14.581 International Trade $Class notes on 2/13/2013^1$

1 Eaton and Kortum (2002)

1.1 Basic Assumptions

- N countries, i = 1, ..., N
- Continuum of goods $u \in [0, 1]$
- Preferences are CES with elasticity of substitution σ :

$$U_i = \left(\int_0^1 q_i(u)^{(\sigma-1)/\sigma} du\right)^{\sigma/(\sigma-1)}$$

- One factor of production (labor)
- There may also be intermediate goods (more on that later)
- $c_i \equiv$ unit cost of the "common input" used in production of all goods
 - Without intermediate goods, c_i is equal to wage w_i in country i
- Constant returns to scale:
 - $-Z_i(u)$ denotes productivity of (any) firm producing u in country i
 - $Z_i(u)$ is drawn independently (across goods and countries) from a **Fréchet distribution**:

$$\Pr(Z_i \le z) = F_i(z) = e^{-T_i z^{-\theta}},$$

with $\theta > \sigma - 1$ (important restriction, see below)

- Since goods are symmetric except for productivity, we can forget about index u and keep track of goods through $\mathbf{Z} \equiv (Z_1, ..., Z_N)$.
- Trade is subject to iceberg costs $d_{ni} \ge 1$
 - d_{ni} units need to be shipped from *i* so that 1 unit makes it to *n*
- All markets are perfectly competitive

 $^{^1\}mathrm{The}$ notes are based on lecture slides with inclusion of important insights emphasized during the class.

1.2 Four Key Results

1.2.1 The Price Distribution

• Let $P_{ni}(\mathbf{Z}) \equiv c_i d_{ni}/Z_i$ be the unit cost at which country *i* can serve a good \mathbf{Z} to country *n* and let $G_{ni}(p) \equiv \Pr(P_{ni}(\mathbf{Z}) \leq p)$. Then:

$$G_{ni}(p) = \Pr\left(Z_i \ge c_i d_{ni}/p\right) = 1 - F_i(c_i d_{ni}/p)$$

• Let $P_n(\mathbf{Z}) \equiv \min\{P_{n1}(\mathbf{Z}), ..., P_{nN}(\mathbf{Z})\}$ and let $G_n(p) \equiv \Pr(P_n(\mathbf{Z}) \leq p)$ be the price distribution in country n. Then:

$$G_n(p) = 1 - \exp[-\Phi_n p^\theta]$$

where

$$\Phi_n \equiv \sum_{i=1}^N T_i (c_i d_{ni})^{-\theta}$$

• To show this, note that (suppressing notation \mathbf{Z} from here onwards)

$$\Pr(P_n \leq p) = 1 - \prod_i \Pr(P_{ni} \geq p)$$
$$= 1 - \prod_i [1 - G_{ni}(p)]$$

• Using

$$G_{ni}(p) = 1 - F_i(c_i d_{ni}/p)$$

then

$$1 - \prod_{i} [1 - G_{ni}(p)] = 1 - \prod_{i} F_{i}(c_{i}d_{ni}/p)$$

= $1 - \prod_{i} e^{-T_{i}(c_{i}d_{ni})^{-\theta}p^{\theta}}$
= $1 - e^{-\Phi_{n}p^{\theta}}$

1.2.2 The Allocation of Purchases

• Consider a particular good. Country n buys the good from country i if $i = \arg\min\{p_{n1}, ..., p_{nN}\}$. The probability of this event is simply country i's contribution to country n's price parameter Φ_n ,

$$\pi_{ni} = \frac{T_i (c_i d_{ni})^{-6}}{\Phi_n}$$

• To show this, note that

$$\pi_{ni} = \Pr\left(P_{ni} \le \min_{s \ne i} P_{ns}\right)$$

• If $P_{ni} = p$, then the probability that country *i* is the least cost supplier to country *n* is equal to the probability that $P_{ns} \ge p$ for all $s \ne i$

• The previous probability is equal to

$$\Pi_{s \neq i} \Pr(P_{ns} \ge p) = \Pi_{s \neq i} \left[1 - G_{ns}(p) \right] = e^{-\Phi_n^{-i} p^{\theta}}$$

where

$$\Phi_n^{-i} = \sum_{s \neq i} T_i \left(c_i d_{ni} \right)^{-\theta}$$

• Now we integrate over this for all possible p's times the density $dG_{ni}(p)$ to obtain

$$\int_0^\infty e^{-\Phi_n^{-i}p^\theta} T_i \left(c_i d_{ni}\right)^{-\theta} \theta p^{\theta-1} e^{-T_i \left(c_i d_{ni}\right)^{-\theta} p^\theta} dp$$
$$= \left(\frac{T_i \left(c_i d_{ni}\right)^{-\theta}}{\Phi_n}\right) \int_0^\infty \theta \Phi_n e^{-\Phi_n p^\theta} p^{\theta-1} dp$$
$$= \pi_{ni} \int_0^\infty dG_n(p) dp = \pi_{ni}$$

