# Problem Set \#6 

Issued: Wednesday, April 2, 2003
Due: Monday, April 7, 2003

## Problem 1

Do problem 1 in May \& Spanos, Chapter 5, as repeated below.
Assuming a Poisson model, calculate the maximum defect density allowable on 100,000 NMOS transistors in order to achieve a functional yield of $95 \%$. Assume the gate of each device is $10 \mu \mathrm{~m}$ wide and 1 $\mu \mathrm{m}$ long.

## Problem 2

Do problem 5 in May \& Spanos, Chapter 5, as restated below (wording change in italics).
10,000 units of a product with area $0.5 \mathrm{~cm}^{2}$ and 200 chips per wafer are to be produced in three manufacturing areas (each wafer passes through all three of these manufacturing areas in turn), with a $\mathrm{D}_{0}$ of 0.9 ,
1.1 , and $1.3 \mathrm{~cm}^{-2}$, respectively. How many wafers need to be ordered? Assume a negative binomial model with $\alpha=2$ and a combined fabrication, assembly, and test yield of $95 \%$.

## Problem 3

Do problem 4 in May \& Spanos, Chapter 5, as repeated below with modifications. This problem is based on the figure and discussion in the paper by Stapper and Rosner, which may help to refer to. Note that the bounds on the first equation have been modified from that in May \& Spanos to match Fig. 5 in Stapper.

Consider the effect of defects on IC interconnect. Figure P5-4 below illustrates the impact of defect size on critical area for circular defects of diameter $x$.

The area in which the center of such defects must fall to cause a failure increases linearly as a function of defect size. It can be expressed as

$$
\begin{gathered}
A_{c}(x)=L(x+W-2 R) \\
W-R \leq x \leq \infty
\end{gathered}
$$

where $L$ is the interconnect length and $R$ is the minimum remaining width in the interconnect line. Suppose that the normalized probability density function of defect sizes is given by

$$
g(x)=\frac{X_{U}^{2} \cdot X_{L}^{2}}{x^{3}\left(X_{U}^{2}-X_{L}^{2}\right)}
$$

where $X_{L}^{2}$ and $X_{U}^{2}$ are the lower and upper limits of the range of defect sizes, respectively.


Figure P5-4
(a) Find an expression for the average critical area $\left(A_{A V}\right)$ by evaluating the integral

$$
A_{A V}=\int_{X_{L}}^{X_{U}} A_{c}(x) g(x) d x
$$

(b) Find an expression containing only $L, W, R$, and $X_{L}$ for the average critical area, in the limit as the upper limit on defect size approaches infinity. As the minimum wire remaining value ( $R$ ) goes to zero, does your expression behave as you might expect?

$$
A_{A V}=\frac{L \cdot X_{L}^{2} \cdot W}{R^{2}}
$$

## Problem 4

Do problem 10 in May \& Spanos, Chapter 5, as repeated below.
Suppose that you use 200 mm wafers, and also assume that you can only get functional dice only within the inner 190 mm diameter (outer 5 mm margin is full of defects). On the one product that you have run so far, a chip $5 \mathrm{~mm} \times 5 \mathrm{~mm}$, the yield is $80 \%$.
(a) Using the simple Poisson model, find the defect density (in the good area of the wafer) and plot the yield as a function of $S$, where $S$ is the square root of the area of the die in production. Plot the total and the good die per wafer as a function of $S$ on the same graph.
(b) Repeat the calculations and plots in (a) using the negative binomial model ( $\alpha=1.5$ ).
(c) Suppose that an alternative explanation for the data were that some fraction, $f$, of the wafer was perfect and the rest was totally dead. This is the "black-white" model that assumes a perfect deterministic
clustering of defects. What is $f$ ? Plot the Good Die per wafer for this model on the same graph as in (a)(b).
(d) What defect density reduction would you have to achieve to yield $50 \%$ of the available die at $S=15$ mm according to models (a), (b) and (c)?

## Problem 5

Prior characterization of a fab has been performed for two critical process layers. The metal3 layer has been found to have a random defect density of $1 \mathrm{~cm}^{-2}$. The via3 process has a random failure rate of $10^{-7}$.

A new product with a chip size of 2 mm x 4 mm is proposed to run on this fab line. A functioning chip will sell for $\$ 10$. The product has both memory and logic blocks. The memory block has a critical area to metall failures of $3 \mathrm{~mm}^{2}$, and has $2 \times 10^{6}$ vias. The logic, on the other hand, has a critical area to metall failures of $5 \mathrm{~mm}^{2}$, but only $10^{5}$ vias.
(a) Complete the following yield impact matrix (as in Ciplikas) for this product. As a reminder, the interior cells give the limited yield for that block and process step; the bottom columns give the aggregate yield for the process, the rightmost rows give the aggregate yield for the block, and the corner entry gives to aggregate chip yield.

(b) You are the memory module integration engineer, and you are considering layout changes to the metal3/via3 design to improve the memory block yield. Experimentation in the fab has shown that for each $0.1 \mu \mathrm{~m}$ of border added around all vias in the design, the via3 failure rate decreases by a factor of 10 . However, the extra borders cause the metall critical area to increase: specifically, each $0.1 \mu \mathrm{~m}$ of border added increases the critical area by $10 \%$. How much, if any, border area should be added to the memory block vias, to optimize the memory block yield? Note that the vias borders can be selected in 10 nm ( 0.01 $\mu \mathrm{m})$ increments.
(c) The fab manager is responsible for total income for the product through this 200 mm wafer fab. Given that any borders also increases the total die size by the same amount (i.e. each $0.1 \mu \mathrm{~m}$ added border adds $10 \%$ to the total die size), evaluate the reaction to your proposed product design modification in part b. If implemented (and assuming $100 \%$ yield in all other process steps), how much revenue per wafer would be gained our lost by your proposal?

