15.S50 - Poker Theory and Analytics

Basic Strategy





1

Basic Strategy

- Terminology Position
- Pot Odds
- Implied Odds
- Fold Equity and Semi-Bluffing



Position Terminology





Position Terminology (6-handed)





Position Basics

- In general, later position is preferred since you get more information before acting
- Playable hands are wider for later positions
- Blinds get a discount to see flops, but are in the worst position for every round thereafter
- Early position offers more opportunity for aggression, and is preferred in some low-M situations
 - e.g. in the "Game of Chicken" situation, first actor gets to
 "throw the steering wheel out the window"

Basic Strategy

- Terminology Position
- Pot Odds
- Implied Odds
- Fold Equity



Why do odds come into play?

- Common situation is weak made hand vs drawing hand
 - i.e. pair or two pair on flop vs straight or flush draw
 - Or pocket pair vs anything else pre flop
- Drawer has to balance chance of hitting draw vs how much each addition card costs
- Made hand wants to
 - Bet enough for the drawer to not have a +EV call
 - Bet an amount that bad players might mistake as good odds



Pot Odds







Pot Odds

John_VH925 (UTG+1): \$500 Blinds 20/40 + 10 Hero (MP1): \$500

Pre Flop: (\$140) Hero is MP1 with A♥ T♥ *1 fold*, John_VH925 raises to \$120, Hero calls \$120, 5 *folds*

Flop: (\$380) 8♥ 3♥ K♣ (2 players) John_VH925 bets \$370 all in, Hero...

Should the hero call?





Pot Odds

• What is the maximum bet the hero should call?





Concept – Expected Value (EV)

- Expected Value is the probability-weighted average of possible results
- EV = Win% * WinAmt Lose% * LoseAmt
- For example,
 - If Win% = 25% and you are facing a \$60 bet into a pot of \$100
 - EV = 25% * (100+60) 75% * 30 = 17.5
- In general, decision rules will be made based on Expected Value
- In Scenario A,
 - our Hero is facing a bet into a pot of \$380
 - EV = W% * (380 + x) L% * x
 - Calling threshold is at EV = 0



Concept – Pot Odds

- Pot Odds are the relationship of the call amount to the size of the pot
- In general, a call will be +EV if Win% > CallAmt/(PotAfterCall)
- For example in our scenario,
 - If the bet were \$100 into pot of \$380
 - Pot Odds would be 100/580, where 580 = (Pot + Bet + Call)
 - Hero's call contributes $\sim 17\%$ of the pot
 - He can profitably call if Win% > 17% of the time
- Win% is based on "Outs" (cards that result in a win)
- Outs are 9 hearts to hit flush
- Win% = $1 (40/49 * 39/48) \approx 34\%$. This gives us the odds to call
- EV = 34% * \$480 \$100 * 66% = \$97.2



Concept – Pot Odds





Pot Odds – Gordon's Rule of 2 or 4

- Phil Gordon
 - Fourth Place in 2001 WSOP ME
 - One WPT title
 - Win Two North American Bridge Championships
 - Head Referee World Series of Rock Paper Scissors
 - Author of *Phil Gordon's Little Green Book*



(DBuy at Amazon) Gordon, Phil. *Phil Gordon's Little Green Book: Lessons and Teachings in No Limit Texas Hold'em*. Simon Spotlight, 2005.



Pot Odds – Gordon's Rule of 2 or 4

- Phil Gordon
 - Author of *Phil Gordon's Little Green Book*
- Each Out is worth about 2% equity per card
- If you get to see both turn and river, use 4% per card



- For example, if have a low pair on the flop and are drawing to three-of-akind, you have 2 outs or about 4% to make your hand on each card.
- Other common examples include:
 - Flush Draw (9 outs) gives you odds of $9/47 \approx 18\% = 9*2\%$
 - Inside Straight Draw (4 outs) gives you odds of $4/47 \approx 8\% = 4*2\%$



