

Introduction to Marine Radiochemistry

1. Isotopes and radioactive decay
2. Mathematical description of radioactive decay
3. Decay of a parent isotope to a stable daughter

Example: radiocarbon dating

4. Decay series

Math

U, Th series in oceanography

Examples : Th isotopes

Atoms and Chemical Elements

Atom: a nucleus surrounded by electrons:

Atomic radius $\sim 10^{-8}$ cm

Nuclear radius $\sim 10^{-12}$ cm

Nuclear density $\sim 10^{14}$ g/cm³ !

The nucleus consists primarily of

positively charged **protons**

electrically neutral **neutrons**

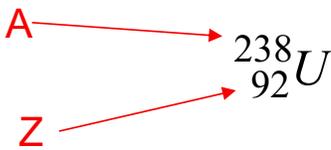
A **chemical element** is characterized by a specific number of protons in its nucleus; different **isotopes** of an element contain different numbers of neutrons

Notation

Z = atomic number (= number of protons in nucleus)

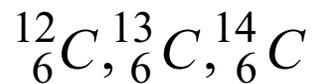
N = neutron number

A = Z + N = mass number



(the "92" is redundant with "U" and is usually omitted)

Or, an element with several isotopes:



Holden, N. E., and F. W. Walker. *Chart of the Nuclides*. 11th ed. Schenectady, NY: General Electric Co., 1972.
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Chart of the nuclides: expanded view

Holden, N. E., and F. W. Walker. *Chart of the Nuclides*. 11th ed. Schenectady, NY: General Electric Co., 1972.

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The unstable nuclides -- “radionuclides”

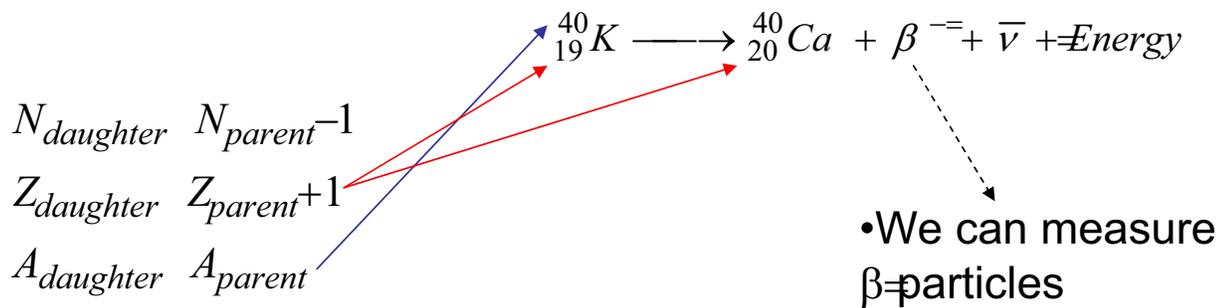
If so many nuclides are unstable, why are they around?

1. Formed during initial nucleosynthesis, but decay very slowly: e.g., ^{238}U , ^{235}U , ^{232}Th
2. Formed by decay of slowly-decaying parent isotope
3. Formed by a naturally occurring process, e.g., cosmogenic isotopes: ^{14}C
4. Anthropogenic: e.g. nuclear bomb testing and nuclear energy production, e.g., Pu isotopes, ^3H , ^{137}Cs ,...

Example : β^- Decay

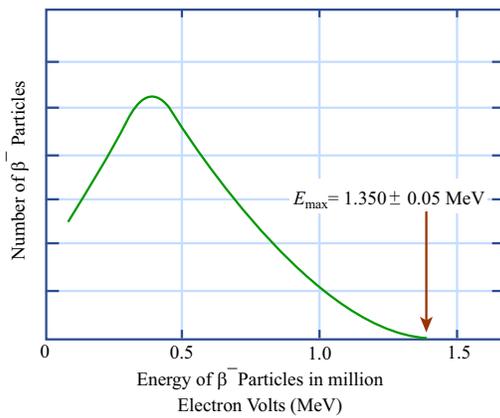
Neutron \longrightarrow proton + electron

For example,



The energy emitted is always the same for a given transition; the energy of the β particle varies up to a maximum. When $E_{\beta} < E_{\max}$, a neutrino is emitted (ν)

Distribution of β energies:



Energy spectrum of beta particles emitted by $^{40}_{19}\text{K}$. Note that most of the beta particles are emitted with energies that are about one-third of the maximum or end point energy. During each beta decay, a neutrino is emitted with a kinetic energy equal to the difference between the maximum energy and the kinetic energy of the associated beta particle.

Figure by MIT OCW.

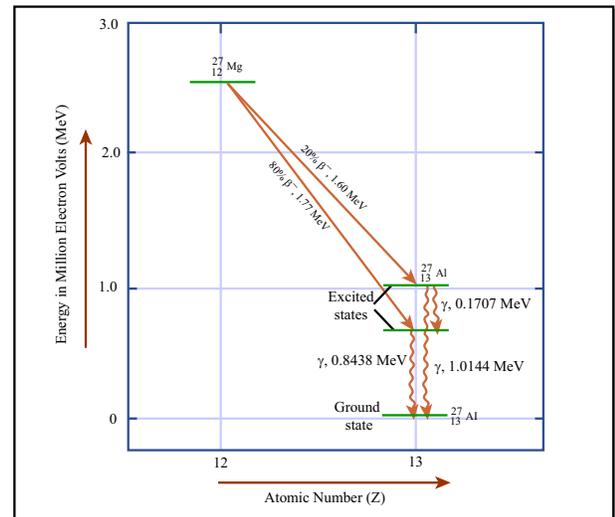


Figure by MIT OCW.

Example : α -decay

Decay by emission of a ${}^4\text{He}$ nucleus...

$${}_{90}^{228}\text{Th} \longrightarrow {}_{88}^{224}\text{Ra} + \alpha + \text{Energy}$$

$$\text{Energy} = \frac{1}{2} M_{\alpha} v_{\alpha}^2 \left(1 + \frac{M_{\alpha}}{M_p} \right)$$