1.2.3 The Conditional Price Distribution

- The price of a good that country n actually buys from any country i also has the distribution $G_n(p)$.
- To show this, note that if country n buys a good from country i it means that i is the least cost supplier. If the price at which country i sells this good in country n is q, then the probability that i is the least cost supplier is

$$\Pi_{s \neq i} \Pr(P_{ni} \ge q) = \Pi_{s \neq i} \left[1 - G_{ns}(q) \right] = e^{-\Phi_n^{-i} q^\circ}$$

• The joint probability that country *i* has a unit cost *q* of delivering the good to country *n* **and** is the the least cost supplier of that good in country *n* is then

$$e^{-\Phi_n^{-i}q^{\theta}} dG_{ni}(q)$$

• Integrating this probability $e^{-\Phi_n^{-i}q^{\theta}} dG_{ni}(q)$ over all prices $q \leq p$ and using $G_{ni}(q) = 1 - e^{-T_i(c_i d_{ni})^{-\theta}p^{\theta}}$ then

$$\begin{split} \int_0^p e^{-\Phi_n^{-i}q^\theta} dG_{ni}(q) \\ &= \int_0^p e^{-\Phi_n^{-i}q^\theta} \theta T_i(c_i d_{ni})^{-\theta} q^{\theta-1} e^{-T_i(c_i d_{ni})^{-\theta}p^\theta} dq \\ &= \left(\frac{T_i(c_i d_{ni})^{-\theta}}{\Phi_n}\right) \int_0^p e^{-\Phi_n q^\theta} \theta \Phi_n q^{\theta-1} dq \\ &= \pi_{ni} G_n(p) \end{split}$$

• Given that $\pi_{ni} \equiv$ probability that for any particular good country *i* is the least cost supplier in *n*, then conditional distribution of the price charged by *i* in *n* for the goods that *i* actually sells in *n* is

$$\frac{1}{\pi_{ni}} \int_0^p e^{-\Phi_n^{-i}q^\theta} dG_{ni}(q) = G_n(p)$$

- In Eaton and Kortum (2002):
 - 1. All the adjustment is at the extensive margin: countries that are more distant, have higher costs, or lower T's, simply sell a smaller range of goods, but the average price charged is the same.
 - 2. The share of spending by country n on goods from country i is the same as the probability π_{ni} calculated above.
- We will establish a similar property in models of monopolistic competition with Pareto distributions of firm-level productivity

1.2.4 The Price Index

• The exact price index for a CES utility with elasticity of substitution $\sigma < 1 + \theta$, defined as

$$p_n \equiv \left(\int_0^1 p_n(u)^{1-\sigma} du\right)^{1/(1-\sigma)},$$

is given by

$$p_n = \gamma \Phi_n^{-1/\theta}$$

where

$$\gamma = \left[\Gamma\left(\frac{1-\sigma}{\theta}+1\right)\right]^{1/(1-\sigma)},$$

where Γ is the Gamma function, *i.e.* $\Gamma(a) \equiv \int_0^\infty x^{a-1} e^{-x} dx$.

• To show this, note that

$$p_n^{1-\sigma} = \int_0^1 p_n(u)^{1-\sigma} du =$$
$$\int_0^\infty p^{1-\sigma} dG_n(p) = \int_0^\infty p^{1-\sigma} \Phi_n \theta p^{\theta-1} e^{-\Phi_n p^{\theta}} dp.$$

• Defining $x = \Phi_n p^{\theta}$, then $dx = \Phi_n \theta p^{\theta-1}$, $p^{1-\sigma} = (x/\Phi_n)^{(1-\sigma)/\theta}$, and

$$p_n^{1-\sigma} = \int_0^\infty (x/\Phi_n)^{(1-\sigma)/\theta} e^{-x} dx$$
$$= \Phi_n^{-(1-\sigma)/\theta} \int_0^\infty x^{(1-\sigma)/\theta} e^{-x} dx$$
$$= \Phi_n^{-(1-\sigma)/\theta} \Gamma\left(\frac{1-\sigma}{\theta} + 1\right)$$

