

# SOLID LIQUID SEPARATION: CENTRIFUGATION

CHARLES L. COONEY  
DOWNSTREAM PROCESSING  
COURSE

MIT Professional Institute

August 1-5, 2005

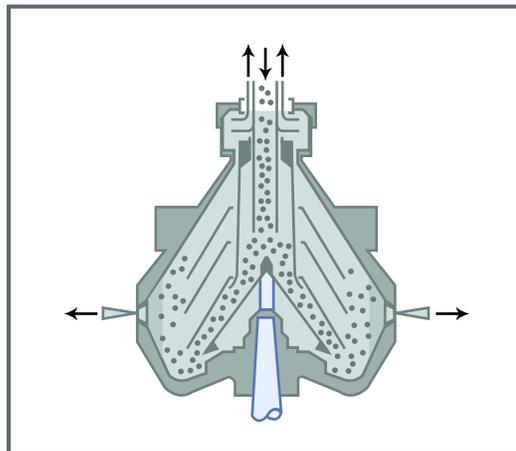


Figure by MIT OCW.

# Centrifugation is Effective in Volume Reduction

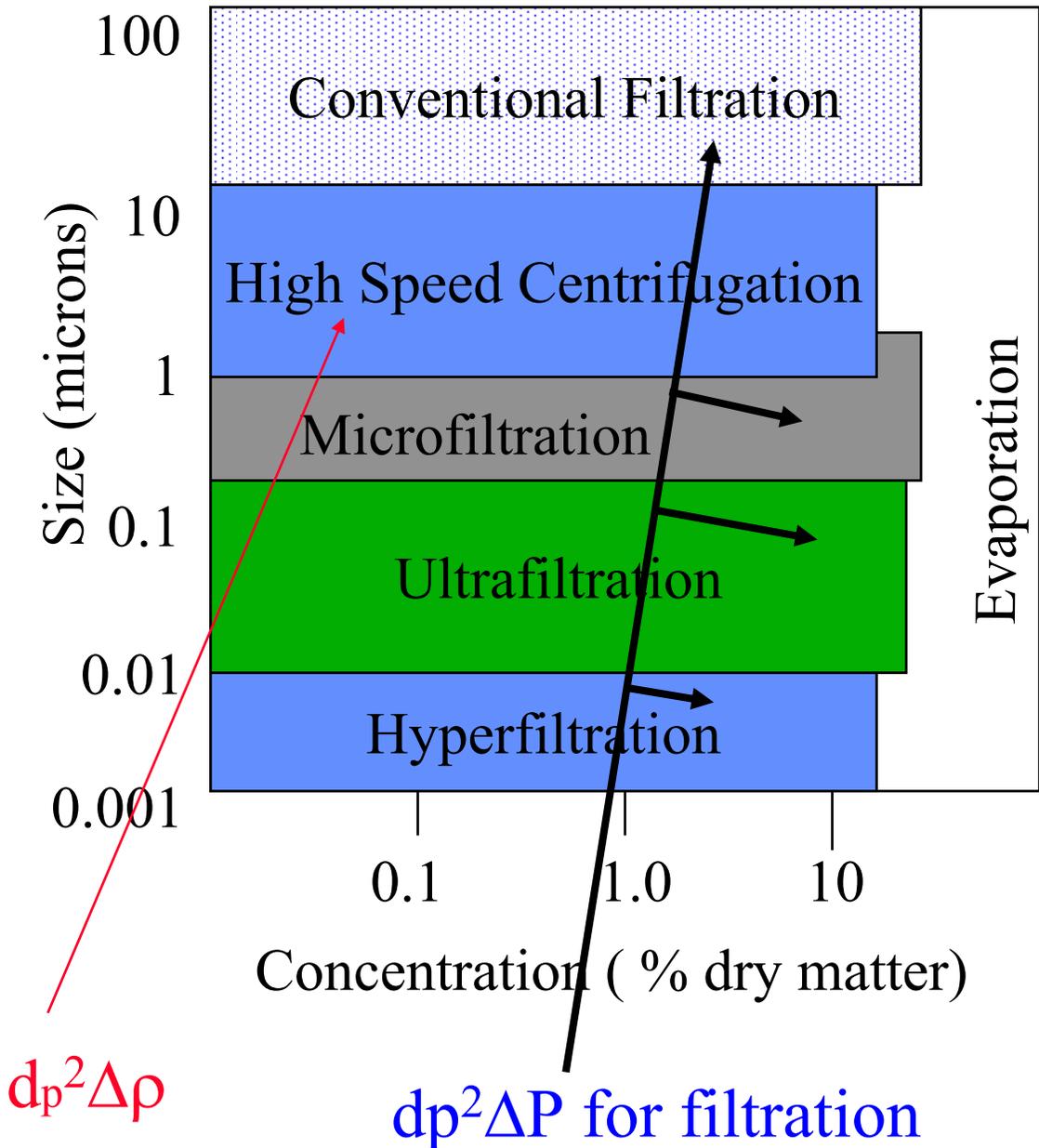
## Characteristics of process streams in primary recovery

