

**Problem Set 6**  
**Marine Chemistry 12.742**

**Problem 1:**

A suite of biological and geochemical constraints can be used to estimate the major terms for the upper ocean carbon budget. Shown below is a figure from Brix et al. (2004) based on data from the Hawaii Ocean Time-series (HOT) in the subtropical North Pacific.

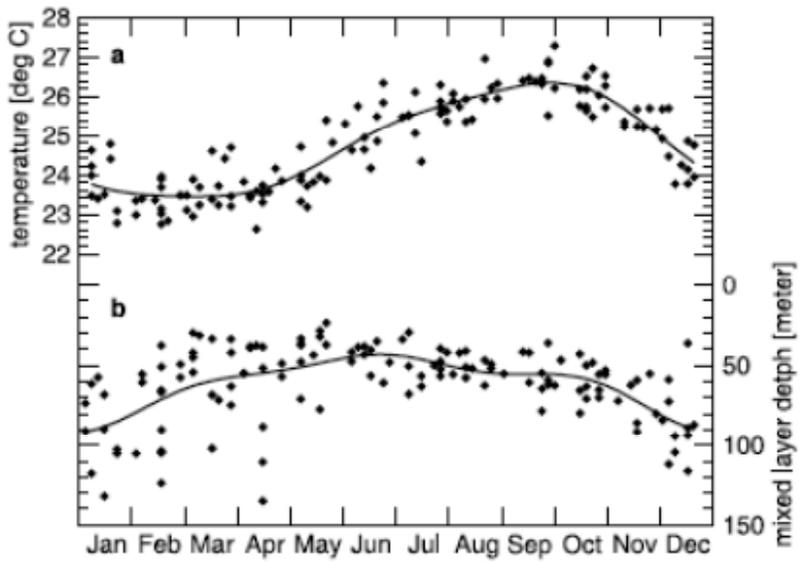
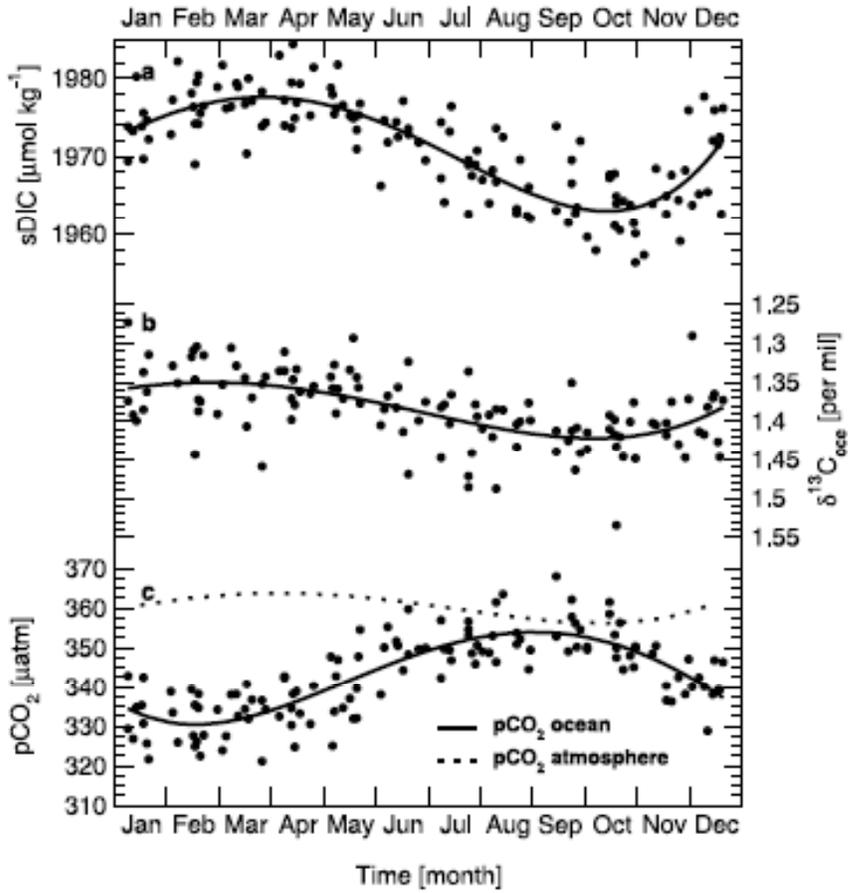
For the calculations below, assume the following:

$$\frac{1}{pCO_2} \frac{\partial pCO_2}{\partial T} = 4\% / K$$

$$\text{-Revelle factor } \frac{\partial pCO_2}{pCO_2} \frac{DIC}{\partial DIC} = 10$$

