

Warm-Ups 05

⚠ This is a preview of the published version of the quiz

Started: Mar 4 at 12:55pm

Quiz Instructions



Question 1 2 pts

Assume you could be sure of getting a 4% annual return forever on money you invest now; in other words, every dollar invested now will grow to 1.04^k dollars k years from now.

You'd like to set up an annuity that will pay you \$10,000 every year, forever, starting a year from now. Which of the following expresses the minimum amount you would need to invest now? In other words, what is the sum of all of these annual \$10,000 payouts, after converting each one to the equivalent value today?



$$\sum_{k=1}^{\infty} 10000 \cdot (1.04)^k$$



$$\sum_{k=1}^{\infty} \frac{10000}{(1.04)^k}$$



\$20,000



Impossible. Even with 4% annual growth, no annuity can provide that much value indefinitely.



Question 2 2 pts

Use the formula for the sum of a geometric series (Theorem 14.1.1) to evaluate the sum in the previous problem. What is the required investment? Careful: the formula in Theorem 14.1.1 starts at $i=0$, but our sum starts at $k=1$.



\$240,000



\$250,000



\$260,000



\$20,000



Question 3 3 pts

Let $f : \mathbb{R}^+ \rightarrow \mathbb{R}^+$, and define the sum $s = \sum_{k=1}^n f(k)$ and the integral $i = \int_1^n f(x) dx$.

If f is weakly increasing, what lower and upper bounds do we get for s from the integral method?

[Select]
▼

 $\leq s \leq$

[Select]
▼

If f is weakly decreasing, what lower and upper bounds do we get for s from the integral method?

[Select]
▼

 $\leq s \leq$

[Select]
▼



Question 4 3 pts

Let $s = \sum_{n=1}^{57} \frac{1}{\sqrt[3]{n+7}}$. Given that $\int_1^{57} \frac{1}{\sqrt[3]{x+7}} dx = 18$, what lower and upper bounds does the integral method provide on the sum s ?

Lower bound:

[Select]
▼

Upper bound:

[Select]
▼

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6.1200J Mathematics for Computer Science
Spring 2024

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