## Computing the time dependent amplitude function

$$ec{A}(q)$$
  $ec{\Psi}(x,t)$   $ec{A}(q)$ 

Now that we have , how do we find the time dependence of ? Since is the coefficient vector for the eigenfunctions of  $\mathbf{H}$ , we know the time dependence is accounted for by multiplying each coefficient by  $\mathbf{e}^{-i\mathbf{E}\mathbf{t}/\hbar}$ . So, we now create a vector  $\mathbf{E}$ , indexed by  $\mathbf{q}$ .

$$ec{E} = rac{\hbar^2}{2m} * ec{q^2} = rac{\hbar^2}{2m} \left( egin{array}{c} q_1^2 \ q_2^2 \ q_3^2 \ dots \ q_m^2 \end{array} 
ight)$$

Now, if we take the exponential of times each element, where t is the time we

 $\Psi(x)$  wish to evaluate at, we get

$$ec{\zeta} = \left(egin{array}{c} e^{-iE_1t/\hbar} \ e^{-iE_2t/\hbar} \ dots \ e^{-iE_mt/\hbar} \end{array}
ight)$$

Now, if we perform element by element multiplication (MATLAB® command is ``.\*") on  $\vec{\zeta}$   $\vec{A}(q)$ 

$$ec{A}_t(q) = ec{A}(q) \cdot * ec{\zeta}(q) = \left(egin{array}{c} A(q_1)\zeta(q_1) \ A(q_2)\zeta(q_2) \ dots \ A(q_m)\zeta(q_m) \end{array}
ight) = \left(egin{array}{c} A(q_1)e^{-iE_1t/\hbar} \ A(q_2)e^{-iE_2t/\hbar} \ dots \ A(q_m)e^{-iE_mt/\hbar} \end{array}
ight)$$

Now, we have taken account for the time dependence by modifying our amplitude

function (note the subscript t to denote that this is at a particular time t). The last chore is to now compute the wave function in x-space from the modified amplitude function.