## Semantic Localization

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## Overview

1. Motivation for Semantic Localization
2. Particle Filters
3. Semantic Localization Implementation

## Motivation

## Orienteering Grand Challenge



## What would you do?

- You're dropped in the wild
- You have a compass
- You have a map



## Orienteering Relocation Tips

Tips from orienteering experts!:

- "Relocate: everyone gets disoriented from time to time."
- "Stop, locate your last known location on the map, think about what you've seen and what direction you were moving, and how far you have gone."
- "Look around you for any feature large or unique enough to be mapped."


## OrienteeringMaps


apen ground rough open ground woodiand: run woodand: slow run woodand: walk fight undergrowth
dirt path indistinct path fence, gats high fence
high wal
seat, cray water uncrossable marsh marsh. seasonal marsh stream, bridge index contour
contour
form line
earthwal broken ground lenal pit cepression

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## What do we want in our map?


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|  | Robot | Human |
| :---: | :---: | :---: |
| Encodes | distances, surfaces | rooms, objects, relationships |
| Memory | dense | sparse |
| Useful for | motion planning | activity planning |

## Semantic Information

"Signs and symbols that contain meaningful concepts for humans"

## Semantic Information: Why is it important?

Human-robot interaction
Function-driven navigation and planning
Performance and memory optimization
Cheaper hardware

## Semantic Localization

The problem of localizing based on semantic information

For the Grand Challenge, we have a map with labeled objects and their coordinates

How can we localize based on what objects we see?

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## Localization

Simple question: Where am I?
Not so simple answer
The answer depends on the map used


## Metric Localization

If you want quantitative pose description:
You need metric map for localization
X, Y, Z coordinates in space
Angles for orientation

## Metric Localization

Quantitative pose descriptions


## Review of Localization

- Localization problem statement

Suppose that the control $u_{t}$ is applied to the robot and, after moving, the robot obtains a random observation $z_{t+1}$. Given a prior belief over $x_{t}$ and the map Y, what is the posterior belief of $\mathrm{x}_{\mathrm{t}+1}$ after taking takes $\mathrm{z}_{\mathrm{t}+1}$ and $\mathrm{u}_{\mathrm{t}}$ into account?

- When we translate the localization question into probabilistic terms, we aim to find the distribution

$$
\begin{aligned}
& p\left(x_{t+1} \mid x_{t}, z_{t+1}, u_{t}, Y\right) \\
& \text { position at position observation command map } \\
& \text { time } \mathrm{t}+1 \text { at time } \mathrm{t} \text { at time } \mathrm{t}+1 \text { variable at time } \mathrm{t}
\end{aligned}
$$

## Review of Localization

- The Bayesian expansion of this posterior decomposes into

$$
p\left(z_{t+1} \mid x_{t+1}\right) p\left(x_{t+1} \mid x_{t}, u_{t}\right) p(x)
$$

Observation Actuation model Belief noise model
representation

- Our representation of the map limits what models we can use:
- Topological map: actuation model to be transition probabilities
- Laser scan observations: noise model over $\mathscr{R}^{n}$
- Object detection observations: noise model over sets, or boolean variables


## Particle Filters

- Representing our posterior over poses can be difficult

$$
p\left(z_{t+1} \mid x_{t+1}\right) p\left(x_{t+1} \mid x_{t}, u_{t}\right)(p(x))
$$

- Kalman filter $\rightarrow p(x)$ is a Gaussian
- Particle filter $\rightarrow \mathrm{p}(\mathrm{x})$ is approximated by a set of points


## Localization demo



## Particle Filter

Sequential Importance Sampling Technique
Algorithm Steps:
0. Sample (using Initial Belief)

1. Update Weights
2. Resample
3. Propagate

## Particle Filter-Example

Focus on problem with only one dimension

Aircraft


- Constant altitude
- Unknown x location
- Noisy forward velocity


## Sensor



- Measures distance to ground below
- Noisy measurements

- Known mapping of x location to ground altitude

Goal: Determining unknown state - our location

## Particle Filter- Example



## Particle Filter

Algorithm Steps:
0. Sample (using Initial Belief)

If completely unknown initial state $>\mathrm{N}$ samples from uniform distribution

1. Update Weights
2. Resample
3. Propagate

## Initial Sampling with Unknown State



## Particle Filter

Algorithm Steps:
0. Sample (using Initial Belief)

If completely unknown initial state -> N samples from uniform distribution

1. Update Weights

Compare observations to expectations of each particle
2. Resample
3. Propagate

## Measured value from our noisy sensor



## Expected height values of each particle



## Likelhood that particle explains measurement



## Particle weights based on likelihood



## Particle Filter

Algorithm Steps:
0. Sample (using Initial Belief)

