## Class 5: Refined statistical models for phonotactic probability

(1) (Virtually) no restrictions on initial CV sequences:

| Vowel | /p/ | /t/ | /k/ |
| :---: | :---: | :---: | :---: |
| [i] | peel | teal | keel |
| [I] | pick | tick | kick |
| [e] | pale | tale | kale |
| [ع] | pen | ten | Ken |
| [æ] | pan | tan | can |
| [u] | pool | tool | cool |
| [v] | put | took | cook |
| [o] | poke | toke | coke |
| [0] | Paul | tall | call |
| [ ${ }^{\text {] }}$ | puff | tough | cuff |
| [a] | pot | tot | cot |
| [ar] | pine | tine | kine |
| [av] | pout | tout | cow |
| [эІ] | poise | toys | coin |
| [ju] | puke | - | cute |

(2) Relatively more restrictions on VC combinations:

| Vowel | /p/ | /t/ | /k/ |
| :--- | :--- | :--- | :--- |
| $[\mathrm{i}]$ | leap | neat | leek |
| $[\mathrm{I}]$ | lip | lit | lick |
| $[\mathrm{e}]$ | rape | rate | rake |
| $[\varepsilon]$ | pep | pet | peck |
| $[æ]$ | rap | rat | rack |
| $[\mathrm{u}]$ | coop | coot | kook |
| $[\overline{\mathrm{v}} \mathrm{]}$ | - | put | book |
| $[\mathrm{o}]$ | soap | coat | soak |
| $[\mathrm{\rho}]$ | - | taught | walk |
| $[\Lambda]$ | cup | cut | tuck |
| $[\mathrm{a}]$ | top | tot | lock |
| $[\mathrm{ar}]$ | ripe | right | like |
| $[\mathrm{av}]$ | - | bout | - |
| $[\mathrm{r}]$ | - | (a)droit | - |
| $[\mathrm{ju}]$ | - | butte | puke |

And compare also voiced:

| Vowel | /b/ | /d/ | /g/ |
| :--- | :--- | :--- | :--- |
| $[\mathrm{i}]$ | grebe | lead | league |
| $[\mathrm{I}]$ | bib | bid | big |
| $[\mathrm{e}]$ | babe | fade | vague |
| $[\varepsilon]$ | Deb | bed | beg |
| $[æ]$ | tab | tad | tag |
| $[\mathrm{u}]$ | tube | food | - |
| $[v]$ | - | could | - |
| $[\mathrm{o}]$ | robe | road | rogue |
| $[\supset]$ | daub | laud | log |
| $[\Lambda]$ | rub | bud | rug |
| $[\mathrm{a}]$ | cob | cod | cog |
| $[\mathrm{ar}]$ | bribe | ride | - |
| $[\mathrm{av}]$ | - | loud | - |
| $[\mathrm{I}]$ | - | void | - |
| $[\mathrm{ju}]$ | cube | feud | fugue |

(3) CV co-occurrence for voiced stops

| Vowel | /b/ | /d/ | /g/ |
| :---: | :---: | :---: | :---: |
| [i] | beep | deep | geek |
| [r] | bin | din | gill |
| [e] | bait | date | gait |
| [ $\varepsilon$ ] | bet | deck | get |
| [æ] | back | Dan | gap |
| [u] | boon | dune | goon |
| [v] | book | - | good |
| [0] | boat | dote | goat |
| [ $]$ | ball | doll | gall |
| [ ${ }^{\text {] }}$ | bun | done | gun |
| [a] | bot | dot | got |
| [ar] | buy | dine | guy |
| [av] | bout | doubt | gout |
| [эІ] | boy | doi(ly) | goi(ter) |
| [ju] | butte | - | (ar)gue |

And after sonorants:

| Vowel | /m/ | /n/ | /n/ | /l/ | /r/ | /w/ | /j/ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| [i] | meat | neat | - | leap | reap | weep | yeast |
| [I] | mitt | nip | - | lip | rip | whip | yip |
| [e] | mate | Nate | - | late | rate | wait | yay |
| [ $\varepsilon$ ] | met | net | - | let | wreck | wet | yet |
| [æ] | mat | nap | - | lap | rap | wax | yak |
| [u] | moot | newt | - | lute | route | woo | you |
| [v] | Muslim | nook | - | look | rook | wood | Europe |
| [0] | moat | note | - | lope | rope | woke | yoke |
| [ $]$ | moss | naught | - | $\log$ | Ross | walk | yawn |
| [ ${ }^{\text {] }}$ | mutt | nut | - | luck | rut | what | young |
| [a] | mock | knock | - | lock | rock | wand | yard |
| [ar] | mine | nine | - | line | rhyme | whine | - |
| [av] | mouse | now | - | lout | route | wound | (yowl) |
| [эг] | moist | noise | - | loin | Roy | [ju] | - (yoink) |

(4) Kessler \& Treiman (1997)

Pearson's $\chi^{2}$ : tests whether relative frequencies of events match predicted (theoretical) frequencies

- In this case: is observed onset/coda asymmetry significantly different from the predicted (equal) distribution?

| $[\mathrm{k}]$ | Onset | Coda |
| :--- | :---: | :---: |
| Observed | 148 | 214 |
| Predicted | 181 | 181 |

(5) Calculation of $\chi^{2}$ :

$$
\chi^{2}=\sum \frac{(\text { Observed-Expected })^{2}}{\text { Expected }}
$$

So for the [k] example:

$$
\frac{(148-181)^{2}}{181}+\frac{(214-181)^{2}}{181}=2 \times \frac{33^{2}}{181}=12.033
$$

(Incidentally: for most uses, Fisher's Exact Test is actually a more honest test)
(6) Nosofsky's GCM:

Similarity of $i$ to existing items $j=\sum e^{-D \cdot d_{i, j}}$
Where

- $d_{i, j}=$ "psychological distance" between $i$ and $j$
- $\quad D$ is a parameter (set to 1 or 2 )
- $e=2.718281828$
(7) Bailey and Hahn (2001): Adapting the GCM for neighborhood effects
- Similarity of items $d_{i, j}$ intuitively related to how differences they have
- How many of their phonemes differ (cat,cap > cat,tap)
- How important those differences are (cat, cap > cat, cup)
- Use string edit distance algorithm to calculate how many modifications are needed to transform one word into the other
- Use method devised by Broe (1993), Frisch (1996), and Frisch, Broe and Pierrehumbert (1997) to weight the relative cost of different modifications based on the similarity of the segments involved
- Also, want to let token frequency plays a role, but in a complex way: not only are low frequency words less important, but very high frequency words are also ignored
- Implementation: add a quadratic weighting term, to allow greater influence of mid-range items (parabola-shaped function)
Similarity of $i=\sum\left(A f_{j}{ }^{2}+B f_{j}+C\right) \cdot e^{-D \cdot d_{i, j}}$

