## **Computing the time dependent amplitude function**

## $\vec{A}(q)$

 $\vec{\Psi}(x,t)$  $A(a)$ Now that we have , how do we find the time dependence of ? Since is the coefficient vector for the eigenfunctions of  $\mathcal{H}$ , we know the time dependence is accounted for by multiplying each coefficient by  $e^{-iEt/\hbar}$ . So, we now create a vector **E**,

indexed by **q**.

$$
\vec{E} = \frac{\hbar^2}{2m} * q^{\frac{1}{2}} = \frac{\hbar^2}{2m} \begin{pmatrix} q_1^2 \\ q_2^2 \\ q_3^2 \\ \vdots \\ q_m^2 \end{pmatrix}
$$

Now, if we take the exponential of  $\overline{t}$  times each element, where **t** is the time we wish to evaluate  $\Psi(x)$  at, we get

$$
\vec{\zeta} = \left( \begin{array}{c} e^{-iE_1t/\hbar} \\ e^{-iE_2t/\hbar} \\ \vdots \\ e^{-iE_mt/\hbar} \end{array} \right)
$$

Now, if we perform element by element multiplication (MATLAB<sup>®</sup> command is `` \*") on  $\vec{A}(q)$ 

 $\mathbf{A} = \mathbf{A} \mathbf{E} \mathbf{A} + \mathbf{A} \mathbf{E} \mathbf{A} + \mathbf{A} \mathbf{A}$ 

(q) and we get:

$$
\vec{A}_t(q)=\vec{A}(q)\cdot\ast\vec{\zeta}(q)=\left(\begin{array}{c}A(q_1)\zeta(q_1)\\A(q_2)\zeta(q_2)\\\vdots\\A(q_m)\zeta(q_m)\end{array}\right)=\left(\begin{array}{c}A(q_1)e^{-iE_1t/n}\\A(q_2)e^{-iE_2t/\hbar}\\ \vdots\\A(q_m)e^{-iE_mt/\hbar}\end{array}\right)
$$

Now, we have taken account for the time dependence by modifying our amplitude  $A(q)$ 

function (note the subscript **t** to denote that this is  $\cdot$  at a particular time **t**). The last chore is to now compute the wave function in x-space from the modified amplitude function.