

Climate Physics and Chemistry

Ocean and Climate: Problem Set

(C. Wunsch)

Corrected Problem 2.

1. The pressure field at depth $z = 1000\text{m}$ in the ocean is found to follow the rule,

$$p = p_0 \cos(\pi x/10^4) \cos(\pi y/10^4).$$

The origin of y is taken to be 30°N and x, y are measured in meters. What are the northward and eastward components of geostrophic velocity at $x = 10^4/2$, $y = 0$? If the fluid density is approximated as uniform, $\rho = \rho_0 = 1.03 \times 10^3 \text{kg/m}^3$, how much water (mass) is moving northward between the seafloor and 1000m , between $x = 0$ and $x = 10^4/2$? For a numerical answer, let $p_0 = 238\text{N/m}^2$. (Hint: Treat the seafloor as flat, and note that the pressure gradient is independent of depth if the density is uniform.)

2. A ship measures the temperature and salinity in the ocean at $x = 0$, and $x = 50\text{km}$ at a latitude of 45°N . When converted to density, the two profiles are found to be closely approximated as,

$$\begin{aligned}\rho(x = 0, z) &= 1.03 \times 10^3 \text{kg/m}^3 (1 - z / (2 \times 10^4)), \\ \rho(x = 50\text{km}, z) &= 1.03 \times 10^3 \text{kg/m}^3 [1 - (z + 1 \times 10^{-7} z^2) / (2 \times 10^4)]\end{aligned}$$

where z is in meters. Compute and plot the northward velocity as a function of z for $0 \leq z \leq 3000\text{m}$ under the assumption that $z = -2000\text{m}$ is a level of no motion. What is different at 10°N ? Take gravity, $g = 10\text{m/s}^2$.

3. A uniform wind blows towards the northeast such that the windstress on the ocean is $\tau = \tau_0(1, 1)$. Using the equations

$$\begin{aligned}-fv &= A \frac{\partial^2 u}{\partial z^2} \\ fu &= A \frac{\partial^2 v}{\partial z^2}\end{aligned}$$

which govern the Ekman layer, find u, v as a function of z . (Hint: multiply the second equation by i and add to the first equation. Solve this equation for the complex quantity $u + iv$.)

(In Problems 1 and 2, the numerical result is less important than telling me what you are doing.)