• This implies $p_n = \gamma \Phi_n^{-1/\theta}$ with $\frac{1-\sigma}{\theta} + 1 > 0$ or $\sigma - 1 < \theta$ for gamma function to be well defined

1.3 Equilibrium

- Let X_{ni} be total spending in country n on goods from country i
- Let $X_n \equiv \sum_i X_{ni}$ be country *n*'s total spending
- We know that $X_{ni}/X_n = \pi_{ni}$, so

$$X_{ni} = \frac{T_i(c_i d_{ni})^{-\theta}}{\Phi_n} X_n \tag{(*)}$$

- Suppose that there are no intermediate goods so that $c_i = w_i$.
- In equilibrium, total income in country i must be equal to total spending on goods from country i so

$$w_i L_i = \sum_n X_{ni}$$

• Trade balance further requires $X_n = w_n L_n$ so that

$$w_i L_i = \sum_n \frac{T_i(w_i d_{ni})^{-\theta}}{\sum_j T_j(w_j d_{nj})^{-\theta}} w_n L_n$$

- This provides system of N-1 independent equations (Walras' Law) that can be solved for wages $(w_1, ..., w_N)$ up to a choice of numeraire. This is like an exchange economy, where countries trade their own labor.
- Everything is as if countries were exchanging labor
 - Fréchet distributions imply that labor demands are iso-elastic
 - Armington model leads to similar eq. conditions under assumption that each country is exogenously specialized in a differentiated good

- In the Armington model, the labor demand elasticity simply coincides with elasticity of substitution σ
- Under frictionless trade $(d_{ni} = 1 \text{ for all } n, i)$ previous system implies

$$w_i^{1+\theta} = \frac{T_i}{L_i} \frac{\sum_n w_n L_n}{\sum_j T_j w_j^{-\theta}}$$

and hence

$$\frac{w_i}{w_j} = \left(\frac{T_i/L_i}{T_j/L_j}\right)^{1/(1+\theta)}$$

1.4 The Gravity Equation

• Letting $Y_i = \sum_n X_{ni}$ be country i's total sales, then

$$Y_i = \sum_n \frac{T_i \left(c_i d_{ni} \right)^{-\theta} X_n}{\Phi_n} = T_i c_i^{-\theta} \Omega_i^{-\theta}$$

where

$$\Omega_i^{-\theta} \equiv \sum_n \frac{d_{ni}^{-\theta} X_n}{\Phi_n}$$

• Solving $T_i c_i^{-\theta}$ from $Y_i = T_i c_i^{-\theta} \Omega_i^{-\theta}$ and plugging into (*) we get

$$X_{ni} = \frac{X_n Y_i d_{ni}^{-\theta} \Omega_i^{\theta}}{\Phi_n}$$

• Using $p_n = \gamma \Phi_n^{-1/\theta}$ we can then get

$$X_{ni} = \gamma^{-\theta} X_n Y_i d_{ni}^{-\theta} (p_n \Omega_i)^{\theta}$$

• This is the **Gravity Equation**, with bilateral resistance d_{ni} and multilateral resistance terms p_n (inward) and Ω_i (outward).

1.4.1 A Primer on Trade Costs

• From (*) we also get that country *i*'s share in country *n*'s expenditures normalized by its own share is

$$S_{ni} \equiv \frac{X_{ni}/X_n}{X_{ii}/X_i} = \frac{\Phi_i}{\Phi_n} d_{ni}^{-\theta} = \left(\frac{p_i d_{ni}}{p_n}\right)^{-\theta}$$



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• This shows the importance of trade costs and comparative advantage in determining trade volumes. Note that if there are no trade barriers (i.e, frictionless trade), then $S_{ni} = 1$.

Letting
$$B_{ni} \equiv \left(\frac{X_{ni}}{X_{ii}} \cdot \frac{X_{in}}{X_{nn}}\right)^{1/2}$$
 then
$$B_{ni} = \left(S_{ni}S_{in}\right)^{1/2} = \left(d_{ni}^{-\theta}d_{in}^{-\theta}\right)^{1/2}$$

• Under symmetric trade costs (i.e., $d_{ni} = d_{in}$) then $B_{ni}^{-1/\theta} = d_{ni}$ can be used as a measure of trade costs.