Kinetic energy of α -particle
"recoil" energy

$$N_{\text{daughter}} = N_{\text{parent}} - 2$$

$$Z_{\text{daughter}} = Z_{\text{parent}} - 2$$

$$A_{\text{daughter}} = A_{\text{parent}} - 4$$

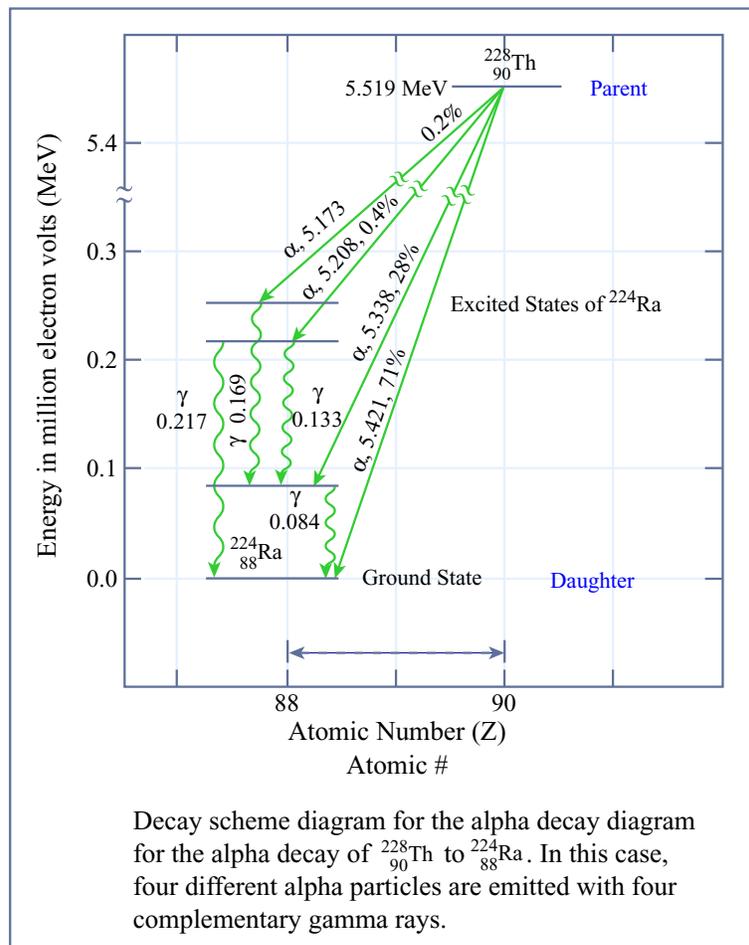


Figure by MIT OCW.

MATHEMATICAL DESCRIPTION OF RADIOACTIVE DECAY

- The **decay rate** of a radionuclide is proportional to the number of atoms of the radionuclide present
- The proportionality constant is the **decay constant**, a property of the particular radionuclide — for practical purposes, independent of T , P , ...

So:

The rate law is

$$\frac{dN}{dt} = -\lambda N$$

↘ decay constant

Often measured: decay rate

∴ Commonly used unit is the

$$\text{activity} = \lambda N$$

e.g. in "dpm" = disintegrations
per minute

ACTIVITY AND CONCENTRATION

Example 1:

Say: Conc. of $^{230}\text{Th} = 1 \times 10^{-12}$ moles/l

Then:

$$\lambda_{^{230}\text{Th}} = 1.75 \times 10^{-11} \text{ min}^{-1}$$

$$A = 1 \times 10^{-12} \frac{\text{mol}}{\text{l}} \times 6.023 \times 10^{23} \frac{\text{atoms}}{\text{mol}} \times 1.75 \times 10^{-11} \text{ min}^{-1}$$

$$= \underline{\underline{10.56 \text{ dpm}}}$$

Example 2:

Suppose: A sediment has $2 \frac{\text{dpm}}{\text{gram}}$ of both ^{238}U and ^{234}Th

$$\lambda_{^{238}\text{U}} = 2.92 \times 10^{-16} \text{ min}^{-1}$$

$$\lambda_{^{234}\text{Th}} = 2.0 \times 10^{-5} \text{ min}^{-1}$$

\Rightarrow Concentrations :

$$^{238}\text{U}: 2 \frac{\text{dpm}}{\text{gram}} \times \frac{1}{2.92 \times 10^{-16} \text{ min}^{-1}} = 6.8 \times 10^{15} \frac{\text{atoms}}{\text{gram}}$$

$$^{234}\text{Th}: 2 \frac{\text{dpm}}{\text{gram}} \times \frac{1}{2.0 \times 10^{-5} \text{ min}^{-1}} = 1 \times 10^5 \frac{\text{atoms}}{\text{gram}}$$

COMMONLY USED DEFINITIONS

Using the rate law,

$$\left. \begin{array}{l} \frac{dN}{dt} = -\lambda N \\ \text{with } N(t=0) = N_0 \end{array} \right\}$$

$$\Rightarrow \boxed{N = N_0 e^{-\lambda t}} = \text{Amount of radionuclid present vs. time}$$

① HALF LIFE ($t_{1/2}$)

- The time it takes for 50% of the atoms present to decay

$$0.5 N_0 = N_0 e^{-\lambda t_{1/2}}$$

$$\rightarrow \ln(0.5) = -\lambda t_{1/2}$$

$$\text{OR } t_{1/2} = \frac{\ln 2}{\lambda} \approx \frac{0.693}{\lambda}$$

Example:

$${}^{238}\text{U} : t_{1/2} = \frac{\ln 2}{2.92 \times 10^{-16} \text{ min}^{-1}} = 4.51 \times 10^9 \text{ years}$$

$${}^{234}\text{Th} : t_{1/2} = \frac{\ln 2}{2 \times 10^{-5} \text{ min}^{-1}} = 24.1 \text{ days}$$

② MEAN LIFE (τ)

- The average lifetime of an atom...

$$\tau = - \frac{1}{N_0} \int_0^{N_0} t dN \quad (1)$$

From the rate law,

$$\frac{dN}{dt} = -\lambda N \Rightarrow dN = -\lambda N dt$$

and

$$N = N_0 \text{ at } t = 0$$

$$N = 0 \text{ at } t = \infty$$

\Rightarrow (1) can be transformed to

$$\tau = - \frac{1}{N_0} \int_{\infty}^0 -t \lambda N dt$$

$$= - \frac{1}{N_0} \int_0^{\infty} \lambda t N_0 e^{-\lambda t} dt$$

$$= - \lambda \int_0^{\infty} t e^{-\lambda t} dt$$

Solution:

$$\tau = \frac{1}{\lambda}$$

- The amount present decays to $\frac{1}{e} \cdot N_0$ during time τ
- $\tau = t_{1/2} \times \frac{1}{\ln 2} \approx 1.443 \times t_{1/2}$

ONE
~~THE~~ METHODS OF OBTAINING AGES
FROM RADIONUCLIDE MEASUREMENTS

① Measure the quantity of the nuclide present in the sample ...

- IF :
- Know the amount incorporated when the sample was formed
 - Know there have been no additions or removals (other than by decay) since formation

THEN:

USE : $N(t) = N_0 e^{-\lambda t}$

Log. of both sides \Rightarrow

$$\text{Age} = t = \frac{1}{\lambda} \ln \frac{N_0}{N}$$

Example: ^{14}C DATING

- Variations in atmosphere/ocean ^{14}C
- $t_{1/2} (^{14}\text{C}) \sim 5730$ yrs
Age limit $\sim 30,000$ yrs.

