$\qquad$

# Massachusetts Institute of Technology <br> Department of Nuclear Science and Engineering Department of Electrical Engineering and Computer Science 

22.071/6.071 - Introduction to Electronics, Signals and Measurement Spring 2006

Final Exam

- Please write your name on each page of the exam in the space provided
- Please verify that there are 26 pages in your exam.
- To the extent possible, do your work for each question within the boundaries of the question or on the back side of the page preceding the question. Extra pages are also provided for computation.
- Note that the total number of points is 100 .
- Closed book. No Calculators
- Partial credit adds up so make sure that you show your work.

| Problem | Points |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |
| Total |  |

Name: $\qquad$

## General Useful Information

Diodes:

| Ideal diode model | Id <br> Reverse-Bias <br> Region |  |
| :---: | :---: | :---: |
| 0.7 Volt offset model | $\qquad$ |  |
| Full diode model $I d=I s\left[\exp \left(\frac{V d}{V_{T}}\right)-1\right]$ $V_{T} \simeq 25 \mathrm{mV}$ |  |  |
| Zener Diode <br> Ideal model |  |  |

## Reactive Elements:

| Capacitor $\begin{aligned} & \mathrm{I}_{\mathrm{c}}=\mathrm{C} \frac{\mathrm{dV}}{\mathrm{c}} \\ & \mathrm{dt} \\ & Z_{C}=-\frac{j}{\omega C} \end{aligned}$ |  |
| :---: | :---: |
| $\begin{array}{ll} \hline \text { Inductor } & \\ \qquad & V_{\mathrm{L}}=\mathrm{L} \frac{\mathrm{dI}_{\mathrm{L}}}{\mathrm{dt}} \\ Z_{L}=j \omega L \end{array}$ | $1: \mathrm{An}_{\mathrm{L}}^{\mathrm{L}} \text {. }$ |

Name: $\qquad$

## General Useful Information

Op-Amps

| Ideal Op-amp model (negative feedback) |
| :---: |
| $\mathrm{I}+=\mathrm{I}-=0$ <br> $\mathrm{~V}+=\mathrm{V}-$ |
| Ideal 3 state op-amp model (open loop and positive <br> feedback) |
| $\mathrm{I}+=\mathrm{I}-=0$ |

BJTs


## Boolean Identities

| $\mathrm{A}+0=\mathrm{A}$ | $\mathrm{A} \bullet 1=\mathrm{A}$ |
| :---: | :---: |
| $\mathrm{A}+\mathrm{B}=\mathrm{B}+\mathrm{A}$ | $\mathrm{AB}=\mathrm{BA}$ |
| $\mathrm{A}+(\mathrm{B}+\mathrm{C})=(\mathrm{A}+\mathrm{B})+\mathrm{C}$ | $\mathrm{A}(\mathrm{BC})=(\mathrm{AB}) \mathrm{C}$ |
| $\mathrm{A}+\mathrm{BC}=(\mathrm{A}+\mathrm{B})(\mathrm{A}+\mathrm{C})$ | $\mathrm{A}(\mathrm{B}+\mathrm{C})=\mathrm{AB}+\mathrm{AC}$ |
| $\mathrm{A}+\mathrm{A}=\mathrm{A}$ | $\mathrm{A} \bullet \overline{\mathrm{A}}=0$ |
| $\mathrm{~A}+1=1$ | $\mathrm{~A} \bullet \mathrm{~A}=\mathrm{A}$ |
| $\mathrm{A}+\overline{\mathrm{A}}=1$ | $\mathrm{~A} \bullet 0=0$ |
| $\mathrm{~A}+\mathrm{AB}=\mathrm{A}$ | $\mathrm{A}(\mathrm{A}+\mathrm{B})=\mathrm{A}$ |
| $\mathrm{A}+\overline{\mathrm{A}} \mathrm{B}=\mathrm{A}+\mathrm{B}$ | $(\mathrm{A}+\mathrm{B})(\mathrm{A}+\mathrm{C})=\mathrm{A}+\mathrm{B} \mathrm{C}$ |
| $\overline{\mathrm{AB}}=\overline{\mathrm{A}}+\overline{\mathrm{B}}$ | $\overline{\mathrm{A}+\mathrm{B}}=\overline{\mathrm{A}} \bullet \overline{\mathrm{B}}$ |

Name:

## Problem 1 - (10 points)

The op-amp in the following circuit outputs a current of 5 mA . ( $I o=5 \mathrm{~mA}$ ). The transistor has $\beta=100$. Calculate the value of the resistor $R$.


