14.02 - Principles of Macroeconomics

Problem Set 6

Spring 2023

Question 1 – Uncovered Interest Parity (23 points)

Consider two bonds, one issued in euros (€) in Italy and one issued in dollars ($) in the U.S. Assume that both government securities are one-year bonds—paying the face value of the bond one year from now. The exchange rate, E, stands at 0.825 euros per dollar. The face value of the U.S. bond is $10,000. The face value of the Italian bond is €10,000. The price of the U.S. bond is $9,615.38. The price of the Italian bond is €9,433.96.

1. (5 points) Compute the nominal interest rate on each of the bonds.
2. (5 points) Compute the expected exchange rate next year consistent with uncovered interest parity.
3. (4 points) If you expect the dollar to depreciate relative to the euro, relative to the current exchange rate, which bond should you buy?
4. (5 points) Assume that you are a U.S. investor and you exchange dollars for euros at time t at the current exchange rate $E_t = 0.825$, and purchase the Italian bond today. For this subpoint, assume that the exchange rate realization at $t + 1$ is actually $E_{t+1} = 0.792$ euros per dollar. What is your realized rate of return in dollars compared to the realized rate of return you would have made had you held the U.S. bond?
5. (4 points) Are the differences in rates of return in 4. consistent with the uncovered interest parity condition? Why or why not?

Question 2 - Aggregate Demand in an Open Economy [55 points]

Let's assume we have an open economy with demand for domestic goods:

$$Z = C + I + G - IM/\varepsilon + X$$

where the real exchange rate ε, investment I, government spending G, and taxes T are assumed to be exogenous. The consumption is given by

$$C = c_0 + c_1 \cdot (Y - T)$$

where $c_0 > 0$ and $c_1 \in (0, 1)$. Demand for imports and demand for exports are given, respectively, by

$$IM = c_2 \cdot Y \cdot \varepsilon$$
$$X = Y^* - \alpha \cdot \varepsilon$$

where $\alpha > 0$, $c_2 \in (0, c_1)$. Finally, the good market equilbirium is characterized by the condition $Y = Z$.

1. [10 Points] Draw the graph of domestic demand for goods, and the demand for domestic goods, as a function of income on the same chart. When you draw the graph, assume that $Y^* - \alpha\varepsilon > 0$. Do both demands have the same slope? If not, which one is flatter, and why? Using an additional chart underneath the one you just drew, draw net exports as a function of income and specify at which point trade balance arises.

2. [15 Points] Compute GDP and trade balance as a function of exogenous variables and parameters.

3. [10 Points] Based on your answers for subpoint 2, compute the government spending multiplier of GDP and of trade balance (i.e., if G increases by 1, by how much do GDP and trade balance change). Answer the same question for the real exchange rate multiplier (i.e., the effect on output and trade balance of a unit increase in ε).

4. [10 Points] Suppose foreign output Y^* decreases by 1 unit. By how much should domestic government spending change to compensate the increase in trade deficit, if we assume ε is fixed? What is the total effect on GDP?

5. [10 Points] Suppose again that Y^* decreases by 1 unit and the central bank can directly change ε to compensate the effect on trade deficit. By how much should the real exchange rate change? What is the total effect on GDP ? Compare to the previous subpoint: which policy seems more efficient in terms of GDP?

Question 3: Policy Coordination in an Open Economy [22 points]

Consider a world with only two *symmetric* countries: Home and Foreign (*). Demand for home good is

$$Z = C + I + G + X - IM/\epsilon$$

where ϵ is the price of Home goods in terms of Foreign goods, and

$$C = 0.7 \cdot (Y - T)$$
$$X = 0.2 \cdot Y^*/\epsilon.$$

The symmetry implies that demand for foreign good is given by

$$Z^* = C^* + I^* + G^* + X^* - IM^*/\epsilon^*$$

where ϵ^* is the price of Foreign goods in terms of Home goods, and

$$C^* = 0.7 \cdot (Y^* - T^*)$$
$$X^* = 0.2 \cdot Y/\epsilon^*.$$

Government spending G and G^* are exogenously given. Assume $I = I^* = T = T^* = 0$ for simplicity.

1. [6 points] Use the symmetry between two countries to calculate IM

2. [6 points] Calculate the equilibrium output Y and net exports NX in terms of G, Y^*, and ϵ.

3. [4 points] Calculate the equilibrium output Y^* and net exports NX^* in terms of G^*, Y, and ϵ^*. [Hint: Use symmetry]

4. [6 points] Assuming $\epsilon = 1$, calculate Y and NX as a function of G and G^*.

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