RADIOCARBON DATING CONVENTIONS

The age equation:

$$\text{Age} = \frac{1}{\lambda_{14C}} \ln \left[\frac{A_0}{A} \right]$$

① Results reported as
"fraction modern" = $\frac{A}{A_0}$

"Modern" is defined to be

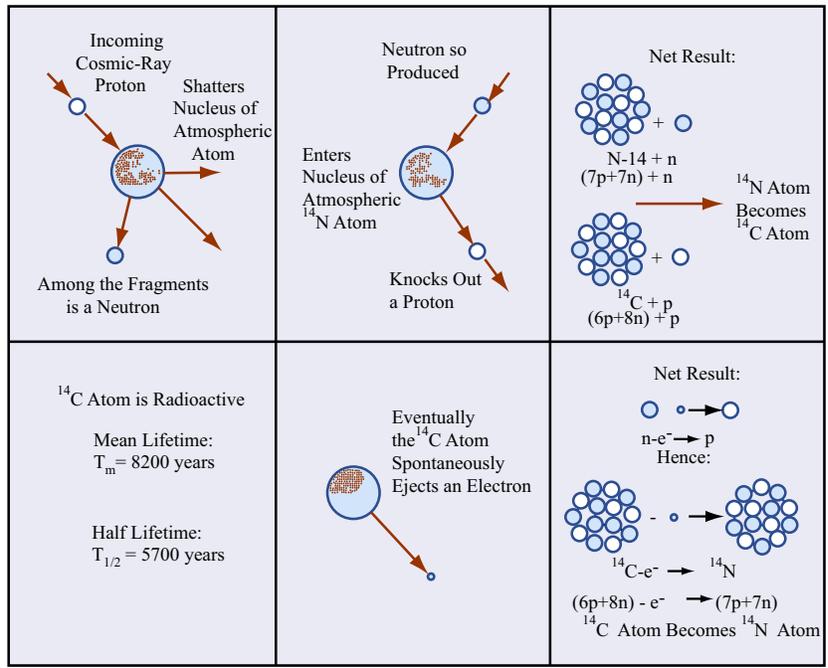
95% of the activity in 1950
of an oxalic acid standard,
after making a specified
correction for C isotope
fractionation

② "Radiocarbon Age"

$$= 8033 * \ln \left[\frac{A_0}{A} \right]$$

for historic reasons, an old
value of λ - incorrect! - is
used.

$$(3) \quad \Delta^{14}C \quad 1000 * \left(e^{-(date-1950) * \lambda_m} - 1 \right)$$



The "life cycle" of a carbon-14 atom. Created in the atmosphere by the collision of a neutron (produced by primary cosmic-ray protons) with a nitrogen atom, the average ^{14}C atom "lives" for 8200 years. Its life is terminated by the ejection of an electron with returns the atom to its original form, ^{14}N .

- ^{14}C is formed in the atmosphere.
- Rate of formation depends on cosmic ray flux
- 1/2 life = 5730 years

Figure by MIT OCW.

Since

- (1) The true A_0 is unlikely to be the same as the defined A_0
- (2) The slightly incorrect λ is used
- (3) There may be "reservoir corrections"

Calibration curves must be used to convert conventional, "radiocarbon date" to a true, calendar date.

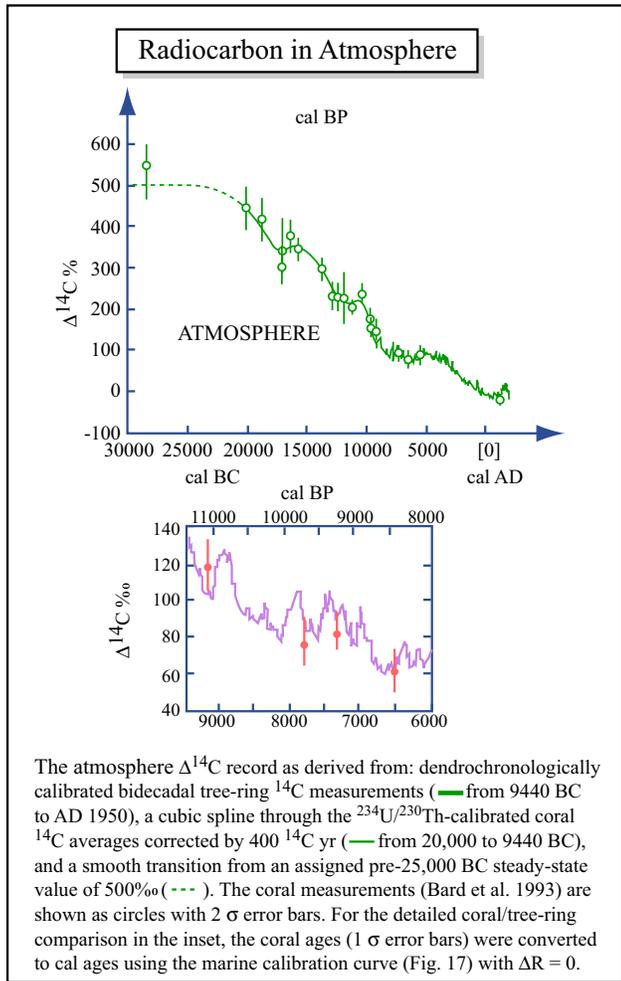


Figure by MIT OCW.

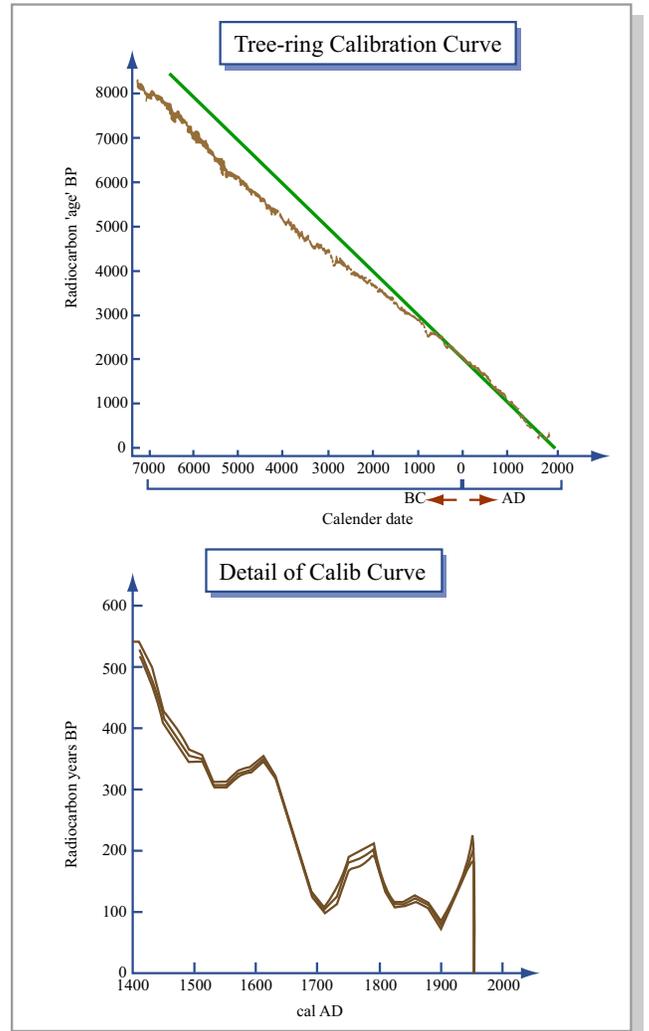


Figure by MIT OCW.

