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5.111 Principles of Chemical Science Fall 2008

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5.111 Lecture Summary #17

Readings for today: Section 7.1 – Spontaneous Change, Sections 7.2 and 7.8 – Entropy, Sections 7.12, 7.13, and 7.15 – Free Energy.

Read for Lecture #18: Section 7.16 – Free-Energy Changes in Biological Systems. (Assigned sections in chapter 7 are the same for the 3rd and the 4th ed.

Topics: Thermodynamics I. Enthalpies of reactions: calculating ΔH_r° (continued from Lecture #16) II. Spontaneous change and free energy III. Entropy IV. Free energy of formation

Clicker question: review of hybridization



I. ENTHALPIES OF CHEMICAL REACTIONS (continued from Lecture #16) **USING HESS'S LAW TO CALCULATE** ΔH_r

Enthalpy is a "STATE" FUNCTION, which means ΔH is ______ of path.

Enthalpy

$$\begin{array}{c}
6 C_{gr} + 6 H_2 + 3 O_2 + 6 O_2 \\
-\Delta H^{\circ}_{f} = +1260. \text{ kJ/mol} \\
\text{decomposition of glucose to its} \\
\text{elements}
\end{array}$$
formation of 6 CO₂

$$\Delta H^{\circ}_{f} = 6(-393.5) = -2,361 \\
6 CO_2 + 6H_2 + 3O_2 \\
\hline
\Delta H^{\circ}_{f} = 6(-285.8) = -1715$$

Hess's Law: If two or more chemical equations are added to give another chemical equation, corresponding _____ must be added.

 ΔH° for glucose oxidation (all values in kJ):

$$\Delta H_{r}^{\circ}$$

$$C_{6}H_{12}O_{6} + 6O_{2} \longrightarrow 6C_{gr} + 6H_{2} + 3O_{2} + 6O_{2}$$

$$6\left[C_{gr} + O_{2} \longrightarrow CO_{2}\right]$$

$$6\left[H_{2} + 1/2O_{2} \longrightarrow H_{2}O\right]$$

$$\overline{C_{6}H_{12}O_{6} + 6O_{2}} \longrightarrow 6CO_{2} + 6H_{2}O \quad \Delta H^{\circ} =$$

We have covered 3 methods (so far) to calculate Δ Hr°:

1) _____ enthalpies (
$$\Delta H \text{ or } \Delta H_B$$
)
 $\Delta H_r^{\circ} = \Sigma \Delta H_B$ (_____) - $\Sigma \Delta H_B$ (_____)

2) Standard enthalpies of formation (_____)

 $\Delta H_{\rm r}^{\rm o} = \Sigma \Delta H_{\rm f}^{\rm o} (\underline{\qquad}) - \Sigma \Delta H_{\rm f}^{\rm o} (\underline{\qquad})$

3) Hess's law

*** END OF EXAM #2 MATERIAL ***

II. SPONTANEOUS CHANGE AND FREE ENERGY

A **spontaneous change** is a process that, given enough time, occurs without the need for outside intervention.

For example, the following reactions are spontaneous at constant pressure:

 $4Fe(s) + 3O_2(g) \rightarrow 2Fe_2O_3(s) \qquad \Delta H^\circ = \underline{\qquad } kJ/mol$ $H_3O^+(aq) + OH^-(aq) \rightarrow 2H_2O(l) \qquad \Delta H^\circ = \underline{\qquad } kJ/mol$



But so are these ...

 $H_2O(s) \rightarrow H_2O(l)$ $\Delta H^\circ = +6.95 \text{ kJ/mol}$

 $NH_4NO_3(s) \rightarrow NH_4^+(aq) + NO_3^-(aq)$

Is ΔH the key to spontaneity? _____!

Condition for spontaneity under constant P + T involves GIBBS FREE ENERGY, ΔG .

$\Delta G = \Delta H - T \Delta S$

where T = temperature and Δ S = change in entropy, a measure of disorder.

 $\Delta H^{\circ} = +28 \text{ kJ/mol}$

Under constant pressure and temperature, a process is spontaneous when $\Delta G < 0$, not necessarily when $\Delta H < 0$. Why?

 $\Delta G = \Delta H - T \Delta S$ Useful work or Amount of reaction FREE energy energy that gets "stuck"

Figuring this out was one of the towering achievements of thermodynamics!!

 ΔG° is negative, even though ΔH° is positive. The reaction is **spontaneous**.

Now consider glucose oxidation at room temperature:

$$C_6H_{12}O_6 + 6O_2 \rightarrow 6CO_2 + 6H_2O$$

$$\Delta H^\circ = -2,816 \text{ kJ/mol}, \quad \Delta S^\circ = +233 \text{ J/K} \bullet \text{mol}$$

 $\Delta G^{\circ} = \underline{\qquad} - 298(\underline{\qquad}) = \underline{\qquad} kJ/mol$

 ΔG° more negative than ΔH° . This reaction is spontaneous at ______ temperatures.

