

6.976

High Speed Communication Circuits and Systems

Lecture 20

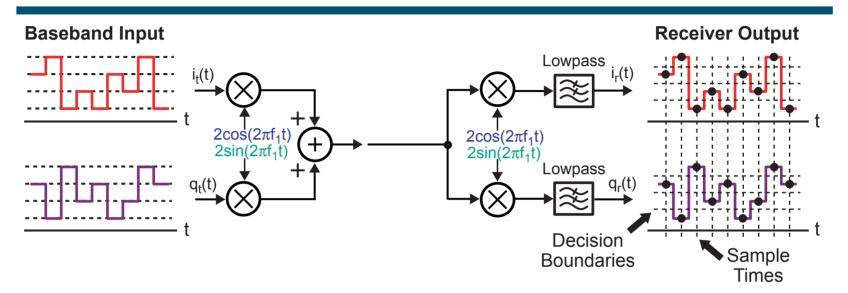
Performance Measures of Wireless Communication

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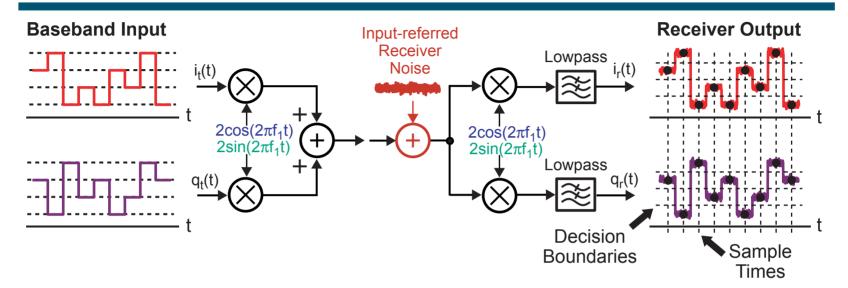
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#### Recall Digital Modulation for Wireless Link



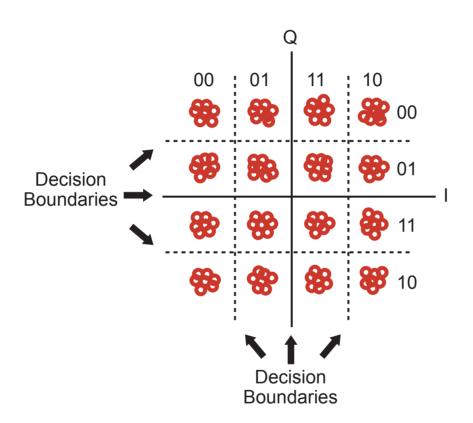
- Send discrete-leveled values on I and Q channels
- Performance issues
  - Spectral efficiency (transmitter)
  - Bit error rate performance (receiver)
- Nonidealities
  - Intersymbol interference
  - Noise
  - Interferers

#### Impact of Receiver Noise



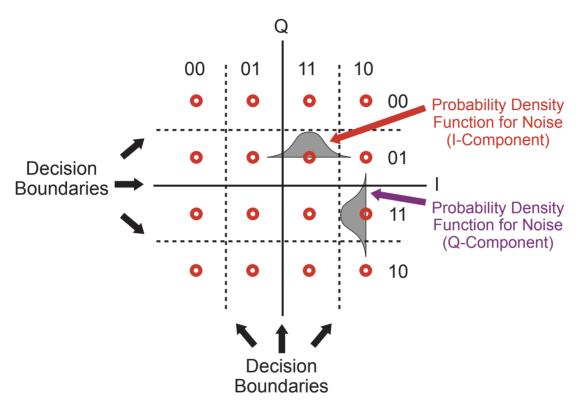
- Performance impact
  - SNR is reduced, leading to possible bit errors
- Methods of increasing SNR
  - Decrease bandwidth of receiver lowpass
    - SNR is traded off for intersymbol interference
  - Increase input power into receiver
    - Increase transmit power and/or shorten its distance from receiver

#### View SNR Issue with Constellation Diagram



- Noise causes sampled I/Q values to vary about their nominal values
- Bit errors are created when sampled I/Q values cross decision boundaries

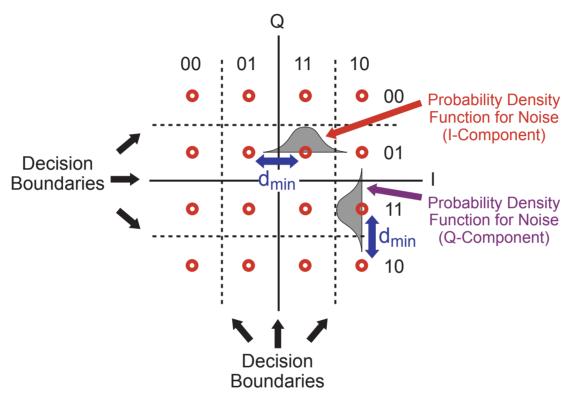
#### Mathematical Analysis of SNR versus Bit Error Rate (BER)



