6.012 - Microelectronic Devices and Circuits

# Lecture 7 - Bipolar Junction Transistors - Outline

• Announcements

First Hour Exam - Oct. 7, 7:30-9:30 pm; thru 10/2/09, PS #4

# Review/Diode model wrap-up

**Exponential diode:**  $i_D(v_{AB}) = I_S (e^{qv_{AB}/kT} - 1)$  (holes) (electrons)<br/>with  $I_S \equiv A \neq n_i^2 [(D_h/N_{Dn} w_n^*) + (D_e/N_{Ap} w_p^*)]$ **Observations:** Saturation current,  $I_S$ , goes down as doping levels go up<br/>Injection is predominantly into more lightly doped side**Asymmetrical diodes:** the action is on the lightly doped side**Diffusion charge stores; diffusion capacitance:** (Recitation topic)<br/>Excess carriers in quasi-neutral region = Stored charge

### Bipolar junction transistor operation and modeling Bipolar junction transistor structure Qualitative description of operation: 1. Visualizing the carrier fluxes (using npn as the example) 2. The control function

3. Design objectives

**Operation in forward active region,**  $v_{BE} > 0$ ,  $v_{BC} < 0$ :  $\delta_{E}$ ,  $\delta_{B}$ ,  $\beta_{F}$ ,  $I_{ES}$ 

#### **Biased p-n junctions:** current flow, cont.



Asymmetrically doped junctions: an important special case

**Current flow impact/issues** 

A p+-n junction (N<sub>Ap</sub> >> N<sub>Dn</sub>):

$$i_{\rm D} = \mathrm{Aqn}_{\rm i}^2 \left[ \frac{D_h}{N_{Dn} w_{n,eff}} + \frac{D_e}{N_{Ap} w_{p,eff}} \right] \left[ e^{q_{\rm V_{AB}}/kT} - 1 \right] \approx \mathrm{Aqn}_{\rm i}^2 \frac{D_h}{N_{Dn} w_{n,eff}} \left[ e^{q_{\rm V_{AB}}/kT} - 1 \right]$$

Hole injection into n-side

An n+-p junction (N<sub>Dn</sub> >> N<sub>Ap</sub>):  

$$i_{\rm D} = {\rm Aqn}_{\rm i}^{2} \left[ \underbrace{\frac{D_{b}}{N_{Dn}w_{n,eff}}}_{N_{Ap}w_{p,eff}} + \frac{D_{e}}{N_{Ap}w_{p,eff}} \right] \left[ e^{q_{\rm V_{AB}}/kT} - 1 \right] \approx {\rm Aqn}_{\rm i}^{2} \frac{D_{e}}{N_{Ap}w_{p,eff}} \left[ e^{q_{\rm V_{AB}}/kT} - 1 \right]$$
Electron injection into p-side

Note that in both cases the minority carrier injection is predominately into the lightly doped side.

Note also that it is the doping level of the more lightly doped junction that determines the magnitude of the current, and as the doping level on the lightly doped side decreases, the magnitude of the current increases.

Two very important and useful observations!!

## **Biased p-n junctions:** excess minority carrier (diffusion) charge stores **Diffusion charge store, and diffusion capacitance**:

Using example of asymmetrically doped p+-n diode



Notice that the stored positive charge (the excess holes) and the stored negative charge (the excess electrons) occupy the same volume in space (between  $x = x_n$  and  $x = w_n$ )!

$$q_{A,DF}(v_{AB}) = Aq[p'(x_n) - p'(w_n)]\frac{[w_n - x_n]}{2} \approx Aq\frac{n_i^2}{N_{Dn}}[e^{qv_{AB}/kT} - 1]\frac{w_{n,eff}}{2}$$