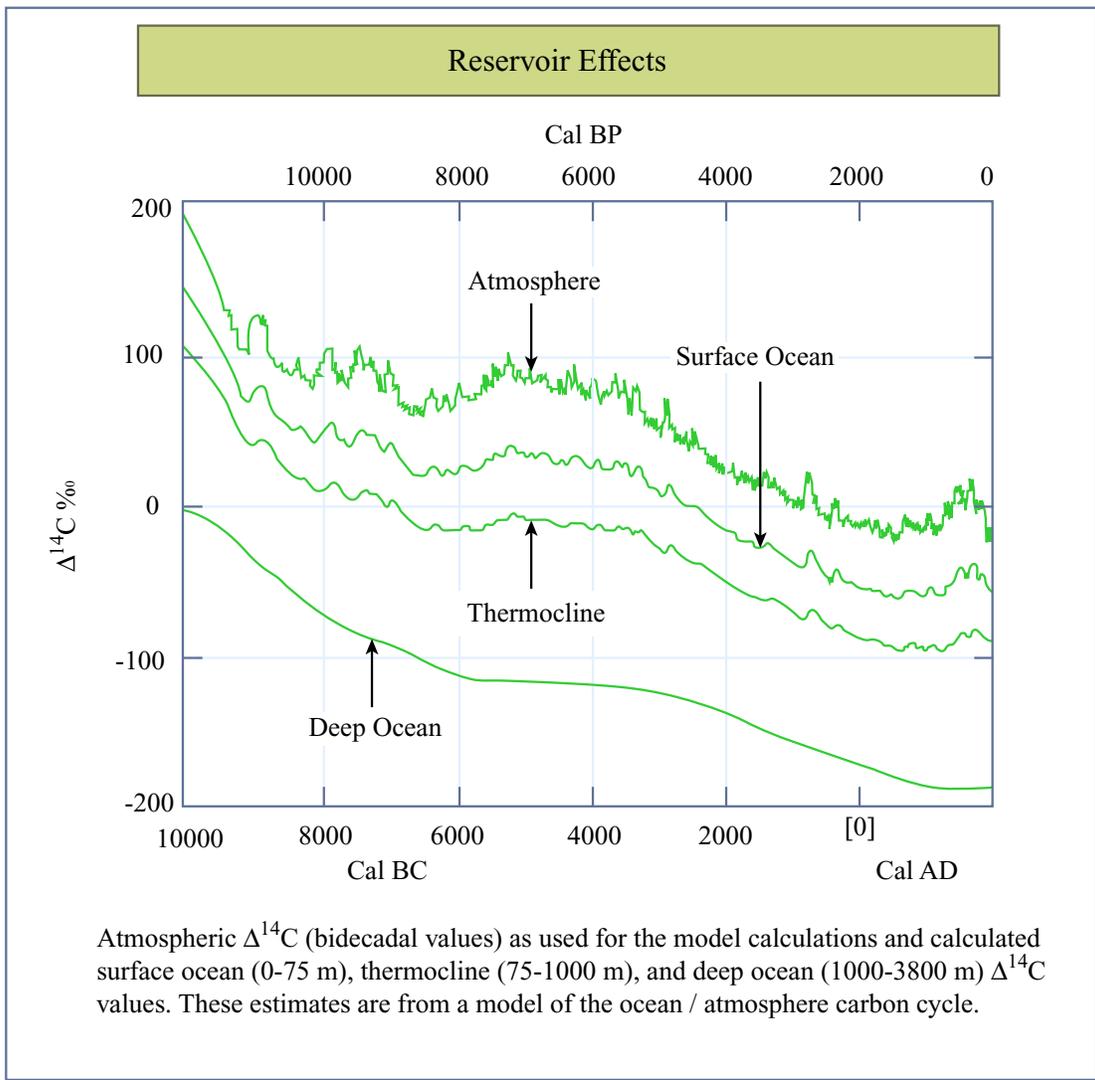
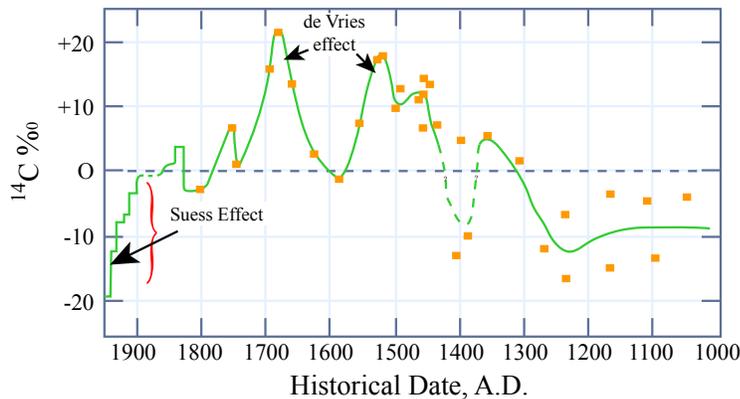


Figure by MIT OCW.

Anthropogenic Perturbations of Atmospheric ^{14}C content

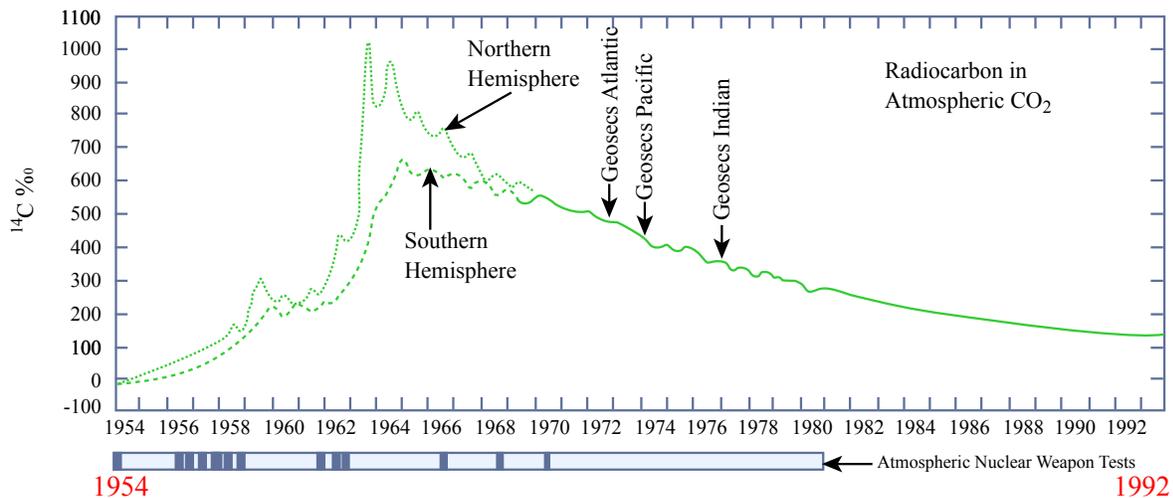
1. The Suess Effect



Deviation of the initial radiocarbon activity in per mil of wood samples of known age relative to 95 percent of the activity of the oxalic acid standard of the National Bureau of Standards. The observed activities were corrected for carbon isotope fractionation and recalculated using a value of 5730 years for the half-life of ^{14}C . The decline in the radiocarbon content starting at about 1900 results from the introduction of fossil CO_2 into the atmosphere by the combustion of fossil fuels (Suess effect). The anomalously high radiocarbon activity around 1710 and 1500 A.D. is known as the "de Vries effect." Its causes are not understood.

Figure by MIT OCW.

2. Bomb Testing



Observed time history for the $^{14}\text{C}/\text{C}$ ratio in ground level air. Before 1970, a clear difference can be seen between the northern and southern hemispheres, and also a clear seasonality appears in both records. These features are related to injections of bomb ^{14}C from stratosphere to troposphere (mainly in the northern hemisphere). Times and magnitudes of the atmospheric weapons tests are shown. Although the test ban treaty was implemented at the beginning of 1963, several small Chinese and French atmospheric tests were conducted after this time.

Figure by MIT OCW.