- Volume at or near process maximum
- Heterogeneous solid/liquid mixture
- Particle size distribution
- Typical particle sizes:
  - Bacteria 1 to 2  $\mu$
  - Yeast 3 to 5  $\mu$
  - Actinomyces 2 to 30  $\mu$
  - Molds 4 to >30  $\mu$
  - Microbial flocs 10 to >100  $\mu$
  - Cell debris <1  $\mu$
  - Solids content: 1-10% dry basis  
5-50% wet basis
- Time variable product and stream quality
- Viscosity: 1 to >5,000 cp
- Temperature: 4-40 C
- Mechanically (shear) sensitive materials
- Temperature and pH sensitive materials
- Potentially toxic materials

# Centrifuge Equipment Process Needs

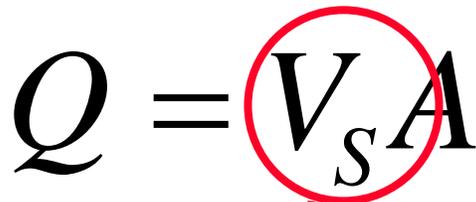
- Cleaning in place (CIP)
- Steam in place (SIP)
- Automation for start-up and operation
- Short process times
- Flexibility in process stream properties
- Temperature control
- Containment to prevent entry of contaminants and release of solvents or toxic materials
- Corrosion resistance
- Small footprint
- Fail safe system in case of off-balance
- Continuous operation for long times
- Interface with upstream and downstream operations

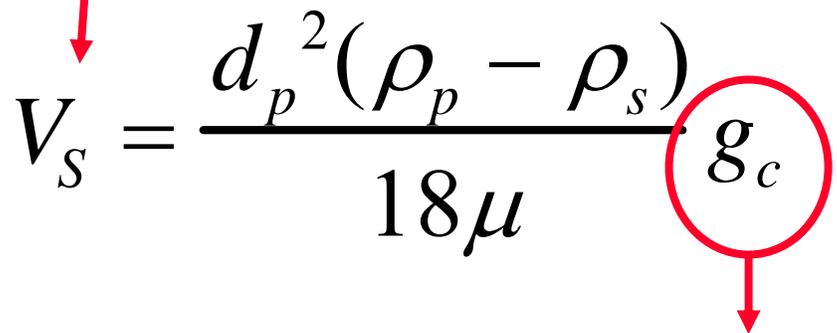
# OPERATING REGION FOR SOLID/LIQUID SEPARATION AND SOLUTE CONCENTRATION



# STOKE'S LAW

## CALCULATION OF CENTRIFUGE THROUGHPUT, Q

$$Q = V_s A$$


$$V_s = \frac{d_p^2 (\rho_p - \rho_s)}{18\mu} g_c$$


Q= Volumetric throughput (cm<sup>3</sup>/s)