Name:

Problem 2 - (10 points)
In this circuit the op-amp may be considered to be ideal and it is not saturated. It drives a load of unspecified resistance.

A. Approximately what is the voltage $V_{+}$?
B. What is the voltage $V$ ?
C. Therefore, what is the current $i_{L}$ and what is the purpose of this circuit?
D. If R 1 is increased by a factor $\exp (1)$, what is the expected change in $i_{L}$ ? (Hint: use the I-V characteristic relationship for a diode)

Name:

## Problem 3-(10 points)

In this circuit $R 1=100 \mathrm{k} \Omega, R 2=25 \mathrm{k} \Omega, R c=25 \mathrm{k} \Omega, R e=5 \mathrm{k} \Omega, C=1 \mu \mathrm{~F}$ and the $\beta$ of the transistor at its DC operating point is 100 .

A. If $I b$ is negligible, what is the steady state (DC) value of $V b$ ?
B. In that case, using a standard simplified model of the transistor, determine the DC values of $V c$ and $V e$.

Name:
C. Estimate the DC value of $I b$ in that case
D. If this value of $I b$ is accounted for in calculating $V b$, then how much does it change from your answer in A?
E. Approximately what is the time constant of the high-pass filter made up by $C$ and the rest of the circuit?
F. For AC signal frequencies well above the high-pass cut-off, what are the small signal voltage gains of the circuit at the outputs i.e. vc/vi and ve/vi?

Name: $\qquad$

## Problem 4 - (10 points)

Here you will analyze the following circuit.


This circuit combines two logic gates (NOR and NOT) and an RC network.
Assume that the logic gates are ideal: no delay time between the output and the input and the output swings between 0 and $V_{D D}$. Furthermore the voltage transfer characteristic of the inverter gate (NOT) is:



Also assume that the diode is ideal with the following Id-Vd characteristic curve.


We will apply a trigger pulse $V_{i}$ and arrange our circuit parameters so that the output $V_{\text {out }}$ is a pulse of specified duration.

Name: $\qquad$

We will solve this problem by breaking it down into small parts, analyze each part and then put it all together for the final answer.
A. Fill in the truth table for the NOR gate

| $\begin{aligned} & A \longrightarrow 0-Y \\ & B \longrightarrow 0 \end{aligned}$ |  |  |
| :---: | :---: | :---: |
| A | B | Y |
| 0 | 0 |  |
| 0 | $V_{D D}$ |  |
| $V_{D D}$ | 0 |  |
| $V_{D D}$ | $V_{D D}$ |  |

B. Now let's independently consider the $R C$ network in order to explore its general characteristics. The voltage $V_{l}$ has the form shown on the graph below. It has been at $V_{D D}$ Volts for a very long time and then at time $=0$ goes to zero Volts, returning to $V_{D D}$ at time $t_{l}$.


What is the voltage $V_{2}$ at time $=0$ ?

What is the voltage $V_{2}$ at time $=0^{+}$?

Give an expression for the voltage $V_{2}$ for time $\geq 0$

Name: $\qquad$

Assuming that $t_{1}=R C \ln (2)$, what is the voltage $V_{2}$ at time $=t_{l}{ }^{+}$? (Hint: the voltage across the capacitor is $V_{2^{-}} V_{1}$ )
C. Draw the complete evolution for $V_{2}$.

$\qquad$
D. Now let's connect a diode to the $R C$ circuit as shown below. Draw the evolution of $V_{2}$ in this case.

E. Now connect the NOT gate as shown below. With the given voltage transfer characteristic for the inverter gate and for $t_{1}=R C \ln (2)$ draw the evolution of the output voltage $V_{\text {out }}$. Indicate relevant transition times and values.


Name: $\qquad$
F. Now let's put it all together. The complete circuit is reproduced here for your convenience.


The signal $V_{i}$ is a pulse as shown below. Draw the form of the voltage $V_{1}, V_{2}$, and $V_{\text {out. }}$ Indicate all relevant transition times and values.


Name: $\qquad$

Problem 5-(10 points)

This circuit explores the principles of signal measurement using bridge circuits and opamps.


You should recognize that the resistor network enclosed by the dotted rectangle is a Wheatstone bridge. In practice such a bridge may be used in performing strain-gauge or temperature measurements.