Abundances, Half-Lives, and Decay Constants of the Principle Naturally Occurring Isotopes of Uranium and Thorium				
Isotope	Abundance %	Half-Life y	Decay Constant y^{-1}	Reference
^{238}U	99.2739	4.510×10^9	1.537×10^{-10}	1
		4.468×10^9	1.55125×10^{-10}	2
^{235}U	0.7204	0.7129×10^9	9.722×10^{-10}	3
		0.7038×10^9	9.8485×10^{-10}	2
^{234}U	0.0057	2.48×10^9	2.806×10^{-6}	4
^{232}Th	100	13.890×10^9	4.990×10^{-11}	5
		14.008×10^9	4.948×10^{-11}	6

1. Kovarik and Adams (1955)
2. Jaffey et al. (1971)
3. Fleming et al. (1952)
4. Strominger et al. (1958)
5. Picciotto and Wilgain (1956)
6. LeRoux and Glendenin (1963)

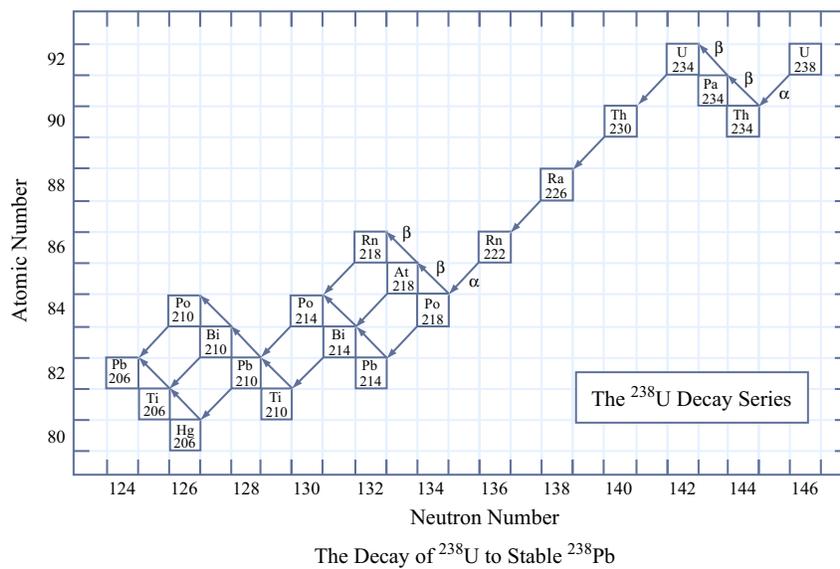


Figure by MIT OCW.

DESCRIBING DECAY IN A
DECAY SERIES



Parent, N_1

$$1) \left. \begin{aligned} \frac{dN_1}{dt} &= -\lambda_1 N_1 \\ N_1(t=0) &= N_1^0 \end{aligned} \right\} N_1 = N_1^0 e^{-\lambda_1 t}$$

Daughter, N_2

$$2) \left. \begin{aligned} \frac{dN_2}{dt} &= \lambda_1 N_1 - \lambda_2 N_2 \\ &= \lambda_1 N_1^0 e^{-\lambda_1 t} - \lambda_2 N_2 \\ N_2(t=0) &= N_2^0 \end{aligned} \right\}$$

$$\Rightarrow N_2 = N_2^0 e^{-\lambda_2 t} + \frac{\lambda_1 N_1^0}{\lambda_2 - \lambda_1} (e^{-\lambda_1 t} - e^{-\lambda_2 t})$$

What if: Longer-lived parent decays to shorter-lived daughters, i.e., $\lambda_2 \gg \lambda_1$?

THEN: a) $e^{-\lambda_2 t} \ll e^{-\lambda_1 t}$
b) $\lambda_1 \ll \lambda_2$

$$\Rightarrow N_2 = N_2^0 e^{-\lambda_2 t} + \frac{\lambda_1 N_1^0}{\lambda_2} e^{-\lambda_1 t}$$

DECAY IN A DECAY SERIES: $\lambda_2 \gg \lambda_1$

$$N_2 = N_2^0 e^{-\lambda_2 t} + \frac{\lambda_1 N_1^0}{\lambda_2} e^{-\lambda_1 t}$$

$N_2^0 = 0$

After several N_2 half-lives,
i.e., $t \gg \frac{1}{\lambda_2} \dots$

• 1st term $\rightarrow 0$

• $\lambda_1 N_1^0 e^{-\lambda_1 t} = A_1 = \lambda_1 N_1$

\Rightarrow

$$\lambda_2 N_2 = \lambda_1 N_1$$

EQUAL DECAY RATES

"

EQUAL ACTIVITIES

"

"SECULAR EQUILIBRIUM"

• Reached after a few $\frac{1}{2}$ -lives of the shorter-lived daughter. **IN A CLOSED SYSTEM**

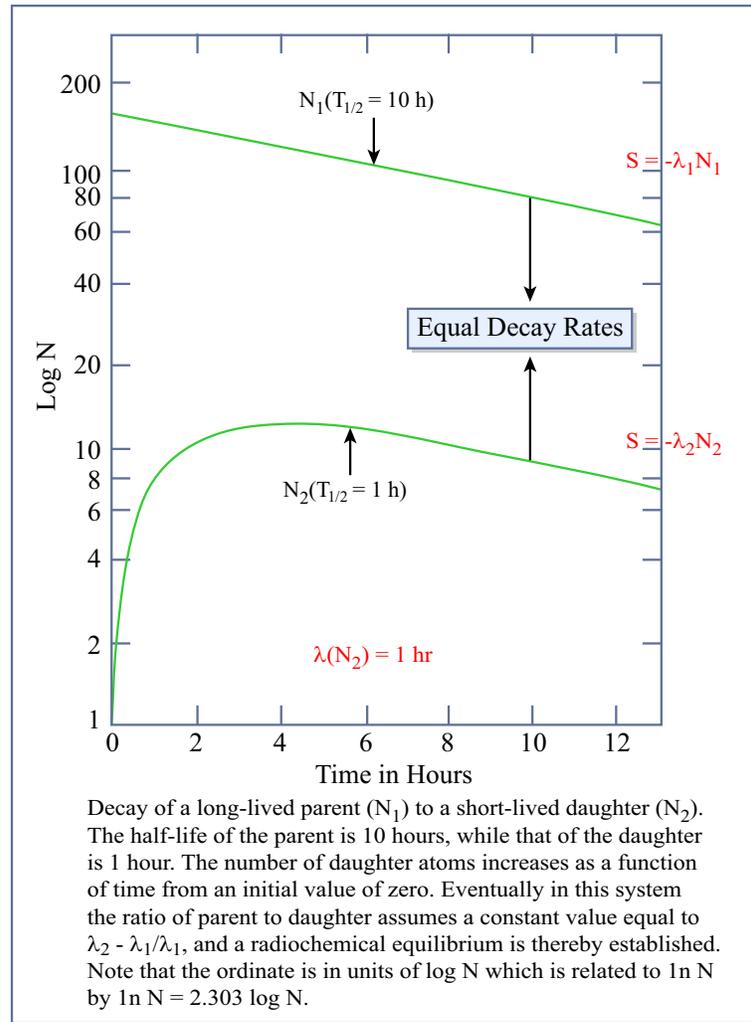


Figure by MIT OCW.

