

3.46 PHOTONIC MATERIALS AND DEVICES

Homework Assignment 5—March 17, 2006

Due: 5pm, March 24, 2006

1. Quantum Wells

- (a) Write the expression relating the quantized energy states of a 1D quantum well with well width.
- (b) Make a plot of the confined E_n values versus quantum well layer thickness, d , for a GaAs/AlAs quantum well (refer to Fundamentals of Photonics pg. 550 for bandgap energy values). The range of your d values should be from 5 nm to 100 nm.

2. LEDs

Consider a GaAs Light-Emitting Diode. In a photoluminescence experiment, you measure the lifetime at temperature $T = 4.2$ K (the temperature of liquid helium) to be 100 ns. You assume that at this very low temperature, you have successfully damped phonons and all possible non-radiative sources of de-excitation; you assume $\tau_r = 100$ ns. You slowly raise the temperature of your cryostat sample holder back up to room temperature, and now measure a lifetime of 50 ns.

At 300 K,

- (a) What is the non-radiative lifetime τ_{nr} ?
- (b) What is the internal quantum efficiency η_i ?
- (c) For an LED design, assume an absorption coefficient of $\alpha = 10^4 \text{ cm}^{-1}$, LED device top layer thickness of $t = 2 \text{ }\mu\text{m}$, and the GaAs refractive index $n = 3.6$. What is the external quantum efficiency η_{ext} ?
- (d) Sketch a schematic plot the output optical power P_o versus input current I . Sketch a schematic plot of wall plug efficiency η_{WP} versus applied voltage V . (Note: a schematic plot means that no numbers need to be present on the two graph axes; the plot should show a qualitative trend.)