Here we have two such strain-gauges whose resistance is given by $R+\Delta R . R$ is the unstrained resistance and $\Delta R$ represents the change in resistance due the loading of the structure that the gauge is attached to. We will analyze this circuit in steps in order to eventually calculate the voltage $V_{O}$ at the output of op-amp OA2.
A. What is the voltage $V_{l}$ ?
B. What is the current $l$ ?

Name:
C. Write an expression for the voltages $V_{2}$ and $V_{3}$. (Assume that the resistance $R_{2} \gg 2 R+R_{1}$ )
D. What is the voltage $V_{+}$?
E. What is the voltage $V$ ?
F. Calculate the voltage $V_{O}$

Name:

## Problem 6 - (10 points)

The Load in this circuit is powered by $V C c$ and the maximum current through it is determined by the maximum current that can be provided the BJT. The BJT has $\beta=100$ and a maximum continuous collector current of 50 mA . The voltage, $V b$, at the base of the BJT varies between 0 and 5.7 Volts as indicated.

A. For $V c c=10.2$ Volts, determine the value of the load resistance $R_{L}$ and the emitter resistor $R$ so that the BJT operates in the active region and the current constraint is not violated (i.e. Vce $\geq 0.2$ Volts and $I c \leq 50 \mathrm{~mA}$ ).
$\qquad$
B. Egatlov's cousin, N.Rub, who went to some school on the west coast, wanted to drive a motor and he used the arrangement shown below. The control voltage Vb is a square wave of $50 \%$ duty cycle ranging from 0 to 5.7 Volts.

N.Rub, was careful to limit the current though the BJT by appropriately selecting resistor $R$ and now he was ready to turn it on by closing switch $S$.

As soon as N.Rub closed the switch, the motor started to turn and immediately it stopped! He checked $V b$ and $V c c$, double checked the resistor value for $R$ and everything seemed to be OK.

He closed the switch again but now nothing happened. He replaces the BJT and the motor, closes the switch and again and the motor makes a few turns and it stops.
N.Rub had no idea what to do next. He asks his coworker Edoid for help. Edoid, who actually took 6.071 , looks at the circuit, skims the data sheet of the BJT and the motor and says:

Well, you are trying to drive an inductive load and thus every time you activate the circuit, the maximum voltage rating of the BJT is exceeded destroying the transistor.
A solution is to place a $\qquad$ in $\qquad$ with the motor.
fill in the name

Show us how Edoid proposes to modify the circuit and give a general plot the voltages $V c$ and $V e$ for both with and without the circuit modification. (next page)

Name:



Name:

Problem 7 - (10 points)
For the following circuit:

A. What is the voltage $V_{1}$ ?
B. What is the voltage $V_{2}$ ?
C. Calculate the voltage gain $\frac{V_{o}}{V_{i}}$
D. Determine the input impedance $\operatorname{Zin}$ seen by the voltage $V_{i}$.

In this impedance inductive, capacitive or resistive?

Name: $\qquad$

Problem 8 - (10 points)
For the following circuit

A. Derive an expression for $\frac{V_{1}}{V_{i}}$
B. Derive an expression for $\frac{V_{2}}{V_{1}}$
C. Derive an expression for $\frac{V_{o}}{V_{i}}$

Name: $\qquad$
D. What is the role of:

Stage 1: $\qquad$
Stage 2: $\qquad$
Stage 3: $\qquad$
E. The frequency domain characteristics of input signal $V_{i}$ is:


For $R=10 k \Omega, C 1=0.8 n F, C 2=1.6 n F, R_{I}=10 k \Omega$ and $R_{f}=20 k \Omega$, draw the expected amplitude of the Fourier transform of $V_{o}$ on the graph below. (Hint: $\frac{1}{2 \pi} \simeq 0.16$ )


Name:

Problem 9 - (10 points)

The following circuit combines a positive feedback path to generate oscillations and negative feedback path to generate gain.

A. By considering the impedance of the elements calculate the voltage ratio $\frac{V_{+}}{V_{o}}$

Name:
B. Determine the condition for which the voltage $V_{o}$ is in phase with the voltage $V_{+}$. What is the ratio $\frac{V_{+}}{V_{o}}$ at this condition? Hint: the phase, $\phi$, of the complex number $a+j b$ is $\phi=\tan ^{-1}\left(\frac{b}{a}\right) . b=0$ gives $\phi=0$

Name:

Problem 10-(10 points)
Find the Thevenin equivalent circuit across the port $A-B$


Name:

Blank page: For computation

Name:

Blank page: For computation

Name:

Blank page: For computation