If completely unknown initial state $->\mathrm{N}$ samples from uniform distribution

1. Update Weights

Compare observations to expectations of each particle
2. Resample

Create N new samples based on weight distribution calculated
3. Propagate

## Resample from measurement distribution



## Resample from measurement distribution



## Particle Filter

Algorithm Steps:
0. Sample (using Initial Belief)

If completely unknown initial state $->\mathrm{N}$ samples from uniform distribution

1. Update Weights

Compare observations to expectations of each particle
2. Resample

Create N new samples based on weight distribution calculated
3. Propagate

Use dynamics model or inputs to propagate particles Take into account uncertainty with new weight calculations

## Dynamics Model

Delta t between sensor measurements


Need to propagate particles in time


## Dynamics Model

Delta t between sensor measurements


Need to propagate particles in time


## Dynamics Model

New weights based on probability of particle transition


How likely was it for the plane to move that far in delta t?


## Particle Filter

Algorithm Steps:
0. Sample (using Initial Belief)

If completely unknown initial state -> N samples from uniform distribution

1. Update Weights

Compare observations to expectations of each particle
2. Resample

Create N new samples based on weight distribution calculated
3. Propagate

Use dynamics model or inputs to propagate particles
Take into account uncertainty with new weight calculations
Repeat Steps 1 - 3

## Keep filtering

Using new measurements and propagating through time
Time Step 2


## Keep fillering

Using new measurements and propagating through time
Time Step 3


## Keep filtering

Using new measurements and propagating through time
Time Step 4


## Keep filtering

Using new measurements and propagating through time
Time Step 5


## Keep filtering

Using new measurements and propagating through time
Time Step 6


## Keep filtering

Using new measurements and propagating through time
Time Step 7


## Keep filtering

Using new measurements and propagating through time
Time Step 8


## Localization demo



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## Implementation

$$
p\left(z_{t+1} \mid x_{t+1}\right) p\left(x_{t+1} \mid x_{t}, u_{t}\right) p(x)
$$

Continuously Solve for most probable x
Thats our location

## Psuedo Code

While the robot is moving
Make observations

$$
\begin{gathered}
Z_{t+1} \\
P(x)
\end{gathered}
$$

Generate a probable location
Update that location based on actuation

$$
P\left(x_{t+1} / x_{t}, u_{t}\right)
$$

Simulate the observations at that location
$\geq P\left(z_{t+1} / x_{t+1}\right)$
Update our location estimates based on comparison

## Observation model selection

We need $_{t}$ o define $\mathbf{z}$ (our observation)
$\mathrm{A}_{\mathrm{L}}$ abeled Laser Scan
$\mathrm{A}_{\mathrm{S}}$ cene with Objects at Locations

$$
\mathrm{A}_{\mathrm{S}} \text { et of } \mathrm{O} \text { bjects }
$$

## Field-of-view with laser scanner



Legend
mailbox
tree
house

## Object-Point Assumption



Legend
mailbox
tree
house

## Field-of-view with point objects



Legend
mailbox
tree
house

Check each point for intersection with FOV

## Field-of-view with polygon objects



Legend
mailbox
tree
house

## New observation type means new error types

Depending on what we characterize the observation as, there are different opportunities to get it wrong

Observation
Potential Errors
Distance \& Bearing

Object Class

Sets of Objects

Noise, Sensor Limitations

Classification Error

Equality under Permutations

$$
P\left(z_{t+1} / x_{t+1}\right) \quad \Longrightarrow \quad P(Z / Y(x), x)
$$

$Z=$ Set of Observed Objects

$$
\{\text { House, Mailbox }\}
$$

$Y(x)=$ Set of Expected Objects for a given position
$X=$ Position

## Example

## Trees \& Mailboxes <br>  <br> 

$$
Z=\{\text { Tree, Tree, Mailbox }\}
$$



$$
Y=?
$$



## What Do We Need To Consider?

Did we classify our observations correctly?
Did we observe everything in our FoV?
Did we interpret nothing as something?

Diu we inteipiet two things as ont thing?
Key Assumption 1: Each observation corresponds to exactly 1 object

## Did we classify correctly?

Assume: We see everything in our FoV<br>Assume: We never see something that doesn't exist

$$
\begin{gathered}
\text { Solve } \\
P(Z \mid Y(x), x)
\end{gathered}
$$

$$
Y=?
$$



## Did we classify correctly?

Assume: We see everything in our FoV
Assume: We never see something that doesn't exist

$$
Z=\{\square \omega \omega\} \quad Y=\left\{\begin{array}{c}
\{\omega \omega \omega\} \\
\{\omega \square \square \omega\}
\end{array}\right.
$$

$$
\underline{P i}=\{Z \Rightarrow Y\}
$$

## Did we classify correctly?

Assume: We see everything in our FoV
Assume: We never see something that doesn't exist
This can keep expanding in relevant terms depending on the structure that detects objects

$$
P\left(z_{i} / y_{i}, x\right)=P\left(c / y^{\text {class }}\right) P\left(s / c, y^{\text {class }}\right) P(b / y, x)
$$

How often do we miss classify

If classifications have a score, is that score statistically likely

If we know the bearing we are viewing the object, does that effect classification?