V<sub>s</sub>=Sedimentation velocity (cm/s)

d<sub>p</sub>=particle diameter (cm)

ρ<sub>p</sub>=particle density (g/cm<sup>3</sup>)

ρ<sub>s</sub>=solvent density (g/cm<sup>3</sup>)

μ=solvent viscosity (g/cm-s)

g<sub>c</sub>=gravitational constant (cm/s<sup>2</sup>)

# Implications of Stoke's Law

## **Causes for deviation**

- Non-spherical particles
- Non-Newtonian rheology
- Hindered settling
- Non-uniform flow

## **Opportunities to improve**

- Increase particle size
- Increase density difference
- Reduce viscosity
- Increase gravitational force

# Continuous Separation in a Tank

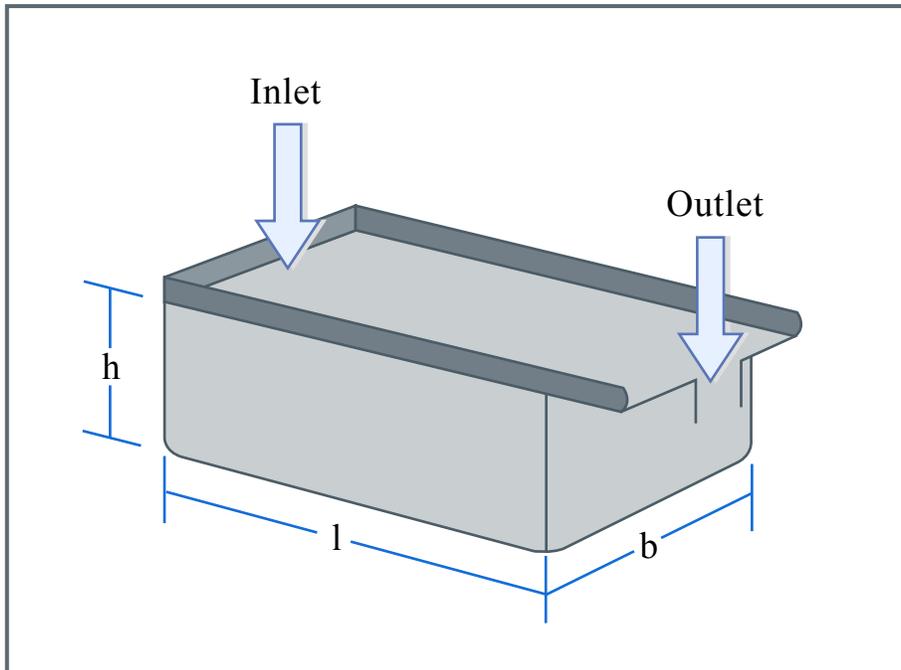


Figure by MIT OCW.

$A$  = Surface area

$V$  = Volume

$Q$  = Throughput – independent of height & proportional to area

$V_{\text{lim}}$  = Sedimentation velocity

$T$  = Time

$$\left. \begin{array}{l} t = \frac{V}{Q} = \frac{bhl}{Q} \\ t = \frac{h}{g_{\text{lim}}} \\ A = bl \end{array} \right\} \Rightarrow Q = g_{\text{lim}} A$$