- Model noise impacting I and Q channels according to a probability density function (PDF)
  - Gaussian shape is often assumed
- Receiver bit error rate can be computed by calculating probability of tail regions of PDF curves

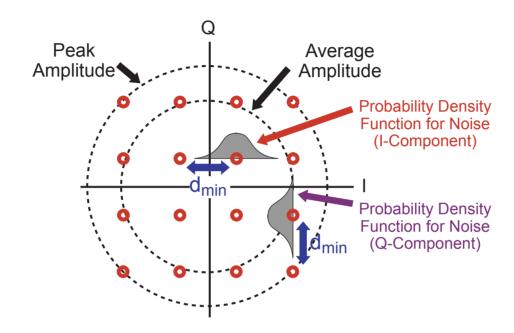
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#### Key Parameters for SNR/BER Analysis



- Bit error rate (BER) is a function of
  - Variance of noise
  - Distance between constellation points (d<sub>min</sub>)
- Larger d<sub>min</sub> with a fixed noise variance leads to higher SNR and a lower bit error rate

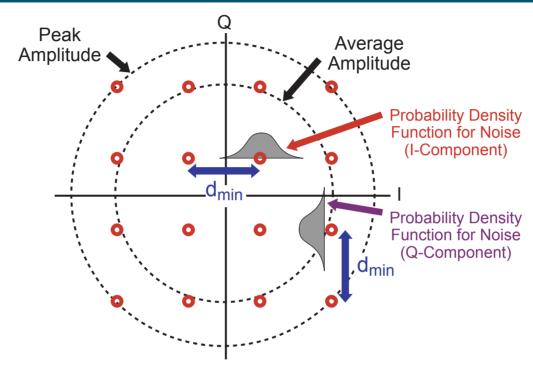
#### Relationship Between Amplitude and Constellation



- Distance of I/Q constellation point from origin corresponds to instantaneous amplitude of input signal at that sample time
- Amplitude is measured at receiver and a function of
  - Transmit power
  - Distance between transmitter and receiver (and channel)

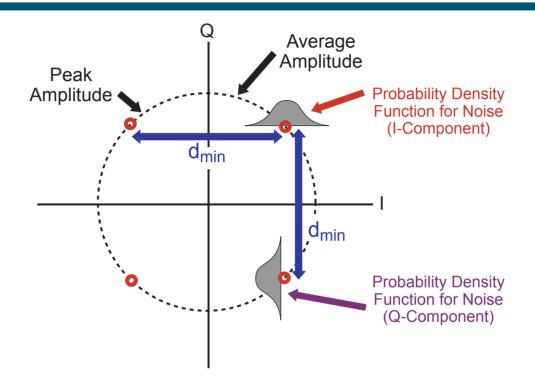
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# Impact of Increased Signal Power At Receiver



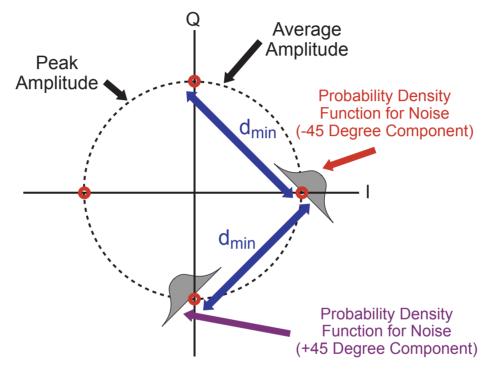
- Separation between constellation points, d<sub>min</sub>, increases as received power increases
- Noise variance remains roughly constant as input signal power is increased
  - Noise variance primarily determined by receiver circuits
- Bit error rate improves with increased signal power!

# Impact of Modulation Scheme on SNR/BER



- Lowering the number of constellation points increases d<sub>min</sub> for a fixed input signal amplitude
  - SNR is increased (given a fixed noise variance)
  - Bit error is reduced
- Actual situation is more complicated when coding is used

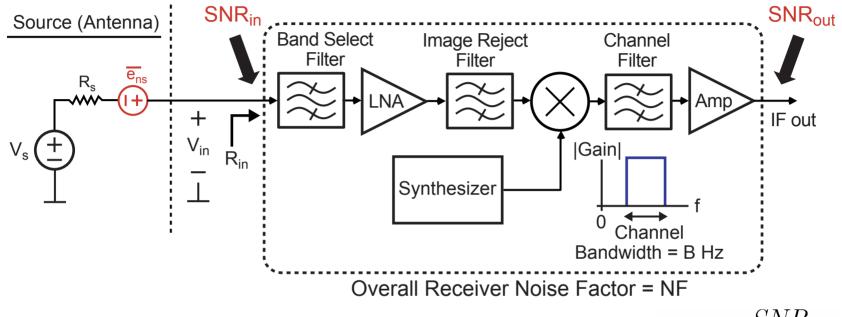
#### Alternate View of Previous Constellation



