6.622 Power Electronics Prof. David Perreault Lecture 32 - Switched-Capacitor Converters 2

Consider the loss encountered in "series" charging a capacitor from a dc voltage source V_s , starting at an initial voltage v_{ci} :



The charge delivered from the source to the capacitor is

$$\Delta q = \int dq = \int_{v_{ci}}^{V_s} C dv = C(V_s - v_{ci})$$

The energy delivered to the cap is

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$$\Delta E_{source} = V_s \Delta q$$

$$= CV_s^2 - CV_s v_{ci}$$

$$\Delta E_{cap} = \int v dq = \int_{v_a}^{V_s} Cv dv$$

$$= \frac{1}{C} V_a^2 - \frac{1}{C} v_{zi}^2$$

The energy <u>lost</u> in the series charging element (e.g. rsistor) is: $\Delta E_{loss} = \Delta E_{source} - \Delta E_{cap} = \frac{1}{2}CV_s^2 - CV_s v_{ci} + \frac{1}{2}cv_{ci}^2$

$$\Delta E_{loss} = \frac{1}{2}C(V_s - v_{ci})^2$$

The energy $\underline{\text{from}}$ the source is

- Note that this loss does <u>NOT</u> depend on the resistance value or even if the resistor is linear or nonlinear!
- The charging <u>efficiency</u> is $\eta = \frac{\Delta E_{cap}}{\Delta E_{source}} = \frac{\frac{1}{2}CV_s^2 \frac{1}{2}Cv_i^2}{CV_s^2 CV_sv_{ci}}$, $\Delta v = v_s v_{ci}$, this reduces to

$$\eta = \frac{1}{2}(1 + \frac{v_{ci}}{V_s}) = 1 - \frac{1}{2}(\frac{\Delta V}{v})$$

50% @ $v_{ci} = 0{\Delta v = V_s}$ 100% as $v_{ci} \rightarrow V_s \Delta V \rightarrow 0$

 \Rightarrow we can make capacitor charging efficient by keeping $\Delta V = V_s - v_{ci}$ small! (This is key to switchedcapacitor converters)

• The only other way to make series charging from constant voltage more efficient is to introduct a series element (e.g. inductor) and use that to charge v_c to a final voltage $> V_s$. Otherwise the delivered charge limits us.

Last time we saw a simple 2:1 switched capacitor converter:



• The fact that the efficiency of v-source charging a capacitor improves with smaller $\Delta V/v \ (\eta = 1 - \frac{1}{2} \frac{\Delta V}{V_s})$ is reflected in the fact that $R_{eq} \propto \frac{1}{C_f}$

Given appropriate switch implementations, SC converters are bidirectional. Consider "turning around" the converter above:



We get the following SSL model:



• State 1: Discharge $V_{in} + v_c$ into $C_{big}@V_{out}$

• State 2: Charge up v_c to V_{in}

Notice how R_{eq} scales through the "transformer"

$$I_{out} = \frac{1}{2}I_{in} \ V_{out} = 2V_{in} - \frac{I_{out}}{fC}$$

For this converter, C_{big} must "hold up" the output voltage as it only gets current pulses in 1 of 2 (phase 1). We can fix this with "interleaving".



• By interleaving we can greatly reduce C_{big} for a given allowed ripple. (In theory we can eliminate C_{big} if we can tolerate ripple in the output voltage).

There are many other SC converter types, each with its own properties. One classic extension of the converter already shown is the "series-parallel"



Another classic design is the "ladder" converter (4:1 ladder)



- Capacitors charge (discharge) in series and discharge (charge) in parallel
- Capacitors see only $\min(V_{in}, V_{out})$ (Switches see more)
- N:1 has N-1 transfer caps, +1 output cap = N caps, 3N-2 switches
- <u>State 1</u> re-balances "flying" cap set and delivers charge from V_{in} to stack
- <u>State 2</u> rebalances rest of cap set and delivers more charge to output
- N:1 converter has 2N-2 caps +2N switches all rated for min(V_{in}, V_{out}) (This is a popular feature)
- Can generate several ratiometric voltages at once $\left(\frac{V_{in}}{4}, \frac{2V_{in}}{4}, \frac{3V_{in}}{4}\right)$

The interleaved version of this converter is very useful for multiouput conversion.

General achievable limits for 2-phase SC converters have been explored (see Makowski work).

For a number of capacitors k (including output cap but <u>not</u> input cap), we get a max conversion ratio N = f(k), where f(k) is the kth Fibonacci number, and require 3k - 2 switches.

| # Capacitors | k | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|--------------------------|----------|---|---|---|---|----|----|----|
| Max conversion ratio | N = F(k) | 1 | 1 | 2 | 3 | 5 | 8 | 13 |
| Min $\#$ of switches (m) | 3k-2 | - | 0 | 4 | 7 | 10 | 13 | 16 |

The component count limits do not tell us stresses on switches, capacitors. Different designs yield tradeoffs on how well they utilize switches, capacitors (some better for switches, some for caps), how many components of what voltage/current, etc.

In each case, we can find an equivalent circuit model comprising a transformer with rational turns ratio and an equivalent output resistance. To find these, we merely find the charge transfers in each state. [See Seeman, et al., *IEEE Trans. Power Electron.*, March 2008]

Note: If we replace many of the active switches with diodes, we get "voltage multipliers," e.g., the Cockcroft-Walton voltage multiplier is related to the ladder converter (used to generate very high voltages from a low-voltage AC input).

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There are likewise many ways to integrate <u>modest</u> amounts of magnetics to get hybrid SC/magnetic converter with interesting properties.

Consider our 2:1 step-down converter with a resonant inductor in series with the energy XFER capacitor: Resonant SC conversion



This is known as a "resonant" switched-capacitor circuit. It provides the same conversion ratio as the non-resonant version. However, instead of exponential pulses in the SC, we can switch this such that each phase (1 and 2) is $\frac{1}{2}$ a resonant cycle (or an odd multiple) and get smooth currents with ZCS switching. This gives us $FS2_{Reg}$ values while operating at low switching frequency, at the expense of adding an inductor and control timing.

If we eliminate C_{big} and make the load <u>inductive</u> (either by inserting an inductor at the output or by adding a second stage converter), we can also get low-loss "soft charging".



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