# Comparison of Sedimentation in a Tank and Centrifuge

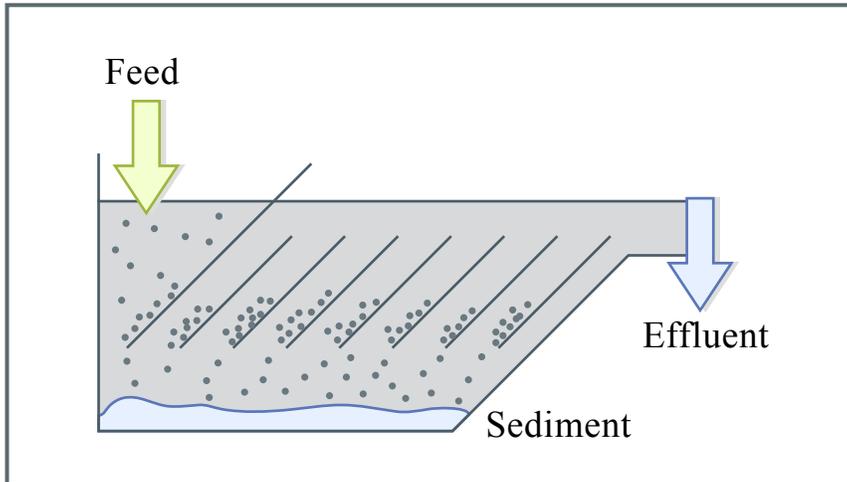


Figure by MIT OCW.

Increase **AREA**  
to increase **Q**

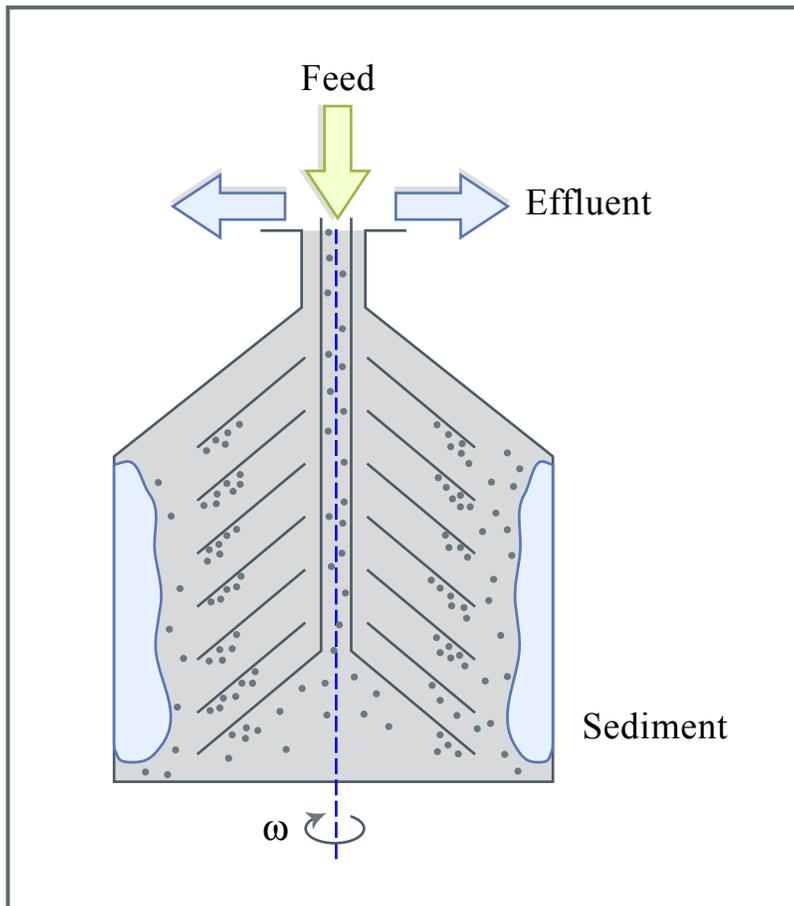


Figure by MIT OCW.

