3.020 Lecture 10

Prof. Rafael Jaramillo



1 Unary phase transformations



• Enthalpy (or "heat") of melting

$$\Delta H^{s \to l} = \Delta Q_{rev}^{s \to l} = T_m \Delta S^{s \to l}$$

Higher-temp phase always has higher entropy Consider $\alpha \leftrightarrow \beta$ coexistence at temp $T^{\alpha \to \beta}$

• Heating converts $\alpha \to \beta$

$$dn^{\alpha} = -dn^{\beta} < 0$$

- Heating increases entropy $dS = \frac{\delta Q|_{rev}}{T^{\alpha \leftrightarrow \beta}} > 0$
- Entropy is extensive $S' = n^{\alpha}S^{\alpha} + n^{\beta}S^{\beta}$

requires that $S^{\beta} > S^{\alpha}$



 S^{α}, S^{α} : molar entropy of phases intensive

S': total entropy of system extensive

2 Building unary phase diagrams

(1) Role of chemical potential

$$dG^{'} = -S^{'}dT + V^{'}dP + \sum_{k} \mu^{k}dn^{k}$$

At fixed (T, P), equilibrium condition is dG = 0



(2) What is chemical potential ?

$$\mu = \frac{\partial G}{\partial n}_{T,P} = \text{molar Gibbs free energy}$$
$$G'(T, P, n = 1) = \mu \qquad G'(T, P, n) = n\mu$$

- (3) Determining phase equilibrium-drawing phase diagrams
 - (a) At each (P,T), calculate μ for all possible phases
 - (b) Equilibrium phae is the one with lowest $\mu(P,T)$
 - (c) If multi phases have equal μ , then they can coexist

3 Chemical potential surfaces

- $\mu(T, P)$ is a surface over the (T, P) plane
- Each phase has its own surface



• Calculating $\Delta \mu$ for a change in temperature/pressure for a given phase

$$d\mu = -SdT + VdP$$

$$\Delta \mu = \int_{i}^{f} d\mu = \underbrace{\int_{i}^{f} dT(-S) + \int_{i}^{f} dPV}_{i}$$

implicitly assumes that we have EoS for S(T, P), V(T, P)



• In general we don't know S(T, P) and V(T, P), but we can calculate from S^0, V^0 at standard conditions and differential forms :

$$dS = \frac{C_P}{T}dT - V\alpha dP$$



• Caculating $\Delta \mu$ for a change of phase at fixed (T, P)

$$\Delta \mu = \Delta G = \Delta H - T \Delta S$$

- At phase coexistence, $\Delta \mu = 0$, $\Delta H = T \Delta S$
- Away from phase coexistence, can evaluate $\Delta H, \Delta S$ from standard values and differential froms:

$$dH = C_P dT + V(1 - T\alpha)dP$$
$$dS = \frac{C_P}{T} dT - V\alpha dP$$

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