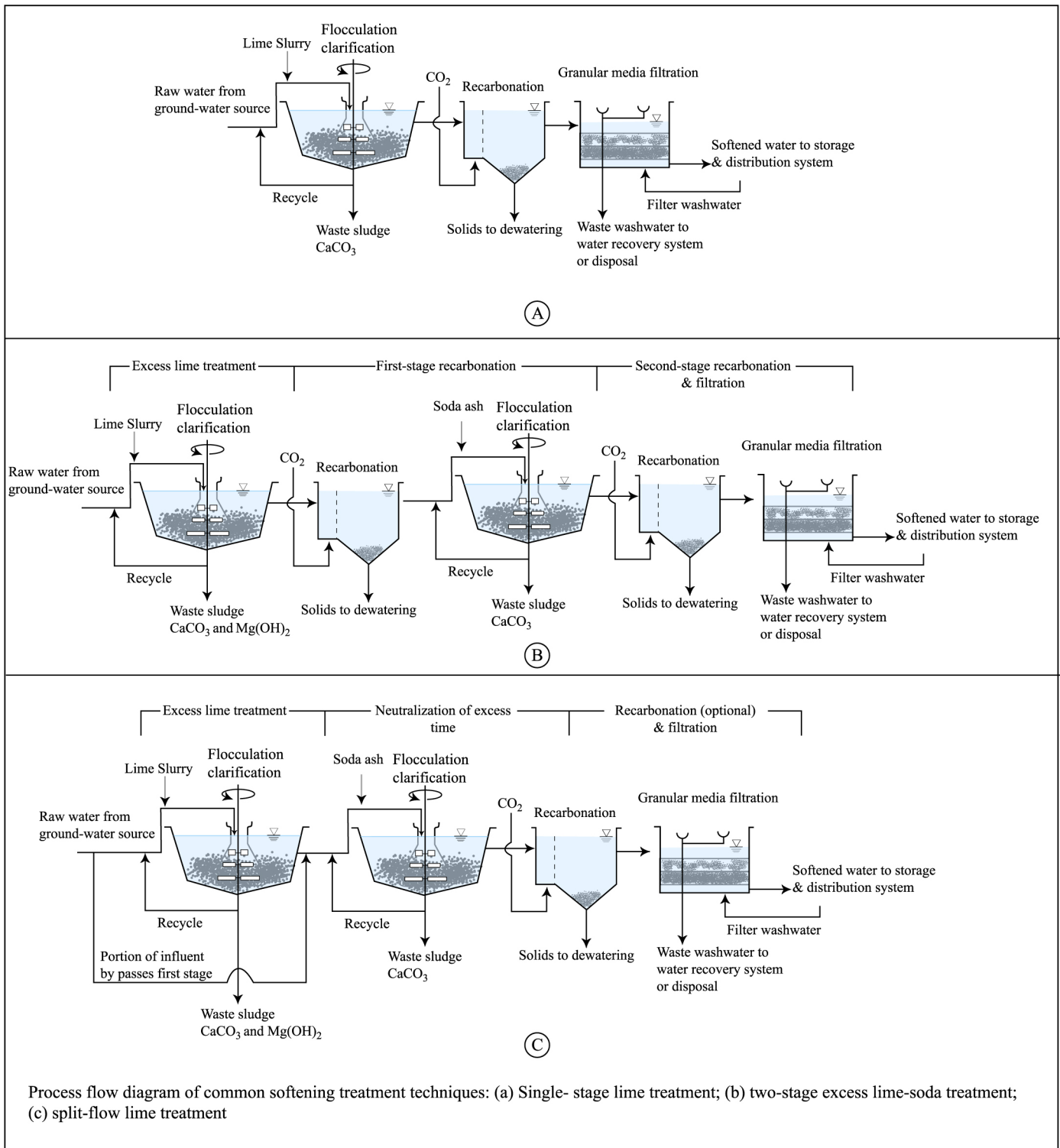
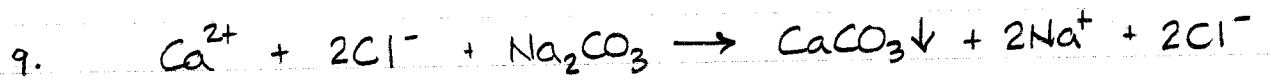
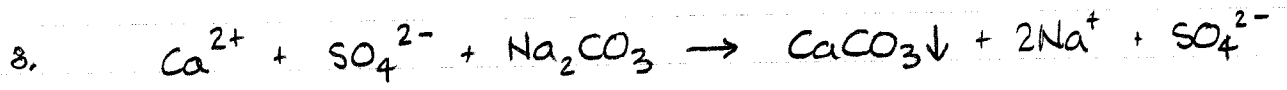


Figure by MIT OCW.

