### 5.73

## Quiz 5

$$
\begin{aligned}
& \delta(a(x-b))=\frac{1}{|a|} \delta(x-b) . \\
& \delta(g(x))=\sum_{i}\left|\frac{d g\left(x_{i}\right)}{d x}\right|^{-1} \delta\left(x-x_{i}\right) ; x_{i} \text { are zeroes of } g(x) . \\
& \delta^{\prime}(x-d) \text { means derivative of } \delta \text {-function evaluated at } x=\mathrm{d} . \\
& \text { Infinite box of width L: } E_{n}=\frac{n^{2} h^{2}}{8 m L^{2}}, k_{n}= \pm \frac{n \pi}{L}, n=1,2, \ldots \\
& \hline
\end{aligned}
$$

1. $f(x)=(x-3)(4 x+8)$
A. Evaluate $\int \delta(x-d) f(x) d x$.
B. Evaluate $\int \delta^{\prime}(x-d) f(x) d x$.
C. Express $\delta(f(x))$ in terms of $\delta\left(x-x_{i}\right)$.
2. Density of States.
A. Compute $\frac{d n}{d k}$.
B. Compute $\frac{d n}{d E}$.

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