We can also see how B_{ni} varies with physical distance between n and i:

2 How to Estimate the Trade Elasticity?

- As we will see the trade elasticity θ is the key structural parameter for welfare and counterfactual analysis in EK model
- Cannot estimate θ directly from $B_{ni} = d_{ni}^{-\theta}$ because distance is not an empirical counterpart of d_{ni} in the model
 - Negative relationship in Figure 1 could come from strong effect of distance on d_{ni} or from mild CA (high θ)
- Consider again the equation

$$S_{ni} = \left(\frac{p_i d_{ni}}{p_n}\right)^{-\theta}$$



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• If we had data on d_{ni} , we could run a regression of $\ln S_{ni}$ on $\ln d_{ni}$ with importer and exporter dummies to recover θ

- But how do we get d_{ni} ?

- EK use price data to measure $p_i d_{ni}/p_n$:
- They use retail prices in 19 OECD countries for 50 manufactured products from the UNICP 1990 benchmark study.
- They interpret these data as a sample of the prices $p_i(j)$ of individual goods in the model.
- They note that for goods that n imports from i we should have $p_n(j)/p_i(j) = d_{ni}$, whereas goods that n doesn't import from i can have $p_n(j)/p_i(j) \le d_{ni}$.
- Since every country in the sample does import manufactured goods from every other, then $\max_{j} \{p_n(j)/p_i(j)\}$ should be equal to d_{ni} .
- To deal with measurement error, they actually use the second highest $p_n(j)/p_i(j)$ as a measure of d_{ni} .
- Let $r_{ni}(j) \equiv \ln p_n(j) \ln p_i(j)$. They calculate $\ln(p_n/p_i)$ as the mean across j of $r_{ni}(j)$. Then they measure $\ln(p_i d_{ni}/p_n)$ by

$$D_{ni} = \frac{\max 2_j \{r_{ni}(j)\}}{\sum_j r_{ni}(j)/50}$$

• Given $S_{ni} = \left(\frac{p_i d_{ni}}{p_n}\right)^{-\theta}$ they estimate θ from $\ln(S_{ni}) = -\theta D_{ni}$. Method of moments: $\theta = 8.28$. OLS with zero intercept: $\theta = 8.03$.

2.1 Alternative Strategies

- Simonovska and Waugh (2011) argue that EK's procedure suffers from upward bias:
 - Since EK are only considering 50 goods, maximum price gap may still be strictly lower than trade cost
 - If we underestimate trade costs, we overestimate trade elasticity
 - Simulation based method of moments leads to a θ closer to 4.
- An alternative approach is to use tariffs (Caliendo and Parro, 2011). If $d_{ni} = t_{ni}\tau_{ni}$ where t_{ni} is one plus the ad-valorem tariff (they actually do this for each 2 digit industry) and τ_{ni} is assumed to be symmetric, then

$$\frac{X_{ni}X_{ij}X_{jn}}{X_{nj}X_{ji}X_{in}} = \left(\frac{d_{ni}d_{ij}d_{jn}}{d_{nj}d_{ji}d_{in}}\right)^{-\theta} = \left(\frac{t_{ni}t_{ij}t_{jn}}{t_{nj}t_{ji}t_{in}}\right)^{-\theta}$$

• They can then run an OLS regression and recover θ . Their preferred specification leads to an estimate of 8.22

2.2 Gains from Trade

- Consider again the case where $c_i = w_i$
- From (*), we know that

$$\pi_{nn} = \frac{X_{nn}}{X_n} = \frac{T_n w_n^{-\ell}}{\Phi_n}$$

• We also know that $p_n = \gamma \Phi_n^{-1/\theta}$, so

$$\omega_n \equiv w_n / p_n = \gamma^{-1} T_n^{1/\theta} \pi_{nn}^{-1/\theta}$$

• Under autarky we have $\omega_n^A = \gamma^{-1} T_n^{1/\theta}$, hence the **gains from trade** are given by

$$GT_n \equiv \omega_n / \omega_n^A = \pi_{nn}^{-1/\theta}$$

- Trade elasticity θ and share of expenditure on domestic goods π_{nn} are sufficient statistics to compute GT
- A typical value for π_{nn} (manufacturing) is 0.7. With $\theta = 5$ this implies $GT_n = 0.7^{-1/5} = 1.074$ or 7.4% gains. Belgium has $\pi_{nn} = 0.2$, so its gains are $GT_n = 0.2^{-1/5} = 1.38$ or 38%.

• One can also use the previous approach to measure the welfare gains associated with any foreign shock, not just moving to autarky:

$$\omega_n'/\omega_n = \left(\pi_{nn}'/\pi_{nn}\right)^{-1/\theta}$$

• For more general counterfactual scenarios, however, one needs to know both π'_{nn} and π_{nn} .