The charge stored depends non-linearly on  $v_{AB}$ . As we did in the case of the depletion charge store, we define an incremental linear equivalent <u>diffusion capacitance</u>,  $C_{df}(V_{AB})$ , as:

$$C_{df}(V_{AB}) \equiv \left. \frac{\partial q_{A,DF}}{\partial v_{AB}} \right|_{v_{AB} = V_{AB}} \approx A \frac{q^2}{2kT} w_{n,eff} \frac{n_i^2}{N_{Dn}} e^{qv_{AB}/kT}$$

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A very useful way to write the diffusion capacitance is in terms of the bias current, I<sub>D</sub>:

$$I_D \approx Aqn_i^2 \frac{D_h}{N_{Dn}w_{n,eff}} \left[ e^{qV_{AB}/kT} - 1 \right] \approx Aqn_i^2 \frac{D_h}{N_{Dn}w_{n,eff}} e^{qV_{AB}/kT} \text{ for } V_{AB} \gg kT$$

To do this, first divide  $C_{df}$  by  $I_D$  to get:

$$\frac{C_{df}(V_{AB})}{I_D(V_{AB})} \approx \frac{\frac{q^2}{2kT} w_{n,eff}}{\frac{2kT}{N_{Dn}}} \frac{\frac{m_i}{N_{Dn}} e^{\frac{qV_{AB}}{kT}}}{\frac{1}{N_{Dn}} e^{\frac{qV_{AB}}{kT}}} = \frac{q w_{n,eff}^2}{2kT D_h}$$

**Isolating C**<sub>df</sub>, we have:

$$C_{df}(V_{AB}) \approx \frac{w_{n,eff}^2}{2D_h} \frac{q I_D(V_{AB})}{kT}$$

\* Notice that the area of the device, A, does not appear explicitly in this expression. Only the total current!

#### <u>Comparing charge stores; small-signal linear equivalent capacitors:</u>



only accounting for the charge store on the lightly doped side.

$$(V_{AB}) \approx \frac{w_{n,eff}^2}{2D_h} \frac{q I_D(V_{AB})}{kT}$$

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-Wn

### p-n diode: large signal model including charge stores



 q<sub>AB</sub>: Excess carriers on p-side + excess carriers on n-side + junction depletion charge.

small signal linear equivalent circuit

$$\mathbf{g}_{d} \underbrace{\mathbf{C}_{d}}_{\mathbf{D}} \left[ \begin{array}{c} \mathbf{g}_{d} = \frac{\partial i_{D}}{\partial v_{AB}} \right]_{v_{AB} = V_{AB}} \approx \begin{cases} 0 & \text{for } V_{AB} < 0 \\ \frac{qI_{D}}{kT} & \text{for } V_{AB} >> kT/q \end{cases}$$

$$C_{d}(V_{AB}) = \frac{\partial q_{AB}}{\partial v_{AB}} \Big|_{v_{AB} = V_{AB}} \approx \begin{cases} C_{dp}(V_{AB}) & \text{for } V_{AB} < 0 \\ C_{dp}(V_{AB}) + C_{df}(V_{AB}) & \text{for } V_{AB} >> kT/q \end{cases}$$

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# Moving on to <u>transistors</u>!

Amplifiers/Inverters: back to 6.002





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Lecture 7 - Slide 9 At its output each device looks like a current source controlled by the input signal.

#### How do we make a BJT?

**Basic Bipolar Junction Transistor (BJT) -** cross-section



How does it work?

Bipolar Junction Transistors: basic operation and modeling...

... how the base-emitter voltage,  $v_{BE}$ , controls the collector current,  $i_{C}$ 



A good way to envision this is to think "carrier fluxes":

Next foil



**Bipolar Junction Transistors:** the carrier fluxes through an npn

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**<u>Bipolar Junction Transistors</u>**: basic operation and modeling...

... how the base-emitter voltage,  $v_{BE}$ , controls the collector current,  $i_{C}$ 



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**Bipolar Junction Transistors:** basic operation and modeling...