Adapted from: MWH, J. C. Crittenden, R. R. Trussell, D. W. Hand, K. J. Howe, and G. Tchobanoglous. *Water Treatment: Principles and Design*. 2nd ed. Hoboken, NJ: John Wiley & Sons, 2005, p. 1601.

For waters with non-carbonate hardness, single-stage softening is insufficient. Leftover hardness is removed by addition of soda ash (Na_2CO_3)

NaX



Practical limits of lime-soda ash softening are dictated by solubility of precipitates: CaCO_3 & $\text{Mg}(\text{OH})_2$

Ca: 30 mg/L as CaCO_3

Mg: 10 mg/L as CaCO_3

Total hardness = 40 mg/L as CaCO_3

In practice, residual hardness = 50 to 80 mg/L

This water has high pH and needs to be recarbonated

Lime-soda ash treatment is usually treated by "two-stage softening" also called "excess-lime treatment" and "split recarbonation treatment"

See pg 10 Fig 19-12(b) from MWH

Split treatment is similar, except only part of water is treated with lime. Other part by-passes lime treatment and gets soda-ash treatment along with lime-treated water

The CO_2 in untreated water neutralizes high pH in lime-treated water and recarb. is not needed

Water split is computed such that enough Mg is removed in lime-treated water to meet target Mg level in combined finished water

Computing chemical doses for lime soda ash softening - Example 11.4
 from Vicsman and Hammer, pg. 445 - pg 13 and 14

$$\text{CO}_2 = 8.8 \text{ mg/L as CO}_2$$

$$\text{Ca}^{2+} = 70 \text{ mg/L}$$

$$\text{Mg}^{2+} = 9.7 \text{ mg/L}$$

$$\text{Na}^+ = 6.9 \text{ mg/L}$$

$$\text{Alk} = 115 \text{ mg/L as CaCO}_3$$

$$\text{SO}_4^{2-} = 96 \text{ mg/L}$$

$$\text{Cl}^- = 10.6 \text{ mg/L}$$

Easiest method is to construct a table that converts all concentrations to equivalent concentrations, and then to equivalents of CaCO_3

Also use chart from VH Fig 11.8, pg 446

	<u>mg/L</u>	<u>MW</u>	<u>equiv</u>	<u>eq wt</u>	<u>meq/L</u>	<u>mg/L as CaCO₃</u>
CO_2	8.8	44.0	2	22.0	0.4	20.0
Ca^{2+}	70	40.0	2	20.0	3.5	175.
Mg^{2+}	9.7	24.4	2	12.2	0.80	39.8
Na^+	6.9	23.0	1	23.0	0.30	15.0
					4.6	229.8
Alk	115	100	2	50.0	2.3	115.0
SO_4^{2-}	96	96.0	2	48.0	2.0	100.0
Cl^-	10.6	35.5	1	35.5	0.30	14.9
					4.6	229.9

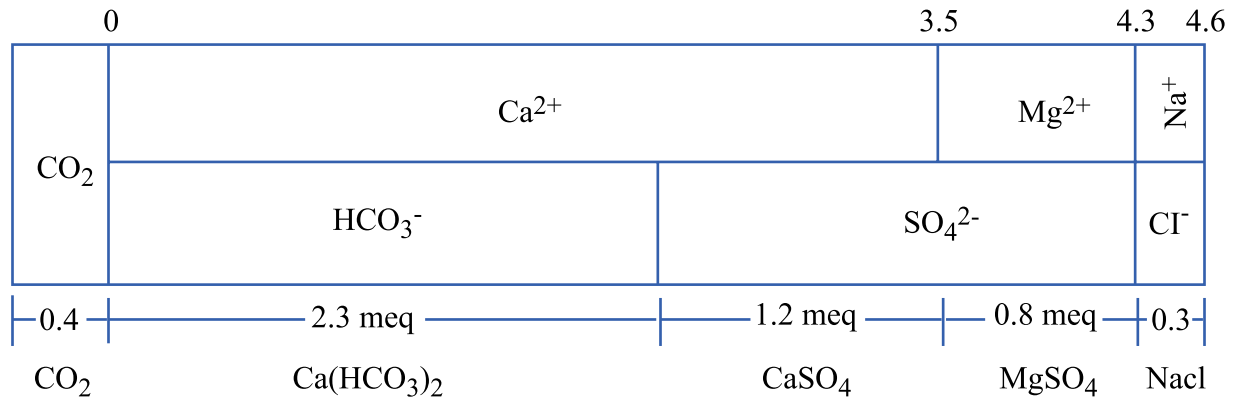
$$\text{Total hardness} = \text{Ca}^{2+} + \text{Mg}^{2+} = 175 + 39.8 = 214.8 \text{ mg/L as CaCO}_3$$

