

There was a heated argument in the grad lounge today. And I need your help in proving that I am right and the other person is wrong.

We all know that:

$$dU(S,V) = (dU/dS)_{\text{constant } V} dS + (dU/dV)_{\text{constant } S} dV$$

and this corresponds to:

$$du(S,V) = T dS - P dV$$

and therefore

$$T = (dU/dS)_{\text{constant } V} \text{ and } P = -(dU/dV)_{\text{constant } S}$$

--Everything above this line is true

One of us says that this same method can be applied for U as a function of T and P. That is:

$$dU(T,P) = (dU/dT)_{\text{constant } P} dT - (dU/dP)_{\text{constant } T} dP$$

--Line above is true. That is just math: expressing the differential of a function of two variables.

and this corresponds to:

$$dU(T,P) = S dT - V dP$$

--Who is the scoundrel that says the above thing? This must be an invented statement? You see, the way we get to the equations of state is by comparing a mathematically true statement: $dU(S,V) = (dU/dS)_{\text{constant } V} dS + (dU/dV)_{\text{constant } S} dV$, with the first/second law combo: $du(S,V) = T dS - P dV$.

--And by the way, when we do this for other functions (F,G,H etc.) we are implicitly still using the first/second law combo.

--The scoundrel that claims that $dU(T,P) = S dT - V dP$ is making it up. --There is no such statement in thermodynamics.

and therefore:

$$S = (dU/dT)_{\text{constant } P} \text{ and } V = (dU/dP)_{\text{constant } T}$$

The argument against this is that we know $dU = T dS - P dV$. But we cannot say anything like $U = TS - PV$ because we only know that $dU = \delta Q + \delta W$ and that does not give info on the integral of dU .

I can't say which is my argument for fear of being wrong in front of the professor.

--If this does settle the score, I suggest you duel it out. I will be --happy to referee. No seriously, I'll be happy to talk to you in --person if more clarification is needed.

Gerd Ceder