Decay Series Chemical Properties and the Potential for Radioactive Disequilibrium in the Oceans

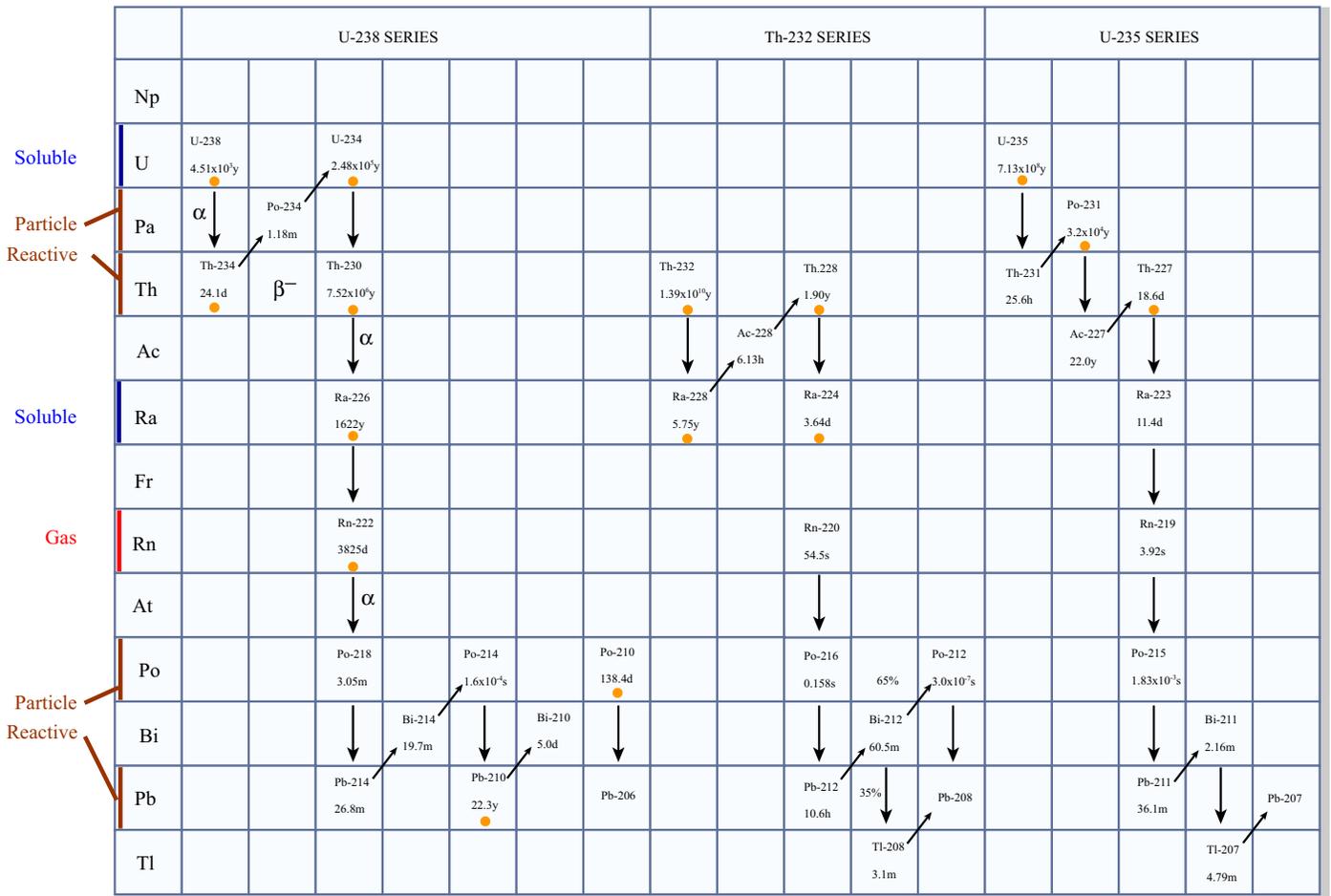
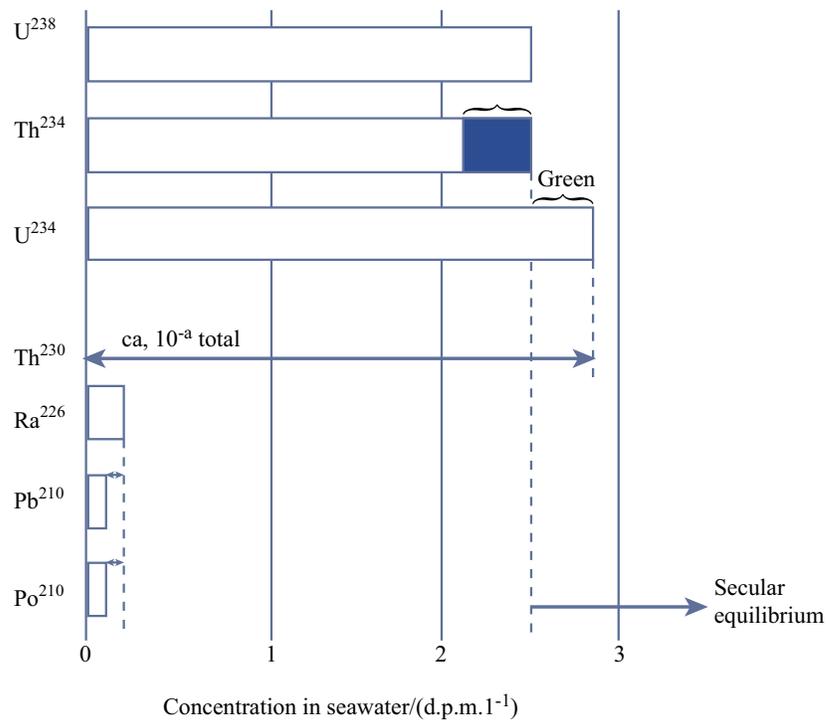


Figure by MIT OCW.

The U^{238} Series in Seawater



Concentrations of the longer-lived members of the U^{238} decay series in seawater arranged in descending order within the series. The values chosen are representative of deep ocean water. Somewhat different relationships are found in the surface waters. Shaded areas represent the suspended particulate fraction. Deficiencies of Th^{230} and Pb^{210} relative to their parent nuclides result from scavenging. A Th^{234} deficiency is not found because of the short half-life, but a significant uptake by the suspended particles is evident.

