Prob. 4.8

:

Engineering stress G=E/3 for rubber

sigma[e]:=G*(lambda-(1/lambda^2));

$$\boldsymbol{\sigma}_{e} := G\left(\lambda - \frac{1}{\lambda^{2}}\right)$$

True stress:

sigma[t]:=sigma[e]*lambda;

$$\sigma_t := G\left(\lambda - \frac{1}{\lambda^2}\right)\lambda\tag{1}$$

Set *G*=1 and plot to investigate the nature of this function: G:=1;plot(sigma[t],lambda=0..10);



This function has no tangents, and thus will not form a neck.

We can also examine the Considere condition mathematically, which states that necking occurs when

$$\frac{\sigma_t}{\lambda} \ge \frac{d\sigma_t}{d\lambda}$$

Using Eq (1) above for σ_t , this gives

$$\lambda + \frac{2}{\lambda^2} \le 0$$

But for λ positive this never occurs, so necking cannot occur either.