Open Problem 3.3 Let $G=(V, E, W)$ be a graph and $k$ a positive integer, is the following true?

$$
\begin{equation*}
\rho_{G}(k) \leq \operatorname{poly} \log (k) \sqrt{\lambda_{k}} . \tag{30}
\end{equation*}
$$

We note that (30) is known not to hold if we ask that the subsets form a partition (meaning that every vertex belongs to at least one of the sets) [LRTV12]. Note also that no dependency on $k$ would contradict the Small-Set Expansion Hypothesis above.

## 5 HHHFH

[LRTV12] A. Louis, P. Raghavendra, P. Tetali, and S. Vempala. Many sparse cuts via higher eigenvalues. STOC, 2012.

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