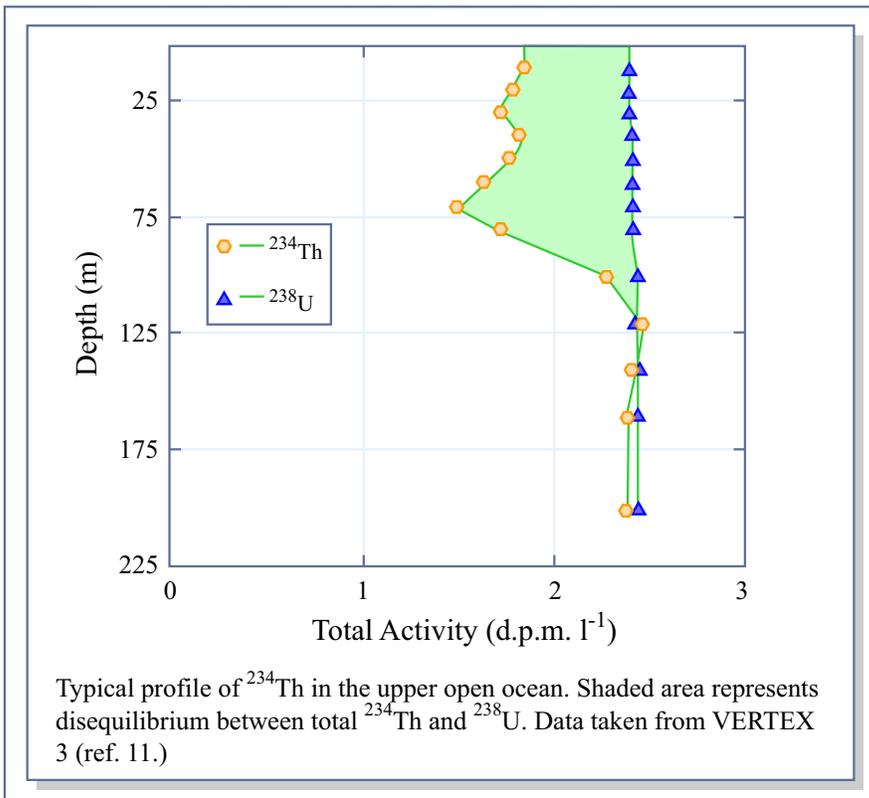
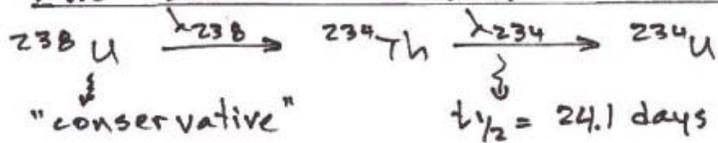
Figure by MIT OCW.

USES OF ^{238}U SERIES DISEQUILIBRIUM
IN THE OCEANS
(a few examples)

<u>Disequilibrium between</u>	<u>in</u>	<u>USE</u>
$^{234}\text{Th}/^{238}\text{U}$ $^{230}\text{Th}/^{234}\text{U}$ $^{210}\text{Pb}/^{226}\text{Ra}$	water column	scavenging rates
$^{222}\text{Rn}/^{226}\text{Ra}$	surface ocean sediments	gas exchange solute transport
$^{230}\text{Th}/^{234}\text{U}$ $^{234}\text{Th}/^{238}\text{U}$ $^{210}\text{Pb}/^{226}\text{Ra}$	sediments	sed accumulation + mixing rates

(... and more ...)

EXAMPLE: Removal of particle-reactive elements from the surface ocean.

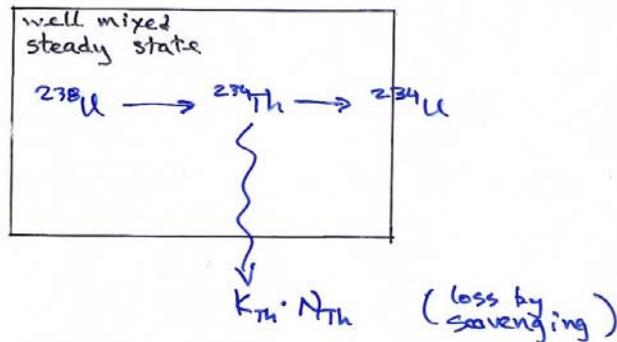


$A_{234} < A_{238}$: removal on time scale of ~ a few $t_{1/2}$ lives of ${}^{234}\text{Th}$

$A_{234} \approx A_{238}$
 slower removal (or no removal)

Figure by MIT OCW.

Box model for surface ocean ^{234}Th



Mass balance for ^{234}Th

Production by decay of ^{238}U	=	Loss by decay of ^{234}Th	+	Loss by scavenging
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$$(1) \lambda_{238} N_{238} = \lambda_{234} N_{234} + k_{234} N_{234}$$

Define: $\frac{1}{k_{\text{TH}}} = \tau_{\text{scav}} =$ "residence time of ^{234}Th with respect to scavenging"

$$(1) \rightarrow (2) A_{238} = A_{234} + \frac{1}{\tau_{\text{scav}}} N_{234}$$

$$\rightarrow (3) \lambda_{234} A_{238} = \lambda_{234} A_{234} + \frac{1}{\tau_{\text{scav}}} A_{234}$$

\therefore (rearrange)

$$\Rightarrow \tau_{\text{scav}} = \left[\frac{1}{\lambda_{234}} \right] \left(\frac{A_{234}/A_{238}}{1 - A_{234}/A_{238}} \right)$$

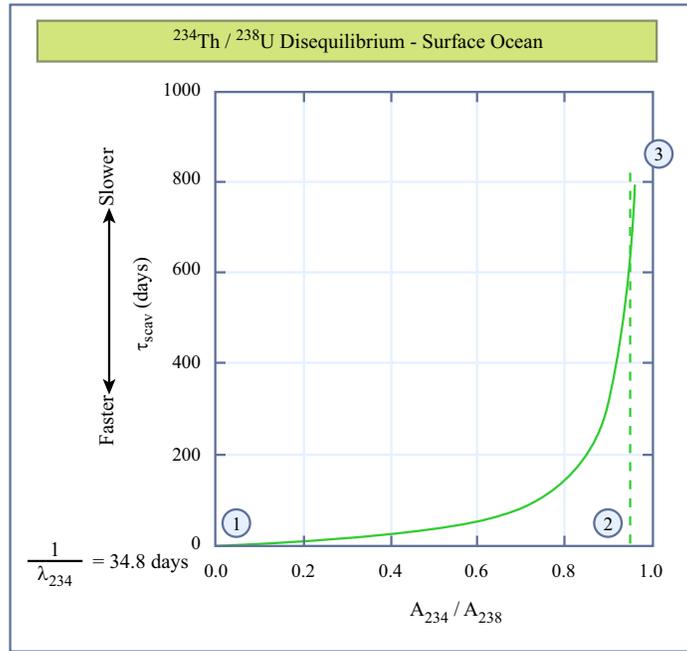


Figure by MIT OCW.

Plot for the scavenging model:

$$\tau_{\text{scav}} = \frac{1}{\lambda_{234}} \left[\frac{A_{234}/A_{238}}{1 - A_{234}/A_{238}} \right]$$

- ① $A_{234}/A_{238} \rightarrow 0$: the greater the ^{234}Th deficit, the faster the scavenging
- ② if can measure ratio to $\sim 5\%$, slowest scavenging you can measure is $\tau_{\text{scav}} \sim 600 \text{ days}$
- ③ $A_{234}/A_{238} \rightarrow 1$: the smaller the deficit, the slower the scavenging

How to quantify scavenging
in the deep ocean, where

$$A_{234\text{Th}} = A_{238\text{U}} ?$$

Use:



$$\left\{ \begin{array}{l} ^{234}\text{U} : \text{conservative, } t_{1/2} = 245,000 \text{ yr} \\ ^{230}\text{Th} : \text{particle reactive, } t_{1/2} = 75,200 \text{ yr} \end{array} \right.$$