2.2.1 Adding an Input-Output Loop

- Imagine that intermediate goods are used to produce a composite good with a CES production function with elasticity $\sigma > 1$. This composite good can be either consumed or used to produce intermediate goods (input-output loop).
- Each intermediate good is produced from labor and the composite good with a Cobb-Douglas technology with labor share β . We can then write $c_i = w_i^{\beta} p_i^{1-\beta}$.
- The analysis above implies

$$\pi_{nn} = \gamma^{-\theta} T_n \left(\frac{c_n}{p_n}\right)^{-\theta}$$

and hence

$$c_n = \gamma^{-1} T_n^{-1/\theta} \pi_{nn}^{-1/\theta} p_n$$

• Using $c_n = w_n^{\beta} p_n^{1-\beta}$ this implies

$$w_n^\beta p_n^{1-\beta} = \gamma^{-1} T_n^{-1/\theta} \pi_{nn}^{-1/\theta} p_n$$

 \mathbf{SO}

$$w_n/p_n = \gamma^{-1/\beta} T_n^{-1/\theta\beta} \pi_{nn}^{-1/\theta\beta}$$

• The gains from trade are now

$$\omega_n/\omega_n^A = \pi_{nn}^{-1/\theta\beta}$$

• Standard value for β is 1/2 (Alvarez and Lucas, 2007). For $\pi_{nn} = 0.7$ and $\theta = 5$ this implies $GT_n = 0.7^{-2/5} = 1.15$ or 15% gains.

2.2.2 Adding Non-Tradables

- Assume now that the composite good cannot be consumed directly.
- Instead, it can either be used to produce intermediates (as above) or to produce a consumption good (together with labor).

- The production function for the consumption good is Cobb-Douglas with labor share α .
- This consumption good is assumed to be non-tradable.
- The price index computed above is now p_{gn} , but we care about $\omega_n \equiv w_n/p_{fn}$, where

$$p_{fn} = w_n^{\alpha} p_{gn}^{1-\alpha}$$

• This implies that

$$\omega_n = \frac{w_n}{w_n^{\alpha} p_{gn}^{1-\alpha}} = \left(w_n / p_{gn}\right)^{1-\alpha}$$

• Thus, the gains from trade are now

$$\omega_n/\omega_n^A = \pi_{nn}^{-\eta/\theta}$$

where

$$\eta \equiv \frac{1-\alpha}{\beta}$$

• Alvarez and Lucas argue that $\alpha = 0.75$ (share of labor in services). Thus, for $\pi_{nn} = 0.7$, $\theta = 5$ and $\beta = 0.5$, this implies $GT_n = 0.7^{-1/10} = 1.036$ or 3.6% gains

3 Comparative statics (Dekle, Eaton and Kortum, 2008)

• Go back to the simple EK model above ($\alpha = 0, \beta = 1$). We have

$$X_{ni} = \gamma^{-\theta} T_i(w_i d_{ni})^{-\theta} p_n^{\theta} X_n$$
$$p_n^{-\theta} = \gamma^{-\theta} \sum_{i=1}^N T_i(w_i d_{ni})^{-\theta}$$
$$\sum_n X_{ni} = w_i L_i$$

• As we have already established, this leads to a system of non-linear equations to solve for wages,

$$w_i L_i = \sum_n \frac{T_i (w_i d_{ni})^{-\theta}}{\sum_k T_k (w_k d_{nk})^{-\theta}} w_n L_n.$$

• Consider a shock to labor endowments, trade costs, or productivity. One could compute the original equilibrium, the new equilibrium and compute the changes in endogenous variables.

• But there is a simpler way that uses only information for observables in the initial equilibrium, trade shares and GDP; the trade elasticity, θ ; and the exogenous shocks. First solve for changes in wages by solving

$$\hat{w}_i \hat{L}_i Y_i = \sum_n \frac{\pi_{ni} \hat{T}_i \left(\hat{w}_i \hat{d}_{ni} \right)^{-\theta}}{\sum_k \pi_{nk} \hat{T}_k \left(\hat{w}_k \hat{d}_{nk} \right)^{-\theta}} \hat{w}_n \hat{L}_n Y_n$$

and then get changes in trade shares from

$$\hat{\pi}_{ni} = \frac{\hat{T}_i \left(\hat{w}_i \hat{d}_{ni} \right)^{-\theta}}{\sum_k \pi_{nk} \hat{T}_k \left(\hat{w}_k \hat{d}_{nk} \right)^{-\theta}}.$$