... how the base-emitter voltage,  $v_{BE}$ , controls the collector current,  $i_{C}$ 



**<u>npn BJT</u>**: Forward active region operation,  $v_{BE} > 0$  and  $v_{BC} \le 0$ 





The emitter current, i<sub>F</sub>

Begin with the good current, the electron current into the base, i<sub>eE</sub>:

$$i_{eE} = -Aqn_i^2 \frac{D_e}{N_{AB} w_{B,eff}} \left[ e^{qV_{BE}/kT} - 1 \right]$$

Next find the bad current, the hole current back into the emitter, i<sub>hE</sub>:

$$i_{hE} = -Aqn_i^2 \frac{D_h}{N_{DE} w_{E,eff}} \left[ e^{qV_{BE}/kT} - 1 \right]$$

and write it as a fraction of i<sub>eF</sub>:

$$i_{hE} = \frac{N_{AB} w_{B,eff}}{D_e} \frac{D_h}{N_{DE} w_{E,eff}} \quad i_{eE} = \delta_E i_{eE}$$

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We'll define  $\delta_{F}$  on the next foil.



The emitter current,  $i_E$ , cont. In writing the last equation we introduced the <u>emitter defect</u>,  $\delta_F$ :

$$\delta_E = \frac{i_{hE}}{i_{eE}} = \frac{D_h}{D_e} \cdot \frac{N_{AB}}{N_{DE}} \cdot \frac{w_{B,eff}}{w_{E,eff}}$$

To finish for now with the emitter current, we write it,  $i_E$ , in terms of the emitter electron current,  $i_{eE}$ :

$$i_E = i_{eE} + i_{hE} = \left(1 + \frac{i_{hE}}{i_{eE}}\right)i_{eE} = \left(1 + \delta_E\right)i_{eE}$$

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The collector current, i<sub>c</sub>

The collector current is the electron current from the emitter,  $i_{eE}$ , minus the fraction that recombines in the base,  $\delta_B i_{eE}$ :

$$i_C = \left(1 - \delta_B\right) i_{eE}$$

To find the fraction that recombine, i.e. the <u>base defect</u>,  $\delta_B$ , we note that we can write the total recombination in the base,  $\delta_B i_{eE}$ , as:

$$\delta_B i_{eE} = -A q \int_0^{w_B} \frac{n'(x)}{\tau_{eB}} dx$$

#### The base defect, $\delta_B$

If the recombination in the base is small (as it is in a good BJT) then the excess electron concentration will be nearly triangular and we can say:

$$\int_{0}^{w_{B}} n'(x) dx \approx \frac{n'(0)w_{B,eff}}{2} \quad \text{and} \quad i_{eE} \approx -Aq D_{eB} \frac{n'(0)}{w_{B,eff}}$$

Thus 
$$\delta_{B} = \frac{-Aq \int_{0}^{w_{B}} \frac{n'(x)}{\tau_{eB}} dx}{i_{eE}} \approx \frac{-Aq \frac{n'(0)w_{B,eff}}{2\tau_{eB}}}{-Aq D_{eB} \frac{n'(0)}{w_{B,eff}}} = \frac{w_{B,eff}^{2}}{2D_{eB} \tau_{eB}} = \frac{w_{B,eff}^{2}}{2L_{eB}^{2}}$$

The collector current, i<sub>c</sub>, cont.

Returning to the collector current, i<sub>c</sub>, we now want to relate it to the total emitter current:

$$\begin{aligned} i_{C} &= -(1 - \delta_{B})i_{eE} \\ i_{E} &= (1 + \delta_{E})i_{eE} \end{aligned} \} \quad i_{C} &= -\frac{(1 - \delta_{B})}{(1 + \delta_{E})}i_{E} = -\alpha_{F}i_{E} \\ \text{with} \quad \alpha_{F} &\equiv \frac{(1 - \delta_{B})}{(1 + \delta_{E})} \end{aligned}$$

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So far...  
We have: 
$$i_E = -Aqn_i^2 \left( \frac{D_h}{N_{DE}w_{E,eff}} + \frac{D_e}{N_{AB}w_{B,eff}} \right) \left[ e^{qV_{BE}/kT} - 1 \right]$$
  
