

Name:

BE.011/2772J
Spring 2004
QUIZ I
February 23, 2004

You have 1 hour for this exam.

CLOSED BOOK
1 page notes allowed

1 (10points)	
2 (5 points)	
3 (25 points)	
4 (60 points)	
total (100 points)	

$$k = 1.38 \times 10^{-23} \text{ J/K}$$

Continued on next page....

Name:

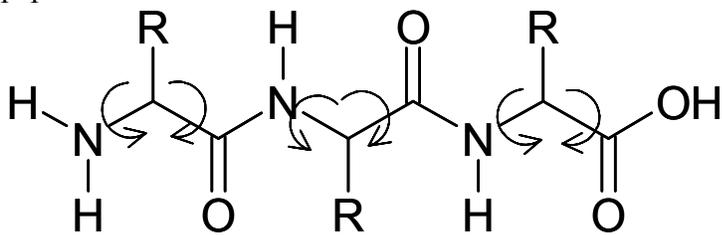
1.) (10 points) **ELVIS is everywhere**

a.) Given 20 naturally occurring amino acids, what is the probability that the amino acid sequence ELVIS occurs in a stretch of a protein sequence?

b.) What is the probability if the order of the amino acids did not matter, i.e., VLSEI, etc.?

2.) (5 points) **Protein folding.**

a.) A protein is a linear chain of amino acids. The amino acid has two torsional angles than can vary around the α carbon, ψ and ϕ . Due to sterics, ψ and ϕ have 3 possible configurations apiece, yielding $3 \times 3 = 9$ possible configurations per amino acid. Pictured below is a three residue peptide:



If a protein has $n = 100$ amino acids, how many different configurations are possible?

Name:

3.) (25 points) **Conditional probabilities of the genetic code**

a) A codon is a sequence of 3 nucleotides that specifies a particular amino acid. How many codons are possible out of the 4 nucleotides?

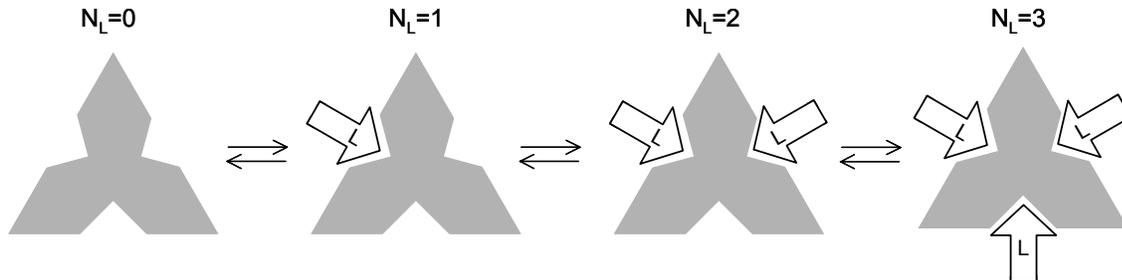
b) Using the table for the genetic code below, what is the joint probability of obtaining a G in the second position (G_2) and A in the first (A_1)?

First Letter	Second Letter								Third Letter
	U		C		A		G		
U	UUU	Phe	UCU	Ser	UAU	Tyr	UGU	Cys	U
	UUC	Phe	UCC	Ser	UAC	Tyr	UGC	Cys	C
	UUA	Leu	UCA	Ser	UAA	Stop	UGA	Stop	A
	UUG	Leu	UCG	Ser	UAG	Stop	UGG	Trp	G
C	CUU	Leu	CCU	Pro	CAU	His	CGU	Arg	U
	CUC	Leu	CCC	Pro	CAC	His	CGC	Arg	C
	CUA	Leu	CCA	Pro	CAA	Gln	CGA	Arg	A
	CUG	Leu	CCG	Pro	CAG	Gln	CGG	Arg	G
A	AUU	Ile	ACU	Thr	AAU	Asn	AGU	Ser	U
	AUC	Ile	ACC	Thr	AAC	Asn	AGC	Ser	C
	AUA	Ile	ACA	Thr	AAA	Lys	AGA	Arg	A
	AUG	Met	ACG	Thr	AAG	Lys	AGG	Arg	G
G	GUU	Val	GCU	Ala	GAU	Asp	GGU	Gly	U
	GUC	Val	GCC	Ala	GAC	Asp	GGC	Gly	C
	GUA	Val	GCA	Ala	GAA	Glu	GGA	Gly	A
	GUG	Val	GCG	Ala	GAG	Glu	GGG	Gly	G

c) Calculate the degree of correlation for obtaining a Serine given G_2 . Is it negatively/positively/not correlated, or mutually exclusive?

Name: **4.) (60 points) Protein ligand binding**

A protein has $M = 3$ sites for binding a ligand. The sites are indistinguishable from each other, as are the ligands.



a) Express the number of ways N_L ligands can be arranged in M sites, $W(M, N_L)$.

b) Calculate the multiplicity and also the entropy for the following states. $N_L = 1$ means that one ligand is bound, $N_L = 0$ means no ligands are bound, etc. You may leave the entropy in terms of the Boltzmann constant, k .

(i) $N_L = 0$

(ii) $N_L = 1$

(iii) $N_L = 2$

(iv) $N_L = 3$

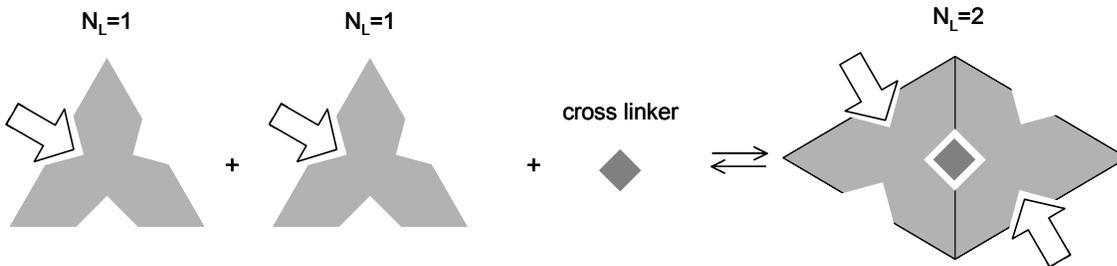
Name:

c) Plot the probability distribution as a function of the number of ligands, $p(N_L)$.

d) Calculate the variance of the distribution.

Name:

e) Upon addition of a cross linker, the protein can dimerize to form the following dimer (pictured below). The dimer can bind up to 4 ligands.



What is the entropy of the dimeric protein where $N_L=2$ (pictured)? You may leave in terms of k .

f) Compare the entropy of two proteins as monomers (left) with $N_L=1$ with the entropy of the dimer (right). What is the change in entropy, ΔS , going from monomeric to dimeric, in terms of k ? Based on your calculation, is the system more likely to be in the monomeric or dimeric form?