Pot Odds – Gordon's Rule of 2 or 4

- Phil Gordon
 - Author of *Phil Gordon's Little Green Book*
- Each Out is worth about 2% equity per card
- If you get to see both turn and river, use 4% per card



- For example, if have a low pair on the flop and are drawing to three-of-akind, you have 2 outs or about 4% to make your hand on each card.
- Other common examples include:
 - Flush Draw (9 outs) gives you odds of $9/47 \approx 18\%$
 - Inside Straight Draw (4 outs) gives you odds of $4/47 \approx 8\%$



Concept – Pot Odds

- Breakeven is when EV = 0
- Bet is *x* into a pot of \$380
- Chance of hitting flush is 9 Outs * 4% (since we get both cards)
- Win% $\approx 36\%$
- Exact Win% = $1 (40/49 * 39/48) \approx 34\%$.
- EV = 34% * (\$380+x) 66% * x = 0 at x = \$404
- So the maximum bet we should call is \$404
- Check with $404 / (404*2 + 380) \approx 0.34$



Solution Set

• Our Hero should call any bet **up to \$404** and fold to anything larger





Practical Solution

John_VH925 (UTG+1): \$500 Blinds 20/40 + 10 Hero (MP1): \$500

Pre Flop: (\$140) Hero is MP1 with A♥ T♥ *1 fold*, John_VH925 raises to \$120, Hero calls \$120, 5 *folds*

Flop: (\$380) 8♥ 3♥ K♣ (2 players) John_VH925 bets \$370 all in, Hero...

Should the hero call?





Practical Solution

In real time: Our Hero knows he will hit the flush about 36% of the time, so he can profitably call up to 36% of the new pot. In the case of a \$370 bet, the Hero will decide to call since the new pot will be 380 + 370 + 370 = 1120 and his contribution is 370/1120 (33%), which is less than his chance of winning (36%)



Villain (MP): \$250 Blinds 20/40 + 10 Hero (BTN): \$1000

Pre Flop: (\$140) Hero is BTN with 6 7 Villain raises to \$90, Hero calls \$90

Flop: (\$320) 8♠ 5♥ K♣ (2 players) Villain bets \$150 all in, Hero...



- 1. What are we drawing to?
 - Straight (open-ended)
- 2. What are our outs?
 - Any 9, any 4 (8 cards total)
- 3. Chance of hitting draw?

- 8 * 4% = 32%

- 4. Correct play?
 - Call, since call is 150 of 620 or 24%
- 5. EV of decision?
 - 32% * 470 68% * 150 = 48.4



Villain (MP): \$3000 Blinds 100/200 Hero (BTN): \$3000

Pre Flop: (\$300) Hero is BTN with 5 \$ 5 Villain raises to \$400, 2 calls, Hero calls \$400

Flop: (\$1900) 5♣ A♣ 6♣ (2 players) Villain bets \$200, 2 folds, Hero...



- 1. What are we drawing to?
 - Full House or 4-of-a-kind
- 2. What are our outs?
 - 3x A or 6, 1x 5 (7 cards total)
- 3. Chance of hitting draw?
 - 7 * 2% = 14%
- 4. Correct play?
 - Call, since call is 200 of 2300 or 9%
- 5. EV of decision?
 - 14% * 2100 86% * 200 = 122



Villain (BB): \$200 Blinds 100/200 Hero (SB): \$1000

Pre Flop: (\$300) Hero is SB with 5♣ 7♥ Hero...