$$\text{Carbonate hardness} = [\text{Alk}] = 115 \text{ mg/L as CaCO}_3$$

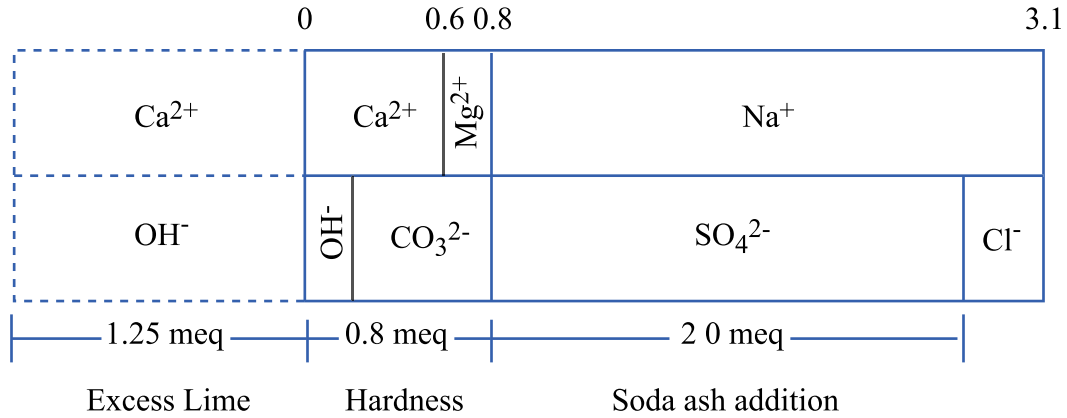
$$\text{Noncarbonate hardness} = \text{TH} - \text{CH} = 99.8 \text{ mg/L as CaCO}_3$$

$$\text{Mg noncarbonate hardness} = 39.8 \text{ mg/L as CaCO}_3$$

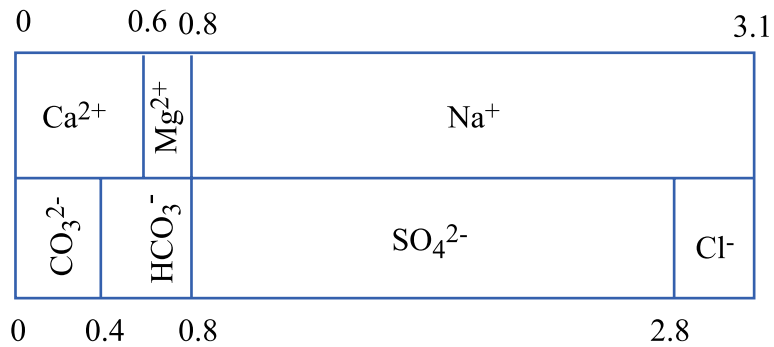
Milliequivalent Bar Graph for Example 11.4



(A) Bar graph & hypothetical chemical combinations in the raw water



(B) Bar graph of the water after lime & soda ash additions & settling but before recarbonation.



(C) Bar Graph of the water after two-stage recarbonation & final filtration

Figure by MIT OCW.

