Philosophy of QM 24.111

Eighth lecture, 23 February 2005

Strategy for analysis

- 1. Break the experimental situation up into steps.
- 2. At each step, look for easy cases.
- 3. Describe hard cases as linear combinations of easy cases.
- 4. Make use of the linearity of Schrödinger's Equation to "transfer" the analysis of the easy cases over to the hard cases: if

 $\Phi \rightarrow \Phi',$

and

 $\Psi \not \rightarrow \Psi',$

then

 $a\Phi + b\Psi \rightarrow a\Phi' + b\Psi'$.

5. Make discreet use of the collapse postulate, as needed.









Spin measurements revisited

What the hell sort of state is that???

Never mind. It will quickly "collapse" into either





















THE TWO-PATH EXPERIMENT— What we observe:





 $| up, 90^{\circ} > | in R1 > \longrightarrow 1/\sqrt{2} | up, 0^{\circ} > | in R2 > + 1/\sqrt{2} | down, 0^{\circ} > | in R3 >$





Two-path analyzed 4



Two-path with detector 1



Two-path with detector 2



Two-path revisited



A warning about "superposition"

Remember that

"SUPERPOSITION"

is a <u>mathematical</u> term. It means the same thing as "LINEAR COMBINATION".

Thus,

```
1/\sqrt{2} | up, 0°> | in R2 > + 1/\sqrt{2} | down, 0°> | in R3 >
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is a superposition of

| up, 0°> | in R2 >

and

| down, 0°> | in R3 >.

It does not follow that the components $|up, 0^{\circ}|$ in R2 > and $|down, 0^{\circ}|$ in R3 > describe distinct parts of the particle (one part located in R2, the other located in R3.

The rotation box 1

We can build a box with the following feature:



The rotation box 2



The rotation box 3

Remember that we didn't have to choose the upward pointing arrow to represent | up, 0 >. We could equally well represent things this way:



The "total-of-nothing" box 1

Now let's build a more complicated box

whose insides look like this:



What will this box do to the spin state of a particle sent through it?

Answer: NOTHING.

The "total-of-nothing" box 2

To see why, observe how the spin-state vector changes:



A twist on the two-path 1



A twist on the two-path 2



A twist on the two-path 3



Here is a box. Inside it there might be a

If there is a bomb, and you

- open the box;
- jiggle the box;
- send but a single photon through the box;
- try to find out whether there is a bomb by any other "classical" means;
- YOU WILL SET THE BOMB OFF.



- set $\omega = \pi/n$
- cycle particle through n times before second magnet



- set $\omega = \pi/n$
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superposition = $\cos(\pi/2n)$ | up, 0>| in R2> + $\sin(\pi/2n)$ | down, 0>| in R3>



superposition = $\cos(\pi/2n)$ | up, 0>| in R2> + $\sin(\pi/2n)$ | down, 0>| in R3>



superposition = $\cos(\pi/2n)$ | up, 0> | in R2> + $\sin(\pi/2n)$ | down, 0> | in R3>

If there is a bomb, what is the probability that it never explodes?

ANSWER: Just the probability of getting **n** "up" outcomes in a row.

The probability of getting one "up" outcome, given that the spin state of the measured particle is | up, π/n >, is $\cos^2(\pi/2n)$.

So the probability of getting **n** "up" outcomes is

$$\cos^{2n}(\pi/2n)$$

This number goes to 1, in the limit as $n \Rightarrow \infty$.

So quantum bomb-detection works!!!





