

### 3.15 Transformers and DC motors C.A. Ross, DMSE, MIT

**References:**

Braithwaite and Weaver, Electronic Materials, sections 3.2 and 3.3  
(Jiles, Introduction to Magnetism and Magnetic Materials 4.3.3 & 12.1.7)

**How do transformers work?**

Two coils wrap around a soft magnetic core. The input side has a varying current  $i_m$  through  $n$  turns of wire.

Ampere:  $\oint H \cdot dl = ni_m$

Within the core,  $B = \mu_0 \mu_r H$

(Soft magnet: large, nearly constant  $\mu_r$ )

Put a secondary coil around the core:  $n'$  turns

Faraday  $V = -n' d\phi/dt$

where  $\phi = B \cdot A$  ( $A$  = coil area)

Now we draw a current from the secondary: current  $i_s$  induces a current  $i_p$  back in the primary. Now primary current is  $i_m + i_p$ .

Power transferred  $V_s i_s = V_p i_p$ , where  $V_s/V_p = n'/n$

Properties of the core:

- easy to magnetize to have a high  $B$
- high  $B_s$
- low hysteresis
- resistive to avoid eddy currents.

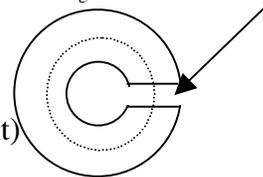
Soft magnetic materials

	$T_c$ / K	$B_s$ / T	$H_c$ / A/m	$\mu_r$	$W$ , J/m <sup>3</sup>
Fe	1043	2.2	~4	200,000	30
Fe-3%Si	1030	2.1	~12	40,000	30
a-FeBSi	630	1.6	~0	>100,000	15

**How do DC motors work?**

We characterize hard magnets by the  $(BH)_{max}$  product in the hysteresis loop. For the magnet to be able to do some useful work, it needs to produce some external flux, e.g. at the gap of a ring-shaped magnet with a cut made in it. Field  $H_g$  exists in the gap.

Ampere:  $l_m H_m + l_g H_g = 0$  around dotted line  
 also  $B_m = B_g$   
 $B_m = \mu_0 \mu_r H_m$  (negative since in second quadrant)  
 $B_g = \mu_0 H_g$   
 hence  $H_m = -l_g B_m / l_m \mu_0$



This linear relation intersects the hysteresis loop and defines uniquely the operating point.

The amount of work that can be done by the magnet is proportional to  $l_g H_g B_g$  so scales with the  $(BH)_{\max}$  product.

In a permanent magnet motor: a current  $i$  runs through a wire length  $l$  in a  $B$  field.

Force  $F = Bi l$  (use Fleming's left hand rule)

This gives a force perpendicular to the wire and to  $B$ .

- A radial  $B$  is produced by two permanent magnets called the stator.
- The wire is wrapped round a vertical piece made of a soft magnet (the rotor). The purpose of the soft magnet is to concentrate the flux lines through the coil, giving maximum  $B$ .
- Current is supplied by a commutator (sliding contact).

Desirable properties of the permanent magnets: must stay magnetized despite their shape, and the fields produced by the wire, hence a high coercivity. Must produce large  $B$ , hence a high  $B_s$  i.e. high  $(BH)_{\max}$ .

Efficiency of motor is maximized if we can reduce the resistive losses in the wire. So minimize  $\rho i / ABv$ , where  $\rho$  is resistivity,  $A$  is wire x-section and  $v$  is rotation velocity.

#### Hard magnetic materials

	$T_c / K$	$B_r / T$	$H_c / kA/m$	$(BH)_{\max}, kJ/m^3$
Alnico-5	1160	1.4	64	44
$BaO.(Fe_2O_3)_6$	720	0.4	264	28
SmCo5	1000	0.85	600	140
$Nd_2Fe_{14}B$	620	1.1	890	216
		remanence		