## Agenda

$\approx$ Hodge Podge of Vision Stuff
\& Stereo Vision
$\&$ Rigid body motion

* Edge Detection
\& Optical Flow
\& EM Algorithm to locate objects
$\approx$ May not be directly applicable, but we've tried to make it relevant.


## Stereo Vision

*We can judge distance based on the how much the object's position changes.


Left Eye Right Eye


Right Image

## Stereo Vision

$\approx$ Use the image to find the angle to the object, then apply some trig:


Left Image


Right Image

angle-side-angle gives
you a unique triangle

## Stereo Vision

*What's the angle?
\& Perspective projection equation tells us
$x / f=X / Z$
$f f$ is focal length, $x$ is pixel location
$x \tan (f)=X / Z=x / f$

center of projection

## Stereo Vision

\& But in a complex image, objects may be hard to identify...
\& Try to match regions instead (block correlation)

## Stereo Vision

$\approx$ Difference metric $=$ Sum of $(\mathrm{Li}-\mathrm{Ri})^{\wedge} 2$

| 6 | 5 | 5 |
| :--- | :--- | :--- |
| 5 | 6 | 5 |
| 5 | 5 | 7 |

*Search horizontally for best match
(least difference)

| 6 | 5 | 5 |
| :--- | :--- | :--- |
| 5 | 6 | 5 |
| 1 | 1 | 6 |

## Stereo Vision

\& Still have a problem: unless the object is really close, the change might be small...


Left Eye Right Eye


Left Image


Right Image

## Stereo Vision

$\approx$ And many regions will be the same in both pictures, even if the object has moved.
$\approx$ We need to apply stereo only to "interesting" regions.


Right Image

## Stereo Vision

$\approx$ Uniform regions are not interesting
\& Patterned regions are interesting
$\approx$ Let the "interest" operator be the lowest eigenvalue of a matrix passed over the region.

| 5 | 5 | 5 |
| :--- | :--- | :--- |
| 5 | 5 | 5 |
| 5 | 5 | 4 |

lowest eigenvalue $=0$

| 8 | 5 | 2 |
| :--- | :--- | :--- |
| 5 | 1 | 5 |
| 5 | 5 | 4 |

lowest eigenvalue $=2.5$

## Stereo Vision



## Stereo Vision

\&For Maslab, the problem is simpler... can easily identify objects and compute horizontal disparity.
\& To convert disparity to distance, calibrate the trig.
\& Use two cameras... or mount a camera on a movable platform... or move your robot

## Rigid Body Motion

\& Going from data association to motion \& Given
$\&$ a starting $\mathrm{x} 1, \mathrm{y} 1, ? 1$

* a set of objects visible in both images

What is $\mathrm{x} 2, \mathrm{y} 2$, and ?2?
position one
position two

## Rigid Body Motion

\& If we only know angles, the problem is quite hard:

$\approx$ Assume distances to objects are known.

## Rigid Body Motion

\& If angles and distances are known, we can construct triangles:
distance between objects should be the same from both positions

## Rigid Body Motion

$\approx$ Apply the math for a rotation:

$$
x 1 i=\cos (?)^{*} x 2 i+\sin (?)^{*} y 2 i+x 0
$$

$$
y 1 i=\cos (?)^{\star} y 2 i-\sin (?)^{*} x 2 i+y 0
$$

$\&$ Solve for $\mathrm{xo}, \mathrm{y}$, and ? with least squares:
$\mathrm{S}\left(\mathrm{x} 1 \mathrm{i}-\cos (?)^{*} \mathrm{x} 2 \mathrm{i}-\sin (?)^{\star} \mathrm{y} 2 \mathrm{i}-\mathrm{xo}\right)^{\wedge} 2+$
(y1i - $\cos (?)^{*}$ уzi $\left.+\sin (?)^{\star} x 2 i-y 0\right)^{\wedge} 2$
$\approx$ Need at least two objects to solve

## Rigid Body Motion

$\&$ Advantages
$\approx$ Relies on the world, not on odometry
\& Can use many or few associations
\& Disadvantage
\& Can take time to compute

## Edge Detection

$\approx$ Edges are places of large change
$\star$ Scan the image with little computational molecules or a 'kernel'

| 1 |
| :---: |
| 0 |
| -1 |



## Edge Detection



## Edge Detection

* More sophisticated filters work better (Laplacian of Gaussian, for example)



## Edge Detection

\& Need to choose a good value for threshold
\& Too small—gets lots of noise, fat edges
2 Too big—lose sections of edge
$\star$ What do you do with an edge?
\& Extract lines for a map?
\& Use to separate regions?

## Optical Flow

$\approx$ Look at changes between successive images
$\&$ identify moving objects
\& identify robot motion (flow will radiate out from direction of motion)
$\approx$ For each point on image, set total derivative of brightness change to zero:
$\approx 0=u^{*} E x+v^{*} E y+E t$

## Optical flow



## Optical Flow

$\approx$ Computationally expensive and requires very fast frame rates... or very slow robots
\& Idea from optical flow: looking at change between frames can help segment an image (only edges will move).

## EM Algorithm

$*$ Given an image with k objects \& How can we find their locations?

## EM Algorithm

$\approx$ Assume there are k red objects
$\approx$ Randomly choose object locations xk, yk

* Loop:
\& Assign each pixel to nearest $\mathrm{xk}, \mathrm{yk}$
$\approx$ Recenter xk , yk at center of all pixels associated with it



## EM Algorithm

\& Key question: what is k?
$\approx$ Need to know how many objects
$\star$ Convergence criteria for random values?
$\approx$ Pick good guesses for centers

## Performance Note

$\approx$ Faster access:
\& bufferedlmage = ImageUtil.convertlmage(bufferedlmage, Bufferedlmage.INT_RGB);
\& DataBufferInt intBuffer = (DataBufferInt) bufferedlmage.getRaster().getDataBuffer();
\& int[] b = dataBufferInt.getData();
$\approx$ Need to keep track of where pixels are:
\& offset $=\left(y^{*}\right.$ width $\left.+x\right)$
\& (b[offset] >> 16) \& 0xFF = red or hue
\& (b[offset] >> 8) \& 0xFF = green or saturation
\& $\mathrm{b}[$ offset $] \& 0 x F F=$ blue or value

## Reminders

* No lecture tomorrow
$\star$ Design Review Wednesday
\& Check Point Two: Friday
\& If you haven't completed check point one, you finish it today!

