Distances to planes and lines

1. Using vector methods, find the distance from the point (1,0,0) to the plane 2x + y - 2z = 0. Include a 'cartoon' sketch illustrating your solution.

<u>Answer</u>: The sketch shows the plane and the point P = (1, 0, 0). Q = (0, 0, 0) is a point on the plane. R is the point on the plane closest to P.

As usual, our sketches are merely suggestive and we do not actually find the point R. The figure shows that

distance =
$$|PR| = \left| \overrightarrow{\mathbf{PQ}} \right| \cos \theta = \left| \overrightarrow{\mathbf{PQ}} \cdot \frac{\mathbf{N}}{|\mathbf{N}|} \right|.$$

Computing $\overrightarrow{\mathbf{PQ}} = \langle 1, 0, 0 \rangle$ gives



2. Using vector methods, find the distance from the point (0,0) to the line 2x + y = 2. Include a sketch.

<u>Answer</u>: Finding the distance from a point to a line in the plane is just like finding the distance from a point to a plane in space.

The normal to the line is $\mathbf{N} = \langle 2, 1 \rangle$ and a point on the line is Q = (1, 0). We have



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