 $= -I_{ES} \left[ e^{qV_{BE}/kT} - 1 \right]$  with  $I_{ES} = Aqn_i^2 \left( \frac{D_h}{N_{DE}w_{E,eff}} + \frac{D_e}{N_{AB}w_{B,eff}} \right)$   
...and we have:

$$i_C \propto i_E$$
:  $i_C = -\alpha_F i_E$  with  $\alpha_F \equiv -\frac{i_C}{i_E} = \frac{(1-\delta_B)}{(1+\delta_E)}$ 

These relationships can be represented by a simple circuit model:

$$i_{E} = -i_{F} \text{ with } i_{F} = I_{ES} \left( 1 - e^{qv_{BE}/kT} \right)$$

$$i_{C} = \alpha_{F}i_{F} \text{ with } \alpha_{F} \equiv -\frac{i_{C}}{i_{E}} = \frac{\left( 1 - \delta_{B} \right)}{\left( 1 + \delta_{E} \right)}$$

$$i_{B} = -i_{E} - i_{C} = \left( 1 - \alpha_{F} \right)i_{F}$$

$$I_{O} = \alpha_{F}i_{F} + i_{C} = \left( 1 - \alpha_{F} \right)i_{F}$$

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B

Note:

0-+

V



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**<u>npn BJT</u>**: What our model tells us about device design.

We have:

$$\alpha_F = \frac{\left(1 - \delta_B\right)}{\left(1 + \delta_E\right)}$$

and the defects,  $\delta_{\text{E}}$  and  $\delta_{\text{B}},$  are given by:

$$\delta_E = \frac{D_h}{D_e} \cdot \frac{N_{AB}}{N_{DE}} \cdot \frac{w_{B,eff}}{w_{E,eff}}$$
 and  $\delta_B \approx \frac{w_{B,eff}^2}{2L_{eB}^2}$ 

We want  $\alpha_F$  to be as close to one as possible, and clearly the smaller we can make the defects, the closer  $\alpha_F$  will be to one. Thus making the defects small is the essence of good BJT design:

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Doping: npn with 
$$N_{DE} >> N_{AB}$$
  
 $w_{B,eff}$ : very small  
 $L_{eB}$ : very large and  $>> w_{B,eff}$ 

<u>npn BJT</u>: Well designed structure (Large  $β_F$ , small  $δ_E$  and  $d_B$ )  $δ_E$  and  $\delta_B$  are small and  $α_F$  is ≈ 1 when  $N_{DE} >> N_{AB}$ ,  $w_E << L_{hE}$ ,  $w_B << L_{eB}$ 



#### npn BJT,cont.: more observations about F.A.R. model

It is very common to think of  $i_B$ , rather than  $i_E$ , as the controlling current in a BJT. In this case we write  $i_C$  as depending on  $i_B$ :

Two circuit models that fit this behavior are the following:





#### **<u>npn BJT</u>**: Equivalent FAR models





### npn BJT: The Ebers-Moll model

The forward model is what we use most, but adding the reverse model we cover the entire range of possible operating conditions.



You are not responsible for this model.

### **npn BJT:** The Gummel-Poon model

Another common model can be obtained from the Ebers-Moll model is the Gummel-Poon model:



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You even less responsible for this model.

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Lecture 7 - Bipolar Junction Transistors - Summary

- Review/Junction diode model wrap-up Refer to "Lecture 6- Summary" for a good overview Diffusion capacitance: adds to depletion capacitance (p<sup>+</sup>-n example) In asym., short-base diodes: C<sub>df</sub>(V<sub>AB</sub>) ≈ (qI<sub>D</sub>/kT)[(w<sub>n</sub>-x<sub>n</sub>)<sup>2</sup>/D<sub>h</sub>] (area doesn't enter expression!)
- Bipolar junction transistor operation and modeling



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