Before treatment:

0.4	0		3.5	4.3	4.6
CO ₂	Ca ²⁺		Mg ²⁺	Na ⁺	
HCO ₃ ⁻		SO ₄ ²⁻		Cl ⁻	
		2.3			
0.4 CO ₂	2.3 meq Ca(HCO ₃) ₂ Carbonate hardness	1.2 meq CaSO ₄ Non-carb. hardness	0.8 meq MgSO ₄ NCH	0.3 NaCl	

**After treatment with lime Ca(OH)₂ and intermediate reaction to remove carbonate hardness:
(chemical equations 1, 2, & 3)**

1.25	0	1.2	2.0	2.3
Ca ²⁺	Ca ²⁺		Mg ²⁺	Na ⁺
OH ⁻	SO ₄ ²⁻		Cl ⁻	
1.25 meq excess lime	2.0 meq NCH		0.3 NaCl	

**After treatment with lime and intermediate reaction to remove noncarbonate Mg hardness:
(chemical equations 4 & 5)**

1.25	0	1.8	2.0	2.3
Ca ²⁺	Ca ²⁺		Mg	Na ⁺
OH ⁻	SO ₄ ²⁻		Cl ⁻	
1.25 meq excess lime	2.0 meq NCH		0.3 NaCl	

**After treatment with soda ash Na₂CO₃:
(chemical equations 8 & 9)**

1.25	0	0.6	0.8	2.8	3.1
Ca ²⁺	Ca ²⁺	Mg	Na ⁺		
OH ⁻	HCO ₃ ²⁻	SO ₄ ²⁻		Cl ⁻	
1.25 meq excess lime	residual 0.8 meq hardness	2.0 meq added soda ash		0.3 NaCl	

**After recarbonation:
(chemical equations 6 & 7)**

0	0.6	0.8	2.8	3.1
Ca ²⁺	Mg	Na ⁺		
HCO ₃ ⁻	SO ₄ ²⁻		Cl ⁻	
residual 0.8 meq hardness	2.0 meq added soda ash		0.3 NaCl	

Lime required

For CO_2 - 20.0 mg/L as CaCO_3

For carbonate hardness - 115.0

For Mg noncarbonate hardness - 39.8

174.8 mg/L as CaCO_3
(3.5 meq)

Convert from CaCO_3 to CaO

$$\frac{\text{CaO}}{\text{CaCO}_3} = \frac{40+16}{40+12+3 \times 16} = \frac{56}{100} = \frac{28}{50}$$

$$174.8 \text{ mg/L as CaCO}_3 = 97.9 \text{ mg/L as CaO}$$

Include excess lime of 35 mg/L

$$\text{Req'd lime} = 133 \text{ mg/L}$$

soda Ash for noncarbonate hardness

$$\text{NCH} = 99.8 \text{ mg/L as CaCO}_3 \quad (2.0 \text{ meq})$$

(recall that Mg NCH was treated with lime but simply swaps Ca for Mg, so still needs treatment with soda ash)