- 1. What are we drawing to?
 - Anything
- 2. Chance of hitting draw?
 - 570 vs ATC \approx 40% [320 vs ATC \approx 32%]
- 3. Correct play?
 - Call, since call is 100 of 400 or 25%
- 4. EV of decision?
 - 40% * 300 60% * 100 = 60

Basic Strategy

- Terminology Position
- Pot Odds
- Implied Odds
- Fold Equity



Implied Odds – Hand Rules

- We are trying to find the amount of chips we need to win **after hitting our draw** to make the bet we are facing a good call
- We do this by figuring out what the pot would have to be after our call to make our *x*% chance of winning equal to the *x*% of the pot for the call
- For example, if we have a flush draw (18% to hit), and we are facing a bet of \$180 into a pot of \$300, then our call represents \$180/\$660 = 27% of the pot (i.e. too expensive to call)
- This would be a good call if we contributed 18% of the pot, or \$180/\$1000. So we need to find \$1000 - \$660 = \$340 in dead money
- The additional \$340 after the draw makes our \$180 bet worth 18% of a \$1000 pot



We need 18% for this to be a good call





We make our call 18% by adding \$340 of dead money









Villain (MP): \$3000 Blinds 25/50 Hero (BTN): \$3000

Pre Flop: (\$75) Hero is BTN with K♦ T♥ Villain raises to \$150, *2 folds*, Hero calls \$150, *2 folds*

Flop: (\$375) T♣ A♥ 6♦ (2 players) Villain bets \$100, Hero...



- 1. What are we drawing to?
 - Two pair or 3-of-a-kind
- 2. What are our outs?
 - 3x K, 2x T (5 cards total)
- 3. Chance of hitting draw?
 - 5 * 2% = 10%
- 4. Pot odds?
 - \$100 of \$575, or about 19%, too expensive
- 5. Additional bets after draw to breakeven?
 - \$100/10% = \$1000 \$575 = \$425 more







Villain (MP): \$3000 Blinds 25/50 Hero (BTN): \$3000

Pre Flop: (\$75) Hero is BTN with K♣ Q♣ Villain raises to \$100, 2 folds, Hero calls \$100, 2 folds

Flop: (\$275) T♣ J♣ 3♥ (2 players) Villain bets \$600, Hero...


Implied Odds Examples

- 1. What are we drawing to?
 - Straight or Flush
- 2. What are our outs?
 - − Any A, any 9, 7 other ♣ (15 cards total)
- 3. Chance of hitting draw?

-15 * 2% = 30%

- 4. Pot odds?
 - \$600 of \$1475, or about 41%, too expensive
- 5. Additional bets after draw to breakeven?
 - \$600/30% = \$2000 \$1475 = \$525 more



Drawing Formulas

- EV (Marginal Value of Any Decision)
 - x = Win%*WinAmt Lose%*LoseAmt
- Rule of 2 or 4 (Chance of Hitting Draw)
 - -x = 2% * #Outs * #FreeCards
- Pot Odds (Decision Rule to Call Bet)
 - Win% > CallAmt/(Pot + BetAmt + CallAmt)
- Implied Odds (Additional Chips After Draw Hits Needed to Call)
 - x = (BetAmt / Win%) (Pot + BetAmt + CallAmt)



Drawing Formulas (Example)

- EV (Marginal Value of Decision)
 - Calling a \$150 bet into a \$320 pot to have a 32% chance of winning
 - \$48.4 = 32% (\$320 + \$150) 68% (\$150)
- Rule of 2 or 4 (Chance of Hitting Draw)
 - You have 9 Outs to a Flush and get to see Turn (not River)
 - 18% = 2% * 9 * 1
- Pot Odds (Decision Rule to Call Bet)
 - You are facing a \$370 all-in bet for a \$380 pot with a flush draw
 - 36% > \$370/(\$380 + \$370 + \$370) =**TRUE**
- Implied Odds (Additional Chips After Draw Hits Needed to Call)
 - \$100 bet into pot of \$375 with 2-pair/3-o-a-k draw on Turn
 - \$425 = (\$100 / 10%) (\$375 + \$100 + \$100)





© ESPN/World Series of Poker. All rights reserved. This content is excluded from our Creative Commons license. For more information, see http://ocw.mit.edu/help/faq-fair-use/.



