Chain Rule

1. The temperature on a hot surface is given by

$$T = 100 \,\mathrm{e}^{-(x^2 + y^2)}.$$

A bug follows the trajectory $\mathbf{r}(t) = \langle t \cos(2t), t \sin(2t) \rangle$.

a) What is the rate that temperature is changing as the bug moves?

b) Draw the level curves of T and sketch the bug's trajectory.

2. Suppose w = f(x, y) and $x = t^2$, $y = t^3$. Suppose also that at (x, y) = (1, 1) we have $\frac{\partial w}{\partial x} = 3$ and $\frac{\partial w}{\partial y} = 1$. Compute $\frac{dw}{dt}$ at t = 1.

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