$$\text{Req'd Soda Ash} - 99.8 \text{ mg/L as CaCO}_3$$

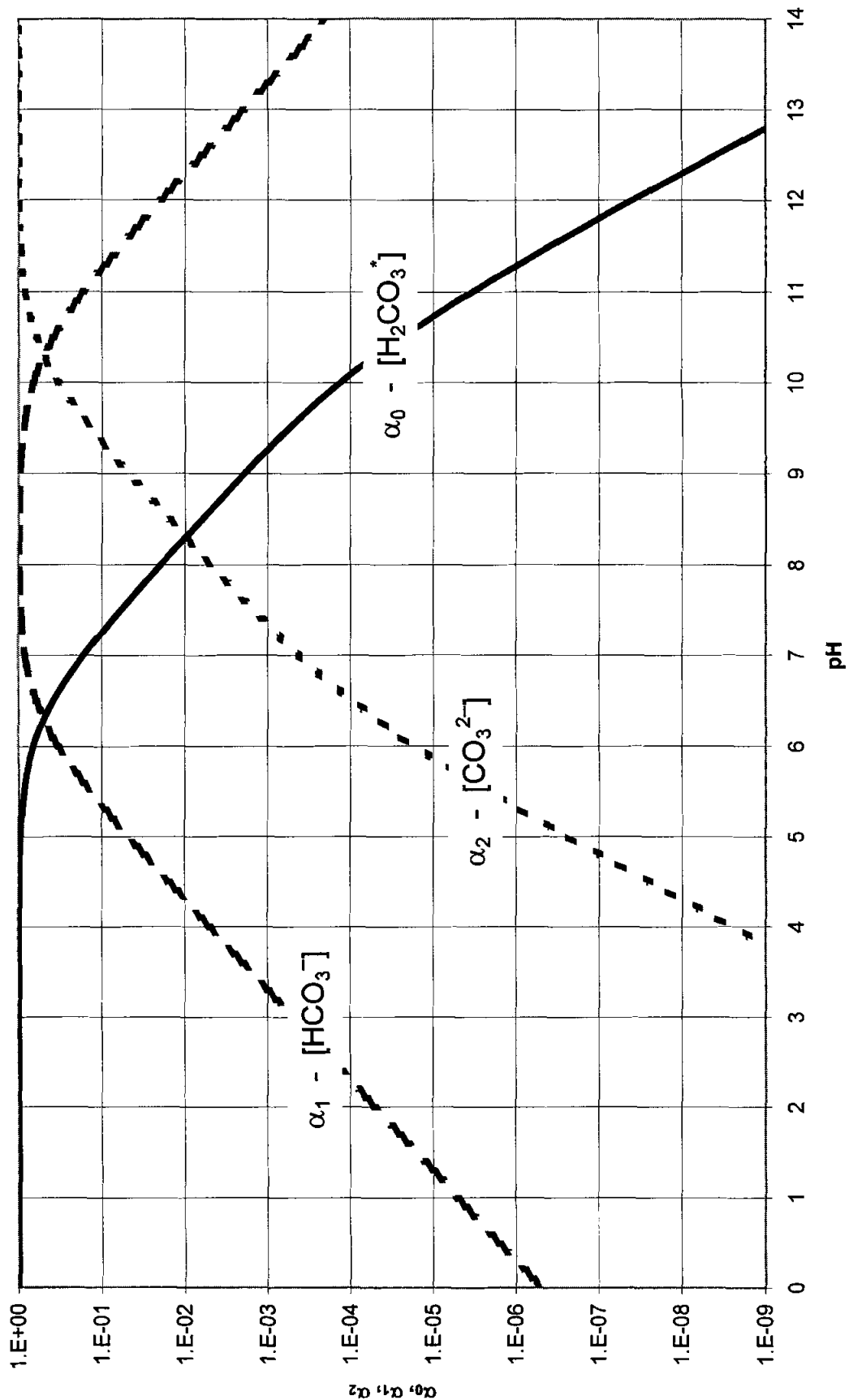
Convert to Na_2CO_3 :

$$\frac{\text{Na}_2\text{CO}_3}{\text{CaCO}_3} = \frac{2 \times 23 + 12 + 3 \times 16}{40 + 12 + 3 \times 16} = 1.06$$

$$\text{Req'd soda ash} = 1.06 \times 99.8 = 106 \text{ mg/L}$$

Note that pg 14 shows HCO_3^- but will actually be an equilibrium between CO_2 , HCO_3^- , CO_3^{2-} depending on pH per pg 16

Carbonate system equilibrium



Summary of chemical dosage calculations required for lime & lime-soda ash softening*