III. ENTROPY

Entropy, S, is a measure of the ______ of a system. ΔS = change in entropy. ΔS is a state function.

 ΔS° positive \Rightarrow ______ in disorder

 ΔS° negative \Rightarrow ______ in disorder

Disorder of gas ____ liquid ____ solid In solids, molecules cannot move around freely- they are locked in ordered locations.

Internal degrees of freedom – e.g. multiple molecular configurations, many quantum states that can be occupied - also contribute to entropy

Without calculations, we can predict the sign of ΔS for many reactions. For example,

 $2H_2O_2(l) \rightarrow 2H_2O(l) + O_2(g)$ has a _____ ΔS .

Entropy for reactions, ΔS_r°

can be calculated from absolute entropies of products and reactants,

 $\Delta S_r^{\circ} = \Sigma S^{\circ}(\underline{\qquad}) - \Sigma S^{\circ}(\underline{\qquad})$

where S° is the absolute standard entropy.

Unlike E or H, where the zero can be selected, S has an absolute zero – the perfect crystal at T = 0 K (perfectly ordered, no disorder at all).

For example, consider the decomposition of hydrogen peroxide.

$$2H_2O_2(l) \rightarrow 2H_2O(l) + O_2(g)$$

$$\Delta S_r^{\circ} = \Sigma S^{\circ}(\text{products}) - \Sigma S^{\circ}(\text{reactants})$$

$$\Delta S^{\circ} = \underline{S^{\circ}(\underline{}) + S^{\circ}(\underline{}) - \underline{S^{\circ}(\underline{})}$$

$$\Delta S^{\circ} = 2(70. \text{ JK}^{-1}\text{mol}^{-1}) + (205 \text{ JK}^{-1}\text{mol}^{-1}) - 2(110. \text{ JK}^{-1}\text{mol}^{-1})$$

$$\Delta S^{\circ} = \underline{J}K^{-1}\text{mol}^{-1}$$

Why is ΔS° positive? The reaction converts liquid \rightarrow liquid and gas.

 $\begin{array}{l} \Delta G^{\circ} &= \Delta H^{\circ} - T \Delta S^{\circ} \\ &= -196 \ kJ/mol - 298.15 \ K \ (____ kJ \ K^{-1}mol^{-1}) \\ &= -233 \ kJ/mol \qquad (The reaction is ____) \end{array}$

Now consider ice melting at 298.15 K. $H_2O(s) \rightarrow H_2O(l)$

 $\Delta S^{\circ} = S^{\circ}(___) - S^{\circ}(___) = 69.91 - 41.32$ $\Delta S^{\circ} = 28.59 \text{ J K}^{-1} \text{ mol}^{-1}$ Why is $\Delta S^{\circ} > 0$?

 $\Delta G^{\circ} = 6.95 - 298.15 \text{K}(2.859 \text{ x } 10^{-2} \text{ kJ/K mol})$ = -1.57 kJ/mol Ice melting is spontaneous at room temperature even though ΔH° is positive.

IV. FREEE ENERGY OF FORMATION, ΔG_f

analogous to ΔH_{f}

 ΔG_{f}^{o} = standard Gibbs free energy of formation

= ΔG_r^{o} for formation of 1 mol of compound from its elements in their most stable form in the standard states at P = 1 bar and T = 298.15 K.

Tabulated for many compounds like ΔH_{f}^{o} , but can also be calculated from

 $___ - T\Delta S^{\circ}$

For example,

 $\Delta G^{\circ} = -394.36 \text{ kJ/mol} = \Delta G_{f}^{\circ}$

 ΔG_{f}^{o} is important because it is a measure of a compound's stability relative to its elements.

If $\Delta G_f^{\circ} < 0$, a compound is thermodynamically ______ relative to its elements. If $\Delta G_f^{\circ} > 0$, a compound is thermodynamically ______ relative to its elements.

 $\begin{array}{ll} 6C(gr) + 3H_2(g) \rightarrow C_6H_6(l) & \Delta G_f^{\,o} = 124 \ kJ/mol \\ C_6H_6(l) \rightarrow 6C(gr) + 3H_2(g) & \Delta G^o = -124 \ kJ/mol \end{array}$

The reverse reaction is spontaneous, but very, very slow!

Free energy tells whether or not a reaction will happen spontaneously, but it tells us _______ about the rate of the reaction (for rate information we need chemical kinetics).

To calculate ΔG° for a reaction...

 $\Delta G_r^{\circ} = \Sigma \Delta G_f^{\circ}(\text{products}) - \Sigma \Delta G_f^{\circ}(\text{reactants})$

OR $\Delta G_r^{\circ} = \Delta H_r^{\circ} - T \Delta S_r^{\circ}$