### 18.04 Recitation 11

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1.1. Find an LFT from the half-plane $H_{\alpha}:=\{(x, y): y>x \tan (\alpha)\}$ to the unit disc $D_{1}$ centered at the origin.
1.2. Find a conformal map from the strip $I_{\pi}:=\{(x, y): 0<y<\pi\}$ to the upper half-plane $H$.
1.3. Find a conformal map from the upper semi-disc $R_{2}:=\left\{(x, y) \in D_{1}: y>0\right\}$ to the upper half-plane $H$.
1.4. Find a conformal map from the "infinite well" $W_{\pi}:=\{(x, y): 0<y<\pi, x<0\}$ to the upper half-plane.
2.1 Find the reflection of a point $z_{1}$ in the $x$-axis.
2.2. Define the reflection $r_{C}\left(z_{2}\right)$ of a point $z_{2}$ in a circle $C$ as follows. Let $T_{C L}$ be an LFT mapping the circle $C$ to a line $L$. Then, $r_{C}\left(z_{2}\right):=T_{C L}^{-1}\left(r_{L}\left(T_{C L}\left(z_{2}\right)\right)\right)$, where $r_{L}$ denotes reflection in the line $L$. Use this definition to find the reflection of a point $z_{2}$ in the unit circle.

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### 18.04 Complex Variables with Applications

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