Apply the same model :

$$\tau_{\text{scav}} = \frac{1}{\lambda_{230}} \left[\frac{A_{230}/A_{234}}{1 - A_{230}/A_{234}} \right]$$

$$\frac{1}{\lambda_{230}} = 108 \text{ ky}$$

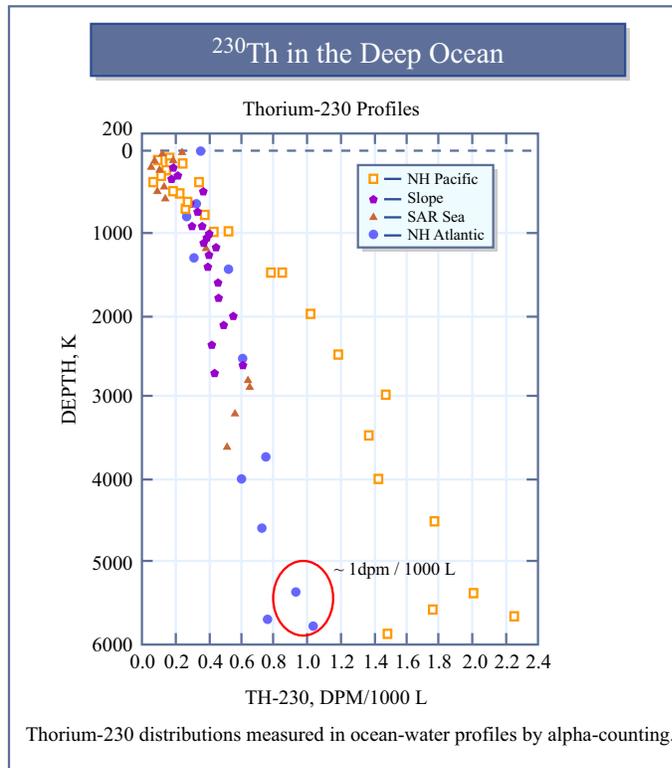


Figure by MIT OCW.

Note: $A_{^{234}\text{U}} \sim 1.14 \times A_{^{238}\text{U}} \approx 2.7 \text{ dpm/l}$

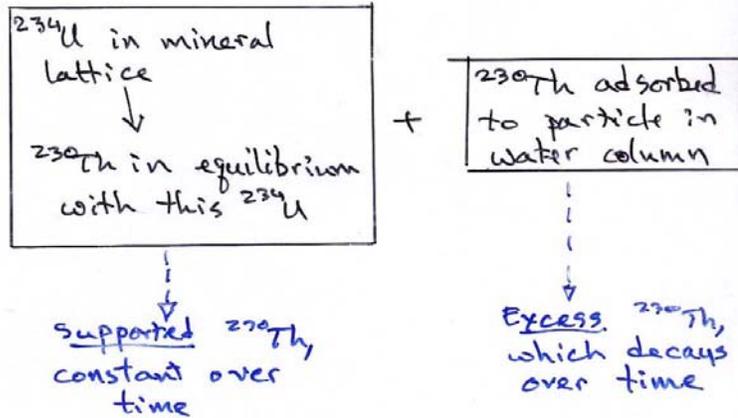
$$\tau_{\text{scav}} = 108,000 \left[\frac{.001/2.7}{1 - .001/2.7} \right]$$

$$= 40 \text{ years}$$

The ^{230}Th is nearly all removed from the water column ...

it must fall with particles to the sediments.

A particle reaching the sediment surface contains:



SUPPOSE:

- ① Sediment accumulates at a constant rate, S

Then: depth in sediments is related to time:

$$Z = t \cdot S \Rightarrow t = \frac{Z}{S}$$

- ② Sedimenting particles carry a constant flux of ^{230}Th

- We know:

Excess ^{230}Th decays by

$$A(t) = A(t=0) e^{-\lambda t}$$

- Convert from time to depth, in segs.

$$A(t) \rightarrow A(z)$$

$$A(t=0) \rightarrow A(z=0) \quad [\text{constant flux} \Rightarrow \text{constant } A_0]$$

$$\lambda t \rightarrow \lambda z/s$$

- So:

In a steadily accumulating sediment with constant S (and no mixing of sediments)

$$A(z) = A(z=0) e^{-\lambda z/s}$$

↓
Excess ^{230}Th

IDEALIZED ^{230}Th PROFILE IN SEDIMENT

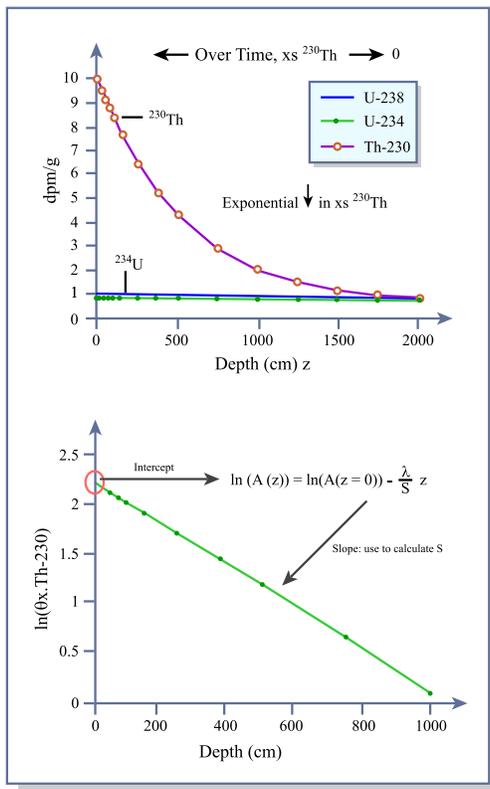


Figure by MIT OCW.

A real example: rapidly accumulating
sediments near Antarctica

(DeMaster et al. 1991, Mar. Chem. 35, 489-502)

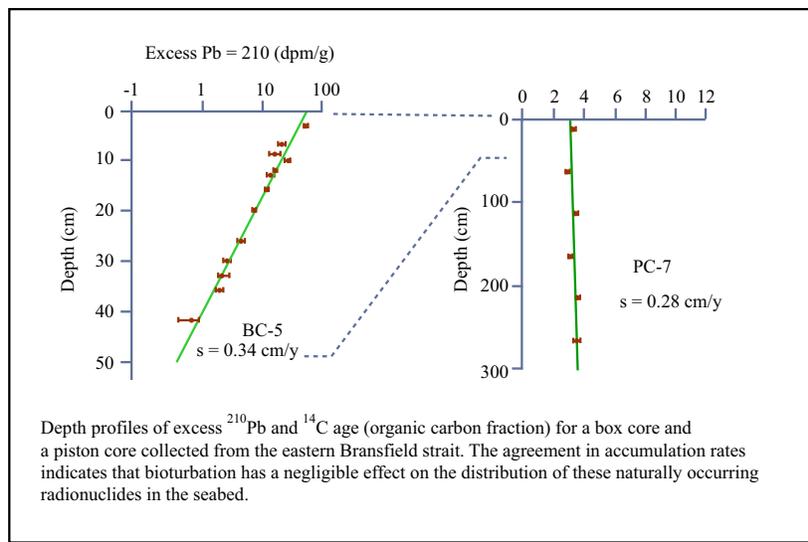


Figure by MIT OCW.

Note:

Different time scales of measurement:

- Excess ^{210}Pb ($= A_{210\text{Pb}} - A_{226\text{Ra}}$)

$$t_{1/2} \approx 22 \text{ yrs}$$

- ^{14}C $t_{1/2} \approx 5730 \text{ yrs}$