- From here, one can compute welfare changes by using the formula above, namely $\hat{\omega}_n = (\hat{\pi}_{nn})^{-1/\theta}$.
- To show this, note that trade shares are

$$\pi_{ni} = \frac{T_i (w_i d_{ni})^{-\theta}}{\sum_k T_k (w_k d_{nk})^{-\theta}} \text{ and } \pi'_{ni} = \frac{T'_i (w'_i d'_{ni})^{-\theta}}{\sum_k T'_k (w'_k d'_{nk})^{-\theta}}.$$

• Letting $\hat{x} \equiv x'/x$, then we have

$$\hat{\pi}_{ni} = \frac{\hat{T}_{i} \left(\hat{w}_{i} \hat{d}_{ni} \right)^{-\theta}}{\sum_{k} T'_{k} \left(w'_{k} d'_{nk} \right)^{-\theta} / \sum_{j} T_{j} \left(w_{j} d_{nj} \right)^{-\theta}} \\ = \frac{\hat{T}_{i} \left(\hat{w}_{i} \hat{d}_{ni} \right)^{-\theta}}{\sum_{k} \hat{T}_{k} \left(\hat{w}_{k} \hat{d}_{nk} \right)^{-\theta} T_{k} \left(w_{k} d_{nk} \right)^{-\theta} / \sum_{j} T_{j} \left(w_{j} d_{nj} \right)^{-\theta}} \\ = \frac{\hat{T}_{i} \left(\hat{w}_{i} \hat{d}_{ni} \right)^{-\theta}}{\sum_{k} \pi_{nk} \hat{T}_{k} \left(\hat{w}_{k} \hat{d}_{nk} \right)^{-\theta}}.$$

• On the other hand, for equilibrium we have

$$w_i'L_i' = \sum_n \pi_{ni}' w_n' L_n' = \sum_n \hat{\pi}_{ni} \pi_{ni} w_n' L_n'$$

• Letting $Y_n \equiv w_n L_n$ and using the result above for $\hat{\pi}_{ni}$ we get

$$\hat{w}_i \hat{L}_i Y_i = \sum_n \frac{\pi_{ni} \hat{T}_i \left(\hat{w}_i \hat{d}_{ni} \right)^{-\theta}}{\sum_k \pi_{nk} \hat{T}_k \left(\hat{w}_k \hat{d}_{nk} \right)^{-\theta}} \hat{w}_n \hat{L}_n Y_n$$

- This forms a system of N equations in N unknowns, \hat{w}_i , from which we can get \hat{w}_i as a function of shocks and initial observables (establishing some numeraire). Here π_{ni} and Y_i are data and we know \hat{d}_{ni} , \hat{T}_i , \hat{L}_i , as well as θ .
- To compute the implications for welfare of a foreign shock, simply impose that $\hat{L}_n = \hat{T}_n = 1$, solve the system above to get \hat{w}_i and get the implied $\hat{\pi}_{nn}$ through

$$\hat{\pi}_{ni} = \frac{\hat{T}_i \left(\hat{w}_i \hat{d}_{ni} \right)^{-\theta}}{\sum_k \pi_{nk} \hat{T}_k \left(\hat{w}_k \hat{d}_{nk} \right)^{-\theta}}$$

and use the formula to get

$$\hat{\omega}_n = \hat{\pi}_{nn}^{-1/\theta}$$

• Of course, if it is not the case that $\hat{L}_n = \hat{T}_n = 1$, then one can still use this approach, since it is easy to show that in autarky one has $w_n/p_n = \gamma^{-1}T_n^{1/\theta}$, hence in general

$$\hat{\omega}_n = \left(\hat{T}_n\right)^{1/\theta} \hat{\pi}_{nn}^{-1/\theta}$$

4 Extensions of EK

- Bertrand Competition: Bernard, Eaton, Jensen, and Kortum (2003)
 - Bertrand competition \Rightarrow variable markups at the firm-level
 - Measured productivity varies across firms \Rightarrow one can use firm-level data to calibrate model
- Multiple Sectors: Costinot, Donaldson, and Komunjer (2012)
 - $T^k_i \equiv$ fundamental productivity in country i and sector k
 - One can use EK's machinery to study pattern of trade, not just volumes
- Non-homothetic preferences: Fieler (2011)
 - Rich and poor countries have different expenditure shares
 - Combined with differences in θ^k across sectors k, one can explain pattern of North-North, North-South, and South-South trade

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