• YouTube video:

ManiaOFpoker. "World Series Of Poker 2014 Main Event Episode 14 HD 720p." November 11, 2017. *YouTube*. Accessed May 1, 2014. https://youtube/Q1HkLjq-GGQ?t=23m24s







Hero (UTG): 22,450k 150k/300k Blinds + 50k Tonking (SB): 6,775k

Pre Flop: (950k) Hero is UTG with A♣ J♣ Hero calls 300k, 7 *folds*, Tonking calls 150k, Sindelar checks

Flop: (1,400k) 7♣ 8♥ T♣ (3 players) Tonking checks, Sindelar bets 500k, Hero raises to 1,750k, Tonking raises 4,525k to 6,275k all in, Sindelar folds

Hero...



- What are we drawing to?
 - Flush, maybe straight
- What are our outs?
 - 2,3,4,5,6,8,9,Q,K of ♣ (9 cards) and maybe 9 of ♠ ♦ ♥ (3 cards)*50%
 - Count this as 10.5 outs
- Chance of hitting draw?
 - -10.5 * 4% = 42%
- Correct play?
 - Pot will be 1400k + 500k + 2*6,275k = 14,450k. Call amount is 4,525k or $\approx 31\%$. So call.
- EV of Decision?

- EV = 42% * 9925k - 58% * 4,525k = 1544k



Drawing – Be careful about

• Drawing to a hand that might not win at showdown

- i.e. a Q-high or lower flush
- Or the low end of a straight
- Or a flush/straight on a paired board
- Assuming you will get to see turn and river for one bet
 - This very rarely happens unless the aggressor is all-in
 - A lot of players will bet on flop with a draw to get this
- Overestimating how easy it is to extract additional chips
 - Flush draws hitting on turn/river are very easy to spot
 - Straight draws are less easy, hitting sets is difficult to see
- Betting too little and letting other players make +EV calls
 - Most flop, turn bets should be around half to 2/3rds of the pot

Basic Strategy

- Terminology Position
- Pot Odds
- Implied Odds
- Fold Equity and Semi-Bluffing



Fold Equity







Turkito694 (UTG): \$2098.00 Hero (CO): \$990.00 Blinds \$5/\$10

Pre Flop: (\$15.00) Hero is CO with 6♠ 7♠

River: (\$350.00) A♦ 5♥ 8♦ Q♠ 2♦ (2 players) Turkito694 checks Hero bets \$150...

How often does this bluff have to work to be profitable?



Concept – Fold Equity

- Fold Equity is the value a player gains from the likelihood that the other player will fold to his bet, assuming a call will result in a loss
- Fold Equity = Current Pot * Fold% Bet * (1-Fold%)
 - If SD-Win% = 0
- Fold Equity = Current Pot * Fold% + (1-Fold%) * EV-if-Called
 - If SD-Win% > 0
- SD Value = (1-Fold%) * EV-if-Called
- **Bluffing** is a bet that is +EV because Fold Equity > 0
- **Semi-bluffing** is a bet that is +EV with negative Fold Equity offset by sufficiently high Showdown-Win%



Fold Equity

River: (\$350.00) A♦ 5♥ 8♦ Q♠ 2♦ (2 players) Turkito694 checks Hero bets \$150...

How often does this bluff have to work to be profitable?

Bet is 150 into pot of 350. Showdown-Win% = 0.

```
EV = 350 * Fold\% - 150 * (1 - Fold\%)
```

EV > 0 when Fold% > 150/(350+150) = 30%

Check with EV = 30% * 350 - 70% * 150 = 0

This seems +EV, given that Hero is representing a flush





Turkito694 (UTG): \$2098.00 Hero (CO): \$990.00 Blinds \$5/\$10

Pre Flop: (\$15.00) Hero is CO with 6♠ 7♠

River: (\$350.00) A♦ 5♥ 8♦ Q♠ 2♦ (2 players) Turkito694 checks Hero bets \$150...

How often does this bluff have to work to be profitable?