PROCESS	REQUIRED CHEMICAL DOSAGE CALCULATIONS
<p>Single-Stage Lime: For waters with high calcium, low magnesium, & carbonate hardness</p>	<p>Lime addition for softening: $\text{CaO} = \{ \text{carbonic acid concentration} \} + \{ \text{calcium carbonate hardness} \}$ </p> <p>Soda ash addition for softening: $\text{Na}_2\text{CO}_3 = \text{none}$ </p> <p>Carbon dioxide for pH adjustment after softening:</p> $\text{CO}_2 = \left\{ \begin{array}{l} \text{estimated carbonate} \\ \text{alkalinity of softened} \\ \text{water} \end{array} \right\} = \left\{ \begin{array}{l} \text{source water} \\ \text{alkalinity} \end{array} \right\} - \left\{ \begin{array}{l} \text{source water} \\ \text{calcium} \\ \text{hardness} \end{array} \right\}$ $+ \left\{ \begin{array}{l} \text{estimated residual} \\ \text{calcium hardness} \\ \text{of softened water} \end{array} \right\}$
<p>Excess Lime: For waters with high calcium, high magnesium, and carbonate hardness; process may be one or two stages</p>	<p>Lime addition for softening:</p> $\text{CaO} = \left\{ \begin{array}{l} \text{carbonic acid} \\ \text{concentration} \end{array} \right\} + \left\{ \begin{array}{l} \text{total alkalinity} \end{array} \right\} + \left\{ \begin{array}{l} \text{magnesium} \\ \text{hardness} \end{array} \right\} + \left\{ \begin{array}{l} \text{excess lime} \\ \text{dose} \end{array} \right\}$ <p>Soda ash addition for softening: $\text{Na}_2\text{CO}_3 = \text{none}$ </p> <p>Carbon dioxide for pH adjustment after softening:</p> $\text{CO}_2 = \left\{ \begin{array}{l} \text{source water} \\ \text{alkalinity} \end{array} \right\} - \left\{ \begin{array}{l} \text{source water} \\ \text{total hardness} \end{array} \right\} - \left\{ \begin{array}{l} \text{excess lime} \\ \text{dose} \end{array} \right\} + \left\{ \begin{array}{l} \text{estimated residual} \\ \text{calcium hardness} \\ \text{of softened water} \end{array} \right\}$ $+ 2 \left\{ \begin{array}{l} \text{excess lime} \\ \text{dose} \end{array} \right\} + \left\{ \begin{array}{l} \text{estimated residual} \\ \text{magnesium hardness} \\ \text{of softened water} \end{array} \right\}$
<p>Single-Stage Lime Soda Ash: For water with high calcium, low magnesium, & carbonate and noncarbonate hardness</p>	<p>Lime addition for softening: $\text{CaO} = \{ \text{carbonic acid concentration} \} + \{ \text{calcium carbonate hardness} \}$ </p> <p>Soda ash addition for softening: $\text{Na}_2\text{CO}_3 = \{ \text{calcium noncarbonate hardness} \} \text{ and/or } \{ \text{magnesium noncarbonate hardness} \}$ </p> <p>Carbon dioxide for pH adjustment after softening:</p> $\text{CO}_2 = \left\{ \begin{array}{l} \text{source water} \\ \text{alkalinity} \end{array} \right\} + \left\{ \begin{array}{l} \text{soda ash} \\ \text{dose} \end{array} \right\} - \left\{ \begin{array}{l} \text{source water} \\ \text{calcium} \\ \text{hardness} \end{array} \right\} + \left\{ \begin{array}{l} \text{estimated residual} \\ \text{calcium hardness} \\ \text{of softened water} \end{array} \right\}$
<p>Excess Lime - Soda Ash: For waters with high calcium, high magnesium, and carbonate and noncarbonate hardness; process may be one or two stages</p>	<p>Lime addition for softening:</p> $\text{CaO} = \left\{ \begin{array}{l} \text{carbonic acid} \\ \text{concentration} \end{array} \right\} + \left\{ \begin{array}{l} \text{calcium carbonate} \\ \text{concentration} \end{array} \right\} + 2 \left\{ \begin{array}{l} \text{magnesium} \\ \text{carbonate} \\ \text{hardness} \end{array} \right\} + \left\{ \begin{array}{l} \text{magnesium} \\ \text{noncarbonate} \\ \text{hardness} \end{array} \right\}$ $+ \left\{ \begin{array}{l} \text{excess lime} \\ \text{requirement} \end{array} \right\}$ <p>Soda ash addition for softening:</p> $\text{Na}_2\text{CO}_3 = \left\{ \begin{array}{l} \text{calcium} \\ \text{noncarbonate} \\ \text{hardness} \end{array} \right\} + \left\{ \begin{array}{l} \text{magnesium} \\ \text{noncarbonate} \\ \text{hardness} \end{array} \right\}$ <p>Carbon dioxide for pH adjustment after softening:</p> $\text{CO}_2, \text{ first stage} = \left\{ \begin{array}{l} \text{estimated hydroxide} \\ \text{alkalinity of softened} \\ \text{water} \end{array} \right\} = \left\{ \begin{array}{l} \text{excess lime} \\ \text{dose} \end{array} \right\} + \left\{ \begin{array}{l} \text{estimated residual} \\ \text{magnesium hardness} \\ \text{of softened water} \end{array} \right\}$ $\text{CO}_2, \text{ second stage} = \left\{ \begin{array}{l} \text{estimated hydroxide} \\ \text{alkalinity of softened} \\ \text{water} \end{array} \right\} = \left\{ \begin{array}{l} \text{source water} \\ \text{alkalinity} \end{array} \right\} + \left\{ \begin{array}{l} \text{soda ash} \\ \text{dose} \end{array} \right\} - \left\{ \begin{array}{l} \text{source} \\ \text{water total} \\ \text{hardness} \end{array} \right\}$ $+ \left\{ \begin{array}{l} \text{estimated residual} \\ \text{hardness of softened} \\ \text{water} \end{array} \right\}$

* All quantities are expressed as mg/L as CaCO₃

Figure by MIT OCW.