

Hi everyone, quick question.

Alright, in McQuarrie (year 2000 edition), equation (5-8) defines the q_{trans} as

$$(2\pi mkT/h^2)^{(3/2)} * V$$

That's all well and good, and I can understand how they obtain this. However, later on in the chapter, they use the approximation $Q = q^N/N!$ and then solve for entropy to get (5-20) as

$$S = k * \ln(Q) = x * \ln(q^N/N!) = N k \ln ((2\pi mkT/h^2)^{(3/2)} * V * e^{(5/2)}/N)$$

sorry for the crappy equations, I didn't want to send latex jpeg's in case you wanted to post this.

Alright, so why does the $e^{(5/2)}/N$ term appear instead of $(1/N!)$? Is this some form of sterling's approximation that I might have missed? It seems that these terms seem to appear and disappear at will. Equation (5-16) has e^1 instead of $e^{(5/2)}$ like 5-20.

Hope I didn't miss something obvious here, but I've been a bit stumped by this.

The entropy of an ideal gas can be calculated as:

$$S = (E - A) / T$$

We know that $A = -kT \ln Q$

where $Q = q^N/N!$ and $q = (2\pi mkT/h^2)^{(3/2)} V = V/\Lambda^3$

We can use this to calculate $\ln Q$, (using Sterlings Approximation):

$$\ln Q = -N \ln N + N + N \ln q = N \ln (Ve/N/\Lambda^3)$$

e comes from the fact that we incorporate the ' N ' term in the logarithm and $N * \ln(e) = N$.

Now,

$$A = -kT \ln Q = -kT N \ln (Ve/N/\Lambda^3)$$

The Energy E of an ideal gas is given by

$$E = (3/2) NkT$$

We can then substitute $S = (E - A) / T$

$$S = (3/2) Nk + Nk \ln (Ve/N/\Lambda^3)$$

$$S = Nk(3/2 + \ln (Ve/N/\Lambda^3))$$

To put the ' $3/2$ ' term in the \ln term, we need to do the following:

$$3/2 = \ln(e^{3/2})$$

$$S = Nk(\ln(e^{3/2}) + \ln(Ve/N/\Lambda^3)) = \ln(V/N/\Lambda^3 * e^{5/2})$$

since

$$\ln(e^{3/2}) + \ln(e) = \ln(e^{5/2})$$

Hope this works..