- Using our example:
 - BetAmt = 150
 - Pot = 350

 $- Fold\% = \frac{-2*BetAmt*Win\%+BetAmt-Pot*Win\%}{-2*BetAmt*Win\%+BetAmt-Pot*Win\%+Pot} - Fold\% = (13W\% - 3) / (13W\% - 10)$























Sensitivity to Bet Size – Impact of Win%

- A pot sized bet would mean a 1% increase in Win% leads to a 1.5% decrease in breakeven Fold%
- A higher bet increases the sensitivity, but it is bound by the interval (1,2)

$$\lim_{Bet \to Pot} \frac{\partial F\%}{\partial W\%} = 1.5$$

 $\lim_{Bet\to\infty}\frac{\partial F\%}{\partial W\%}=2$

$$\lim_{Bet\to 0}\frac{\partial F\%}{\partial W\%}=1$$



Fold Equity – Real Time

- When SDValue = 0
 - F% needed = bet / (pot + bet)
 - Pot sized bet needs to win 50% of time
 - Scales approximately linearly down to zero
 - i.e. a half pot size bet needs to win about 25% of the time
 - actual fold rate needed is .5 / 1.5 = 33%
- When SDValue > 0
 - This is difficult to develop quick rules
 - In general, your value is much higher if you have a real draw
 - A good assumption is your SD-Win% decreases the Fold% 1.5x to 1
 - Preflop is basically always semi-bluffing







Fold Equity Examples

Villain (MP): \$3000Blinds 25/50Hero (BTN): \$3000

Pre Flop: (\$75) Hero is BTN with T♦ 5♠ Villain raises to \$150, *2 folds*, Hero calls \$150, *2 folds*

River: (\$375) 4♣ 8♥ 9♦ 6♥ 6♦ (2 players) Villain checks, Hero bets \$250...



Fold Equity Examples

1. Bluff or semi-bluff?

– Bluff

- 2. What is our Showdown Win%? 0
- 3. What is our breakeven Fold%?

- \$250 / \$625 = 40%

4. Is this a good bet if Villain calls 25% of the time?

- Yes, 75% > 40%

5. What is our Fold Equity if Villain calls 25%?

$$- $375 * 75\% - $250 * 25\% = 218.75$$







Fold Equity Examples

Villain (MP): \$800 Blinds 25/50 Hero (BTN): \$1500 Blinds 25/50

Pre Flop: (\$75) Hero is BTN with 9♥ T♥ Villain raises to \$150, *2 folds*, Hero calls \$150, *2 folds*

Turn: (\$775) 4♣ 8♠ 7♦ 2♥ (2 players) Villain checks, Hero bets \$450 ...



Fold Equity Examples

1. Bluff or semi-bluff?

- Semi-bluff, SD Win% = 16%

- 2. What is our Showdown Value if Villain calls 80%?
 - 80% * [16% * \$1225 84% * \$450] = -\$145.6
- 3. What is our breakeven Fold%?

- \$450 / \$1225 = 37% - 16% * 1.5 = 13%

4. Is this a good bet if Villain calls 80% of the time?

- Yes, 20% > 13%

- 5. What is our Fold Equity if Villain calls 80%?
 - $\$775 \cdot .20 + .80 \cdot (16\% \cdot \$1225 84\% \cdot \$450) = 9.4$





© ESPN/World Series of Poker. All rights reserved. This content is excluded from our Creative Commons license. For more information, see http://ocw.mit.edu/help/faq-fair-use/.





• YouTube video:

ManiaOFpoker. "World Series Of Poker 2014 Main Event Episode 14 HD 720p." November 11, 2013. *YouTube*. Accessed May 1, 2015. https://youtu.be/Q1HkLjq-GGQ?t=30m5s







Jacobson (MP2): 22,000k Hero (CO): 18,000k 150k/300k Blind + 50k

Pre Flop: (950k) Hero is CO with A♣ Q♥ 4 *folds*, Jacobson raises to 650k, 1 fold, Hero raises to 1,425k, 3 *folds*, A♥ exposed, Jacobson calls 775k

Flop: (3,800k) K♦ J♥ 3♣ (2 players) Jacobson checks, Hero bets 1,800k

Is this a good bet?



