### 18.04 Recitation 1

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1.1. Is is true that $e^{\log (z)}=z$ ? Is is true that $\log \left(e^{z}\right)=z$ ?
1.2. If you know one value of $\log (z)$, what are all the other values?
2. Let $z_{1}=2 e^{i \pi / 3}$ and $z_{2}=3+4 i$.
2.1. Compute $\log \left(z_{1}\right)$. What is the value in the principal branch?
2.2. Compute $\log \left(z_{2}\right)$. What is the value in the principal branch?
3.1. Is $z^{a}$ single valued or multi-valued? Why?
3.2. Suppose $z \neq 0$. Is $z^{a}$ single valued or multi-valued when $a$ is an integer?
3.3. If $a$ is a real number, what do all the $a^{\text {th }}$ powers of $z$ have in common?
3.4. If $a$ is a purely imaginary number, what do all the $a^{\text {th }}$ powers of $z$ have in common?
4. Let $z_{1}=2 e^{i \pi / 3}$ and $z_{2}=3+4 i$.
4.1. Compute $z_{1}^{z_{2}}$.
4.2. Compute $z_{1}^{1 / 4}$. How many distinct values do you get? Plot all these values in the complex plane.

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### 18.04 Complex Variables with Applications

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