# Centrifugal Coefficient & Stoke's Law

$$C = \frac{r \cdot \omega^2}{g} \approx \frac{D \cdot n^2}{1800}$$

$$V = \frac{d^2 (S - S_1) g}{18 \eta}$$

- C = centrifugal coefficient**
- R – radius of rotor**
- W = angular velocity**
- D = rotor diameter**
- N = rotor speed**
- V = settling rate**
- D = particle diameter**
- S = particle density**
- S1 = medium density**
- N = medium viscosity**
- g = gravitational constant**

# Sedimentation Velocity

$$Q = V_{\text{lim}} A$$

Tank  $v_{\text{lim}} = \frac{d_{\text{lim}}^2 \Delta \rho g}{18 \mu}$

Disc-Stack Separator

$$v_{\text{lim}} = \frac{d_{\text{lim}}^2 \Delta \rho}{18 \mu} r \omega^2$$

What is different?

$$r \omega^2$$

# AREA

$$Q = V_{\text{lim}} A$$

$$dA = N 2\pi r (\cot a) dr$$

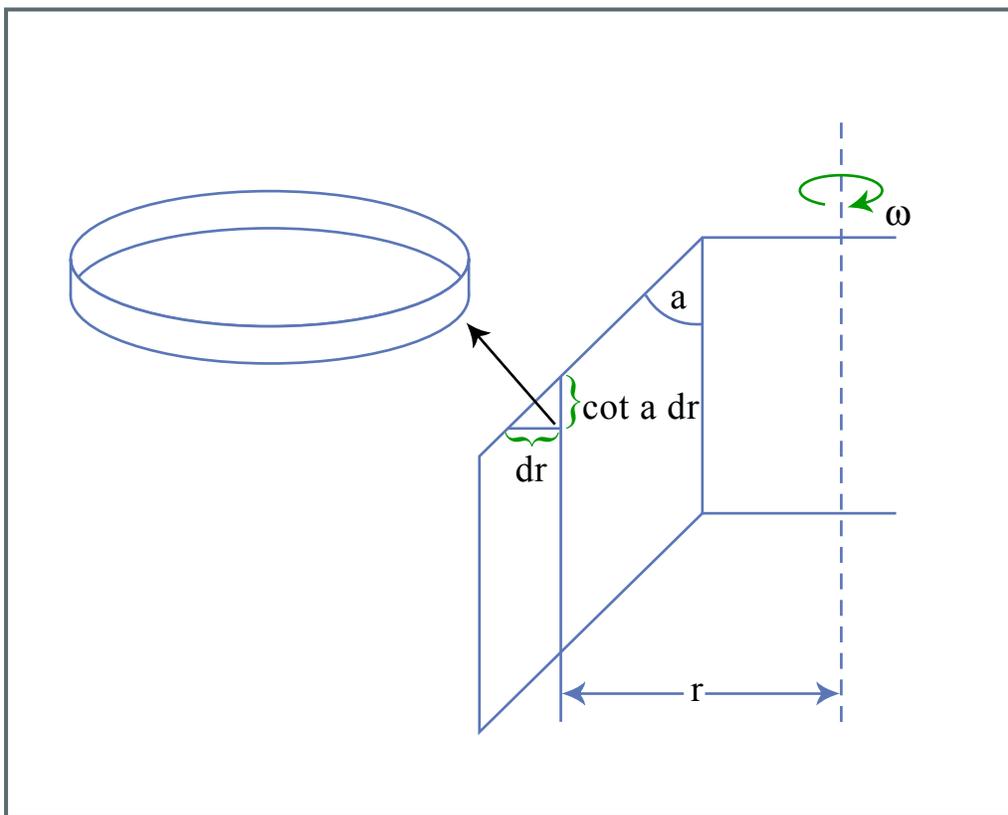


Figure by MIT OCW.