-<sup>13</sup>C of DIC is zero and a biological kinetic isotopic fractionation of -23 per mille

- (1) Describe the major physical and biological processes controlling the seasonal cycle of mixed layer salinity normalized DIC, pCO<sub>2</sub>, and <sup>13</sup>DIC using mass balance equations and simple sketches.
- (2) Estimate quantitatively the partitioning between physical and biological impacts on the seasonal cycle of pCO<sub>2</sub>.
- (3) Estimate the air-sea flux of CO<sub>2</sub> (atmosphere pCO<sub>2</sub> is dashed line in pCO<sub>2</sub> panel below) given a <sup>222</sup>Rn based piston velocity estimate of 3.4 m/day, Sc (<sup>222</sup>Rn)=2000, and Sc (CO<sub>2</sub>) = 660.
- (4) Estimate the Net Community Production assuming a purely local balance and neglecting physical transport.
- (5) Describe how could you use the <sup>13</sup>C to improve your NCP estimate in the presence of horizontal advection. Assume you knew the lateral gradients in salinity normalized DIC (-20 umol/kg/1000 km) and del<sup>13</sup>C (0) but not the advection speed.



### Question 2

On a cruise in the North Atlantic gyre off western Africa, you measured dissolved  $^{234}\text{Th}$  ( $\lambda_{234} = 0.029 \text{ d}^{-1}$ ) in the upper 200m of the water column and the  $C_{\text{org}}/^{234}\text{Th}$  ratio in settling particles collected with a floating sediment trap deployed just below the mixed layer. You also measured “new” production in a few samples within the mixed layer using incubations with  $^{15}\text{N}$ -labeled nitrate.

- Estimate the particle export time-scale given a mean  $^{234}\text{Th}$  activity in the upper 100m =  $1800 \text{ dpm/m}^3$  and no deficit below that depth (100-200m) (the activity of  $^{238}\text{U}$  in seawater is  $2480 \text{ dpm/m}^3$ ).
- Calculate a carbon export flux given that the material collected in the trap has a  $C_{\text{org}}/^{234}\text{Th}$  ratio =  $4 \mu\text{mol C/dpm}$ . [Hint: The vertically integrated mass budget for  $^{234}\text{Th}$  gives the removal flux of  $^{234}\text{Th}$  on to particles, in  $\text{atoms/m}^2/\text{time}$ , which should balance the material caught in the trap].
- The results from the nitrate incubation indicate a mean nitrate uptake rate of  $0.3 \text{ mmolN/m}^2/\text{d}$ . Are these results consistent with the Th based export estimates? What other physical and biogeochemical processes could lead to a disconnect between the C based and N based estimates of net cycling through the

### Question 3

Imagine a hypothetical ocean with a homogeneous euphotic zone occupied by only one species of phytoplankton producing uniform spherical cells with a radius of  $2\mu\text{m}$ . There are no seasonal variations, no predators and no bacteria so that the intact cells sink on their own from the euphotic zone. A sediment trap with an aperture of  $0.5 \text{ m}^2$  is deployed for one year just below the euphotic zone and captures  $91.25\text{g}$  of material. Assume particles sink following Stoke's Law:

$$w = \sqrt{(16 r g (\rho_s - \rho_w) / 3 \rho_w \mu)}$$

where  $\rho_s$  is the density of the particle;  $\rho_w$  is the density of water;  $g$  is the gravitational constant ( $9.81 \text{ m/s}^2$ ),  $\mu$  is the viscosity of water ( $10^{-2} \text{ g/(cm s)}$ ),  $r$  is the radius of the spherical particles, and  $w$  is the terminal velocity. Take the density of water as  $1\text{g/cm}^3$  and that of the particles (individual and colonies) as  $2\text{g/cm}^3$ .

- Suppose that during that year, you filter  $1 \text{ m}^3$  of seawater from the euphotic zone. How much material (in grams) do you expect to collect on the filter?
- How many cells do you expect to collect on the filter?

The following year, everything stays the same but 95% of the cells start to aggregate and produce spherical colonies with a radius of  $50\mu\text{m}$ , which also sink unaltered from the euphotic zone by gravitational settling.

- By how much would the suspended matter concentration in the euphotic zone decrease compared to the previous year?

d) How many individual cells and how many colonies would you find in 1 cubic meter of water from the euphotic zone?