### Variation Buildup in Single Parts

- Learn about the history of interchangeable parts
- See how parts are given tolerances
- Learn what geometric dimensioning and tolerancing is all about
- Look ahead to variation buildup in assemblies

#### The Business Case for Tolerances



## Definitions

- Tolerance
  - What is allowed or acceptable, defined by "specification limits"
  - Specification limits are set by engineers, designers, and/or manufacturing people
- Variation
  - What actually happens with real parts and assemblies
  - Variation can be measured
- Clearance
  - Empty space between surfaces on different parts
  - Often confused with "tolerance"
  - Clearances can have tolerances and can vary
- These are typical definitions in the academic and professional literature

# History of Interchangeable Parts

- Quest for interchangeability
  - Begins in 1760s as a customer requirement for muskets
- Evolved as a means to systematize manufacturing (1830s)
- Culminates in Ford's moving assembly line
  - Permits rapid assembly and mass production
  - Enables supply chains
  - Avoids coordination
  - The "zeroth" interchange occurs at first assembly
- Enabled supply chains via standards for gaging and tolerancing (1915 to today)

## History - 2

 Geometric Dimensioning and Tolerancing (GD&T) replaced ±dimensions (1940s +)

- Replicated gaging procedures on paper

- Solid modeling CAD forced reconsideration of GD&T on a more mathematical basis
- Parts tolerancing seems OK but assemblies are still something of a mystery
- Coordination makes a comeback as demand for quality exceeds capability

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Source:

Figure 5-1 in [Whitney 2004] Whitney, D. E. *Mechanical Assemblies: Their Design, Manufacture, and Role in Product Development*. New York, NY: Oxford University Press, 2004. ISBN: 0195157826.

# Geometric Dimensioning and Tolerancing

- Seeks to deal with solid objects rather than lines on paper
- The result is definition of "zones" where surfaces should lie
- This is good from the point of view of being realistic about solid objects
- It does not shed light on what the tolerances should be in order to achieve any particular function

# How Big is a Cube?

Conventional drawing showing one face



This arrow really sets the distance between two lines. This means nothing. A more realistic view of the cube



How many arrows are needed to say how far apart the two surfaces are???

# All Acceptable Cubes Lie Between Two Perfect Nested Cubes



#### The Actual Surface Must Lie Inside the Zone

Rule #1: The surface must be correct at max material condition.



# Goals of Geometric Dimensioning and Tolerancing

- Account for 3D Geometry of Parts
- Define Datum Hierarchy
  - A, B, C
  - Corresponds to 3,2,1 of Constraint
  - Standardizes machining, fixturing, and gaging
  - Make the A surface wide, stable, 3 points separated
- Guarantee that any randomly selected pair of parts will assemble (i.e., "worst case" tolerancing)
- Has become an international standard
- Does not apply to assemblies

# GD&T Control Frame for Locating and Sizing a Feature



# Virtual Condition Guarantees Assembly



The virtual condition is a perfect round perpendicular pin .300 diam

Part variations 9/30/2004 © Daniel E Whitney

## Virtual Condition Guarantees Assembly - 2



The virtual condition is a perfect round perpendicular hole .305 diam

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# GD&T is ~Equivalent to Chain of Frames Inside a Part



# Summary

- The goal of interchangeable parts is over 250 years old
- Parts can be toleranced by international standard methods in ways that
  - Respect our notions of constraint
  - Locate features with respect to datum surfaces
  - Can ~be represented by chains of frames similar to the way assemblies can
  - Impose worst-case tolerances
- No standard exists for tolerancing assemblies
- No clear path exists in standard methods for linking assembly goals to part tolerancing