**The area of interest is the projected area perpendicular to the centrifugal force**

# THROUGHPUT Q

$$Q = V_{\text{lim}} A$$

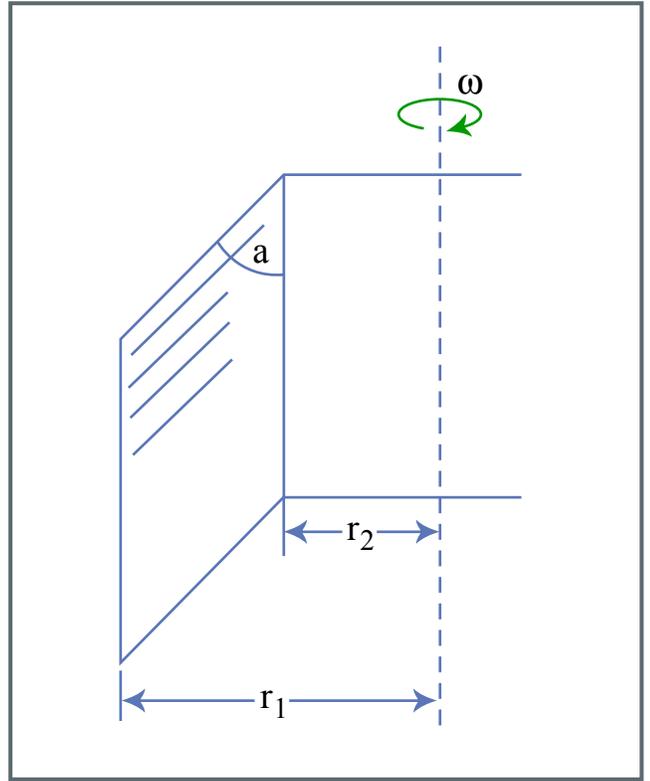


Figure by MIT OCW.

$$Q = \int_{r_2}^{r_1} \frac{\mathcal{G}_{\text{lim}} \Delta P}{18\eta} r \omega^2 N 2\pi r \cot a \, dr$$

$\Leftrightarrow$

$$Q = \underbrace{\left[ \frac{\mathcal{G}_{\text{lim}} \Delta P}{18\eta} \right]}_1 \underbrace{\left[ \frac{2\pi}{3} \omega^2 N \cot a (r_1^2 - r_2^2) \right]}_2$$

**Process Medium**

**Separator Design**

# Area Equivalent = $\Sigma$

Throughput =  $Q =$

$$Q = \left[ \frac{g_{\text{lim}} \Delta P}{18\eta} \right] \left[ \frac{2\pi}{3} \omega^2 N \cot a (r_1^2 - r_2^2) \right]$$
$$Q = \underbrace{\left[ \frac{g_{\text{lim}} \Delta P}{18\eta} g \right]}_1 \underbrace{\left[ \frac{2\pi}{3g} \omega^2 N \cot a (r_1^2 - r_2^2) \right]}_2$$

Note the  
gravitational  
force  
constant

Sedimentation  
velocity for a  
particle

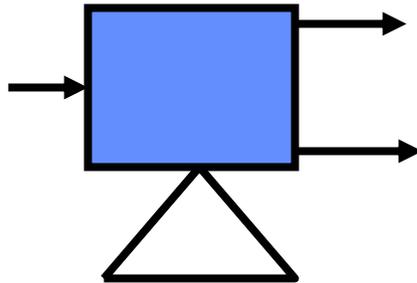
$\Sigma =$  surface area  
required for  
sedimentation in a  
tank to achieve same  
result as centrifuge

$$\frac{Q_2}{Q_1} = \frac{\Sigma_2}{\Sigma_1} \quad \Rightarrow \quad Q_2 = Q_1 \frac{\Sigma_2}{\Sigma_1}$$

# Process Objectives

## CONCENTRATION

Solid product in feed

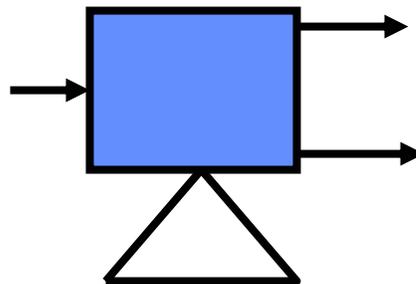


Light phase – any solids are lost product

Heavy phase – any liquid is an impurity

## CLARIFICATION

Dissolved product in feed



Light phase – solids are impurities

Heavy phase – any liquid is lost product