## Did we classify correctly?

Assume: We see everything in our FoV
Assume: We never see something that doesn't exist

$$
P(Z \mid Y(x), x)=\sum^{n} \prod_{10}^{n} P\left(Z_{i, p i} \mid y_{i}, x\right)
$$



## Did we see everything?

Assume. We see everything inour FoV Assume: We never see something that doesn't exist

$$
\begin{aligned}
& Z=\left\{\begin{array}{lll}
\square & \omega & \omega
\end{array}\right\} \\
& \mathrm{Y}=\begin{array}{c}
\left\{\square \square \omega_{\mathrm{m}}\right\} \\
\{\square \Rightarrow \square
\end{array}
\end{aligned}
$$

## Did we see everything?



Assume: We never see something that doesn't exist

What if we see nothing

$$
P(\varnothing / Y(x), x)
$$

## Did we see everything?



Assume: We never see something that doesn't exist

$$
P(\varnothing / Y(x), x)=\prod_{\mathrm{i}=0}^{|Y(x)|}\left(1-P\left(y_{i} / x\right)\right)
$$

Key Assumption 2: An object is observed with some probability $P\left(y_{i} / x\right)$, and not with probability $1-P\left(y_{i} / x\right)$
Key Assumption 3: For a given position $x$ and map, any two object detections are independent

$$
Y=?
$$



## Did we see nothing as something？

> Assume. We see everything in our Fov Assume: We never see something that doesi't exist

$$
\begin{aligned}
& \mathrm{Z}=\left\{\begin{array}{lll}
\square & \text { \% } & 3
\end{array}\right\} \\
& \mathrm{Y}= \\
& \text { [-ロー・ }
\end{aligned}
$$

## Did we see nothing as something?

What if there is nothing

$$
P(Z \mid \varnothing, x)
$$

## Did we see nothing as something?

$$
P(Z \mid \emptyset, x)=e^{\lambda} \prod^{|z|}(\lambda \times K(z))
$$

Key Assumption 4: Noise is poisson distributed in time according to $\lambda$ and spatially according to $K(z)$

## Did we see nothing as something?

So what is $K(z)$ ?


## Putting it all together

Solve

$$
P(Z \mid Y(X), X)
$$

$$
0
$$

## Putting it all together

## Solve

$$
P(Z \mid Y(x), x)
$$

## Let

$$
|Z|=|Y|-n+o
$$

Where $n$ is missed detections and $o$ is false detections

## Putting it all together

## Solve

$$
P(Z \mid Y(x), x)
$$

$P(Z \mid Y(x), x)=$
Pi now maps both actual and false detections
$\sum \prod_{i=0}^{\mathrm{pi}} P\left(z_{i, p i}^{|Y|} / y_{i}, x\right)^{*} P\left(y_{i} / x\right)$
$* \prod^{\mathrm{n}}\left(1-P\left(y_{i} \mid x\right)\right) * e^{\lambda} \prod^{\circ}\left(\lambda * K\left(z_{p i}\right)\right)$

## Semantic Localization Video



## Why?

Humans can't walk into a room and reproduce an exact map, but we can store the most important aspects of the room and reason about what they're used for.

Robots can store a pixel-perfect map of a room, but have no intuitive understanding.
This means we're better at actually doing tasks with the environment.
How can we make robots localize and think more like humans?

## Conclusion

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## References

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http://www.us.orienteering.org/orienteers/training/getting-started
Various YouTube videos embedded in slides

## Appendix: Our Semantic Map Definition

- We will use a labeled object map dl which is a set of labeled N objects $<\mathrm{P}_{\mathrm{i}}, \mathrm{c}_{\mathrm{i}}>$ for $\mathrm{i}=1 . . . \mathrm{N}$
- $\mathrm{P}_{\mathrm{i}}$ is an ordered list of vertices $<\mathrm{x}, \mathrm{y}>$ of the polygon boundary


Legend mailbox
tree
house

- $c_{i}$ is the class of the object, e.g. tree
- Our robot pose $\mathrm{x}_{\mathrm{t}}$ will be a position and orientation $<\mathrm{x}, \mathrm{y}, \theta>$
- The actuation model can be any continuous dynamical probability model
- Must define the observation noise model

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