

# 14.02 - Principles of Macroeconomics

## Problem Set 4

Spring 2023

### Question 1 - The WS-PS Model [20 Points]

Suppose the wage-setting equation is given by:

$$W = P (1 - u) z$$

where  $z$  represents unemployment insurance,  $u$  represents the unemployment rate and  $W$  represents the nominal wage. Suppose the production function is given by  $Y = N$ , where  $N$  is employment, and the price-setting equation is given by:

$$P = W (1 + m)$$

where  $m$  is the markup.

1. [6 Points] Explain how the wage-setting equation depends on the price level, the unemployment rate, and the unemployment insurance. Provide the intuition.
2. [6 Points] Explain how the price-setting equation depends on the wage and the markup  $m$ . Provide the intuition.
3. [8 Points] Express both the wage-setting equation and the price-setting equation in terms of the real wage  $W/P$ . Find algebraically the natural rate of unemployment,  $u_n$ , by equating the real wage implied by the wage-setting equation with the one implied by the price-setting equation. Does the natural rate of unemployment increase or decrease in the mark-up? Provide intuition.

## Question 2 - The Phillips Curve (30 points)

Consider the WS and PS relations in a dynamic setting where the subscript  $t$  represents the year:

$$\begin{aligned}W_t &= P_t^e F(u_t, z) \\ P_t &= (1 + m) W_t\end{aligned}$$

We shall assume for this question that:

$$F(u_t, z) = 1 - \alpha u_t + z$$

where  $\alpha$  captures the strength of the effect of the unemployment rate on the equilibrium wage, and  $z$  represents the catch-all variable that captures the effect on wages of the policy environment (e.g., minimum wage, employment protection legislation, etc).

1. [8 points] Go to the FRED website ([link here](#)). Download the data series for median usual weekly earnings for those with less than a high school degree and those with a bachelor's degree and higher (series LEU0252916700Q and series LEU0252918500Q). Also download the data series for the Consumer Price Index for All Urban Consumers: All Items in US City Average (series CPIAUCSL) since 2007. Calculate the percent change from a year ago at a quarterly frequency for each series and plot them together in one chart. Calculate the average for each of these three series from 2007 to 2021. Using these averages, what can you say about wage inflation and price inflation in the last 15 years? Is there a difference across educational groups? What has happened to the real wage for each of these groups since 2007?
2. [8 Points] Use the WS and PS relations shown above, together with the specification of the function  $F$ , to derive a formula for  $P_t$  in terms of  $P_t^e$ ,  $u_t$  and parameters  $\alpha, m, z$ .

3. [8 Points] Consider the equation you have derived in the previous part, and use it to derive the Phillips Curve

$$\pi_t = \pi_t^e - \alpha (u_t - u^n),$$

where we have defined the *natural unemployment rate* as  $u^n = (m+z)/\alpha$ .

Hint: to get started, divide both sides of your equation by  $P_{t-1}$ . Then, use the following facts:

$$\frac{P_t}{P_{t-1}} = 1 + \pi_t \quad \frac{P_t^e}{P_{t-1}} = 1 + \pi_t^e \quad \frac{1 + \pi_t}{(1 + \pi_t^e)(1 + m)} \approx 1 + \pi_t - \pi_t^e - m.$$

4. [6 points] Go to the FRED website ([link here](#)). Download the data series for the Consumer Price Index for All Urban Consumers: All Items in US City Average (series CPIAUCSL) and the rate of unemployment (UNRATE) of the years 2021 and 2022. Compute monthly inflation in both years and plot the evolution of monthly inflation and the rate of unemployment. What do you observe? Assuming inflation expectations were constant, was the rate of unemployment below or above its natural rate?

### Question 3 - The IS-LM-PC Model [50 Points]

Consider an economy with aggregate demand,

$$Z_t = c_0 + c_1(Y_t - T) + b_0 + b_1 Y_t - b_2 r_t + G,$$

where  $t$  is a time index,  $Y_t$  is output,  $T$  taxes,  $r_t$  the real interest rate,  $G$  government spending and  $c_0, c_1, b_0, b_1, b_2$  are positive constants so that  $c_1 + b_1 < 1$ . Next, consider the Phillips curve,

$$\pi_t - \pi_t^e = -\alpha (u_t - u_n),$$

where  $\alpha > 0$  is a positive parameter,  $u_t$  is the unemployment rate. The natural rate of unemployment is given by  $u_n = \frac{m+z}{\alpha}$  where  $m$  is a markup and  $z$  is a catch-all variable that stands for all other variables that may affect the natural rate of unemployment.

The labor force  $L_t = L$  is constant and the production function is given by

$$Y_t = N_t$$

where the total employment  $N_t$  is given by  $N_t = (1 - u_t) \cdot L_t$ . The variables  $T, G, m, z, L$  are all exogenous.

#### Part (a) Equilibrium of the IS-LM-PC Model [30 Points]

- [10 Points] Rewrite the Phillips curve relationship in terms of  $(Y_t - Y_n)$  instead of  $(u_t - u_n)$ . Calculate the potential output  $Y_n$  in terms of exogenous variables/parameters. (Note:  $u_n$  is NOT an exogenous variable)
- [10 Points] Solve for the equilibrium output  $Y_t$  as a function of  $r_t$  and other exogenous variables/parameters.
- [10 Points] Using the Phillips curve, solve for the natural rate of interest  $r_n$  associated with the medium-run equilibrium, i.e., the interest rate that achieves  $Y_t - Y_n = \pi_t - \pi_t^e = 0$ . The answer should be in terms of exogenous variables/parameters.

#### Part (b) The Effects of an Increase in the Price of Oil [20 Points]

Remember that the medium run equilibrium is characterized by four conditions:

- Output  $Y$  equals its potential level  $Y_n$
- Unemployment rate  $u$  equals the natural rate of unemployment  $u_n$
- The real interest rate is equal to the natural rate of interest  $r_n$
- The expected rate of inflation  $\pi^e$  is equal to the actual rate of inflation  $\pi$ .

Using the results in Part (a), answer the following two questions. (provide either a qualitative answer based on economic intuition OR an algebraic derivation using the results in Part (a))

1. [10 Points] Assume  $\pi_t^e = \bar{\pi}$ , i.e., that inflation expectations are *anchored*. Suppose the economy is initially at the medium-run equilibrium and, suddenly, OPEC successfully increases oil prices, which can be equivalently seen as an increase in the markup:  $m$  increases to  $m'$  ( $m' > m$ ). What happens to output and inflation in the new short-run equilibrium? What will the central bank do with the real interest rate to reach the new medium-run equilibrium? What will happen with inflation and output along the transition?
2. [10 Points] Suppose we had  $\pi_t^e = \pi_{t-1}$  instead. How does this affect your answers to the previous subpoint? What happens with the level of inflation in the new medium-run equilibrium? Explain the intuition.

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