



















$$\begin{array}{l} \text{Short Josephson Junction}\\ \text{Let uself fields generated by the currents be negligible, and $\mathbf{B} = \mathbf{B}_o \mathbf{i}_y$, then

$$\begin{array}{l} \frac{\partial \varphi}{\partial z} = \frac{2\pi}{\Phi_o} B_o h_{eff}\\ \frac{\partial \varphi}{\partial z} = \frac{2\pi}{\Phi_o} B_o h_{eff}\\ \text{That can be integrated directly,}\\ \text{Maison-Wesley, 1991. ISBN: 020118323.}\\ \end{array}$$

$$\begin{array}{l} \text{Fuse sec: Figure 8.14, page 421, from Orlando, T, and K. Delin.}\\ \frac{\partial \varphi}{\partial z} = \frac{2\pi}{\Phi_o} B_o h_{eff} z + \varphi(0)\\ \text{That can be integrated directly,}\\ \text{That can be integrated directly,}\\ \text{The total current with constant } J_c \text{ is}\\ \frac{d/2}{-d/2} \int_{-w/2}^{w/2} J_c \sin \varphi(z) \, dy \, dz\\ \text{Fuse through the junction}\\ \frac{1}{D} = B_o h_{eff} d\\ \text{Critical current of the junction}\\ \frac{1}{D} = J_c w d\\ \end{array}$$

$$\begin{array}{l} \text{Massachusetts Institute of Technology}\\ \frac{1}{D(2)} \sum_{k=0}^{w} 2 \\ \frac$$$$



















Long Josephson Junction (self fields included)

As before,

$$\frac{\partial \varphi}{\partial z} = \frac{2\pi}{\Phi_o} B_y h_{eff}$$
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$$J_s(y, z, t) = J_c(y, z) \sin \varphi(z, t)$$
Please see: Figure 8.14, page 421, from Orlando, T., and K. Delin.
Foundations of Applied Superconductivity. Reading, MA:
Addison-Wesley, 1991. ISBN: 0201183234.

$$\nabla \times \mathbf{B} = \mu_o \mathbf{J} + \epsilon \mu_o \frac{\partial \mathbf{E}}{\partial t}$$
In the general time-dependent case, the sine-Gordon equation governs the phase:

$$\frac{\partial^2 \varphi}{\partial z^2} - \frac{1}{u_p^2} \frac{\partial^2 \varphi}{\partial t^2} = \frac{1}{\lambda_J^2} \sin \varphi \quad \text{where} \quad u_p = \frac{1}{\sqrt{\mu_o \epsilon}} \sqrt{\frac{a}{\lambda + a}}$$
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