

MASSACHUSETTS INSTITUTE OF TECHNOLOGY
Department of Electrical Engineering and Computer Science

Receivers, Antennas, and Signals – 6.661

Problem Set No. 12

Issued: 4/29/03

Due: 5/8/03

Problem 12.1

Design a 10-GHz 1-kw peak-power pulsed radar to track single locusts across the desert at a distance of ~ 10 km; assume the scattering cross-section of a locust is one square centimeter and the pulse bandwidth is B Hz.

- a) What should the diameter D be for a typical circular parabolic-mirror antenna if the SNR for a receiver having $T_R + T_A = 600\text{K}$ is to be >10 dB for a single locust?
- b) What considerations should govern the chosen duration τ [sec] of each CW pulse for this situation? (No τ needs to be chosen here.)
- c) What considerations should govern the chosen spacing T [sec] between consecutive CW pulses?
- d) How does our desire to measure the velocity vector of a swarm of locusts affect our choice of CW pulse length τ ? What τ might you recommend if locusts fly $\sim 10\text{ ms}^{-1}$ and we should like to know their instantaneous (using a single radar pulse) radial velocity within $\sim \pm 1\text{ ms}^{-1}$?
- e) What pulse length τ [sec] might you recommend in order to measure the instantaneous distance of a swarm of locusts within $\sim \pm 10$ m?
- f) How should we redesign the radar pulse to resolve the conflict between (d) and (e)? Roughly sketch and dimension the ambiguity function of your chosen pulse.
- g) Given your answer for (f), what should the diameter D of the antenna be?

Problem 12.2

A certain inverse synthetic aperture radar (ISAR) system consists of a single motionless 10-meter radar dish that views zenith at 10-cm wavelength. It images commercial jetliners flying directly overhead at ~10-km altitude.

- a) What is the approximate lateral (not range) resolution $L(m)$ of this radar in normal (not ISAR) mode at 10-km altitude?
- b) What sort of pulse would yield 1-m range resolution?
- c) What is the approximate lateral resolution (m) of this radar along the flight path of a jetliner when operated in its ISAR mode? What is the resolution in the orthogonal direction?
- d) What changes to the radar operation are required to obtain 1-m resolution along the flight path? Please provide quantitative answers and assume D remains 10 meters.
- e) Assume the jetliners always fly between 8 and 12 km altitude. What is the maximum usable pulse repetition frequency (RPF)?
- f) If we use the techniques of part (d) to obtain ~10-cm resolution in range and 1-m resolution in the flight-path direction, is delay compensation necessary for the pulse envelope? If so, how much delay is required in the worse case?
- g) This ability to track the aircraft permits 10 images to be obtained with the original 10-m resolution. What is the ratio of rms intensity fluctuations to mean intensity for each pixel of the reconstructed average image?

Problem 12.3

A uniformly illuminated aperture antenna is 10-m square and operates at 1-cm wavelength.

- a) At what angle off axis is its first null?
- b) This antenna maps the sky, after which the high spatial frequencies of the resulting image are boosted to yield the principal solution. If the target consists of a spatial impulse (unresolved source), the restored image exhibits nulls at certain angles. At what angle off axis is the first null?
- c) Aperture synthesis is achieved by making multiple observations using two small antennas within the same 10-m square. At what angle off axis is the first null of the synthesized image?