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# Massachusetts Institute of Technology <br> Department of Nuclear Science and Engineering Department of Electrical Engineering and Computer Science 

22.071/6.071 - Introduction to Electronics, Signals and Measurement Spring 2006

Quiz 2

- Please write your name on each page of the exam in the space provided
- Please verify that there are 11 pages in your exam.
- To the extent possible, do your work for each question within the boundaries of the question or on the back side of the page preceding the question. Extra pages are also provided for computation.
- Note that the total number of points is 100 .
- Closed book. No Calculators
- Partial credit adds up so make sure that you show your work.

Name:

Problem 1 - (15 points)
What is the gain $\frac{V o}{V s}$ for the following circuit


Name:

## Problem 2-(15 points)

The circuit below operates in steady state driven by the sinusoidal source Vs.

A. Calculate the transfer function $|H(\omega)|=\left|\frac{V o}{V s}\right|$
B. Graph $|H(\omega)|$ as a function of frequency and indicate how an increase in R will affect your graph.


Name:

## Problem 3-(15 points)

For the following circuit, the capacitor C is known. The circuit operates under sinusoidal steady state conditions. Determine the value of resistors R so that the phase difference between Vo and Vs is $-\frac{\pi}{2}$. $\left(\phi_{V o}-\phi_{V s}=\frac{\pi}{2}\right)$


Name: $\qquad$

Problem 4-(10 points)

Tau finds a black box with 3 terminals labeled X, Y, Z. Tau, who took 6.071 last year, decides to make resistance measurements across the terminals at $\mathrm{DC}(\omega=0 \mathrm{~Hz})$ and at high frequency ( $\omega$ large). She observes the following results:

|  | Resistance $(\Omega)$ at |  |
| :---: | :---: | :---: |
| Measure resistance across | DC | High-Freq. |
| $\mathrm{X}-\mathrm{Y}$ | $\infty$ | 40 |
| $\mathrm{Y}-\mathrm{Z}$ | 0 | $\infty$ |
| $\mathrm{X}-\mathrm{Z}$ | $\infty$ | $\infty$ |

Which of the following equivalent circuits is inside Tau's black box?


Circuit A


Circuit C


Circuit B


Circuit D

Name:

Problem 5-(15 points)
Find the impedance Zin across terminals $a-b$ as indicated in the following circuit


Name:

Problem 6-(15 points)


For the circuit above the current Is has the form

$$
I s(t)= \begin{cases}I_{0} & t>0 \\ 0 & t<0\end{cases}
$$

Where $I_{0}=$ constant
A. Determine the voltage $v$ at $t=0^{+}$and at $t \rightarrow \infty$
B. Determine the equivalent resistance seen by the capacitor

Name: $\qquad$

Problem 7 - ( 15 points)
The signal $\operatorname{Vs}(t)$ is applied to the circuit as indicated in the schematic below


The Fourier transform of the input signal $V s(t)$ is shown below.


The output signal $\mathrm{Y}(\mathrm{t})$ is taken across the resistor. Draw the Fourier transform of the signal $\mathrm{Y}(\mathrm{t})$ on the following graph.


Name:

Blank page: For computation

Name:

Blank page: For computation

Name:

| Problem | Points |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| Total |  |