Pre Flop: (950k) Hero is CO with A♣ Q♥

Flop: (3,800k) K♦ J♥ 3♣ (2 players) Jacobson checks, Hero bets 1,800k

Is this a good bet?

If SD-Win% = 0, the bet is +EV at F%>1800/(3800+1800) = 33%

If only the inside straight draw is good, Win% = 8%, making the breakeven Fold% closer to 21%



Pre Flop: (950k) Hero is CO with A♣ Q♥

Flop: (3,800k) K♦ J♥ 3♣ (2 players) Jacobson checks, Hero bets 1,800k

Is this a good bet?

If we assume any T wins (4 card) and any A wins sometimes (2 cards *.5) then chance to make draw is about 5 * 2 = 10%

Full solution is EV = 3800 * F% - [90% * 1800 * (1-F%)] + [10% * (1-F%) * 5600] = 0 at F% = 21.8%

This is profitable if the Villain folds more than 22% of the time.



Live Example (Result)



© ESPN/World Series of Poker. All rights reserved. This content is excluded from our Creative Commons license. For more information, see http://ocw.mit.edu/help/faq-fair-use/.





Bluffing Formulas

- Fold% (Minimum Fold Rate if SDWin% = 0)
 - -x = BetAmt / (Pot + BetAmt)
- Fold Equity (EV of Bluff, assuming SDWin% = 0)
 - -x = Fold% * Pot (1-Fold%) * BetAmt
- Showdown-Value (EV Contribution of Being Called)
 - x = (1-Fold%) * (Win%*WinAmt Lose%*LoseAmt)
- Fold Equity (EV of Semi-Bluff, if SDWin% > 0)
 - x = Fold% * Pot + (1-Fold%) * (Win%*WinAmt Lose%*LoseAmt)
- Semi-Bluff Fold% (Quick Rule for Breakeven Semi-Bluff Fold%)
 - -x = BetAmt / (Pot + BetAmt) 1.5x Win%



Bluffing Formulas (Example)

- Fold% (Minimum Fold Rate if SDWin% = 0)
 - Making a \$150 bluff into a \$350 pot
 - 30% = \$150 / (\$350 + \$150)
- Fold Equity (EV of Bluff, assuming SDWin% = 0)
 - Making a \$250 bluff into a pot of \$625 against a 25% call rate
 - \$218.75 = 75% * \$625 (1-75%) * \$250
- Showdown-Value (EV Contribution of Being Called)
 - Making a \$450 bluff into a pot of \$775 with a 16% WinRate against an 80% call rate
 - -\$145.6 = (1-20%) * (16% *\$1225 84% *\$450)
- Fold Equity (EV of Semi-Bluff, if SDWin% > 0)
 - \$9.4 = 20% * \$1225 + (1-20%) * (16% * 1225 84% * 450)
- Semi-Bluff Fold% (Quick Rule for Breakeven Semi-Bluff Fold%)
 - 13% = \$450 / (\$775 + \$450) 1.5*16%



Bluffing – Be careful about

- Betting too little on a bluff
 - If you had a real hand, you wouldn't bet $1/3^{rd}$ of the pot
 - Or at least you shouldn't, but we'll get to that
 - Bet enough to make a draw -EV
- Betting too much on a bluff
 - Pot overbets are basically never a good idea (unless you are pot committed on a normal sized bet)
 - If you are short-stacked, don't bluff an amount that would require you to call a raise (i.e. you would have the odds to call a raise)
- Being afraid of being caught bluffing or showing down bad cards
 - This is really common, especially live
- Semi-bluffing when a free card is offered

Bluffing calling stations

MIT OpenCourseWare http://ocw.mit.edu

15.S50 Poker Theory and Analytics January IAP 2015

For information about citing these materials or our Terms of Use, visit: http://ocw.mit.edu/terms.