- Common modulation method is to transmit independent binary signals on I and Q channels
- The above constellation has the same d<sub>min</sub> as the one on the previous slide

 Obtains the same SNR/BER performance given that the noise on I/Q channels is symmetric

# Impact of Noise Factor on Input-Referred SNR



$$NF = \frac{SNR_{in}}{SNR_{out}}$$

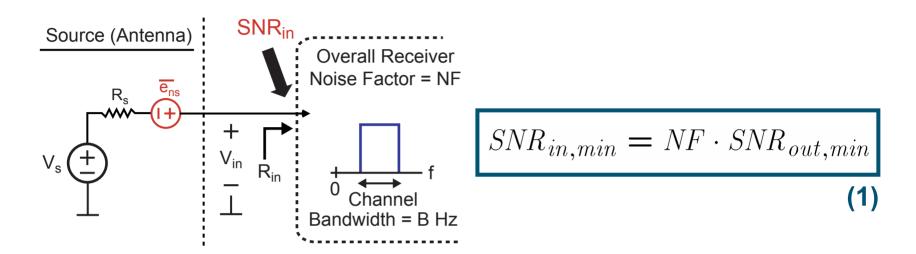
To achieve acceptable bit error rates (BER)

$$SNR_{out} \geq SNR_{out,min}$$

Refer SNR requirement to input

$$SNR_{in} = NF \cdot SNR_{out} \ge NF \cdot SNR_{out,min}$$

# Minimum Input Power to Achieve Acceptable SNR



Calculation of input SNR in terms of input power

$$SNR_{in} = \frac{v_{in}^2/R_{in}}{\alpha^2 \overline{e_{nRs}^2}/R_{in}} = \boxed{\frac{P_{in}}{\alpha^2 \overline{e_{nRs}^2}/R_{in}}}, \text{ where } \alpha = \frac{R_{in}}{R_s + R_{in}}$$

$$\blacksquare \text{ Combine (1) and (2)}$$

$$P_{in,min} = \alpha^2 \overline{e_{nRs}^2} / R_{in} \cdot NF \cdot SNR_{out,min}$$

# Simplified Expression for Minimum Input Power

$$P_{in,min} = \alpha^2 \overline{e_{nRs}^2} / R_{in} \cdot NF \cdot SNR_{out,min}$$

 Assume that the receiver input impedance is matched to the source (i.e., antenna, etc.)

$$\Rightarrow \alpha = \frac{R_{in}}{R_s + R_{in}} \Big|_{R_{in} = R_s} = \frac{1}{2}$$

$$\Rightarrow \alpha^2 \overline{e_{nRs}^2} / R_{in} \Big|_{R_{in} = Rs} = \left(\frac{1}{2}\right)^2 \frac{4kTR_s \Delta f}{R_{in}} \Big|_{R_{in} = Rs} = kT \Delta f$$

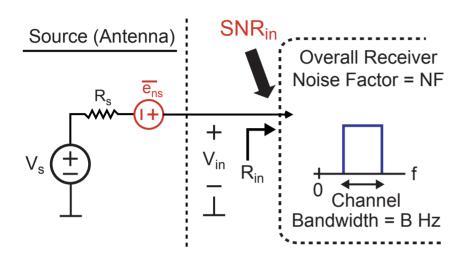
Resulting expression

$$P_{in,min} = kT\Delta f \cdot NF \cdot SNR_{out,min}$$

At room temperature:

$$kT = -174 \text{ dBm/Hz}$$

#### Receiver Sensitivity



$$P_{in,min} = kT\Delta f \cdot NF \cdot SNR_{out,min}$$

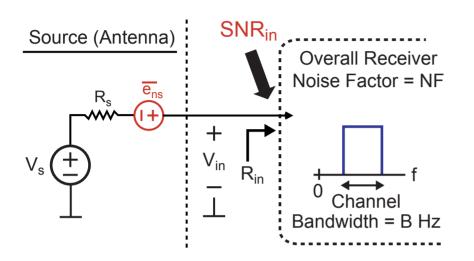
 Sensitivity of receiver is defined as minimum input power that achieves acceptable SNR (in units of dBm)

$$dBm(P_{in,min}) = 10\log(kT\Delta f \cdot NF \cdot SNR_{out,min})$$

$$= -174 + 10 \log(B) + dB(NF) + dB(SNR_{out,min})$$

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# Example Calculation for Receiver Sensitivity

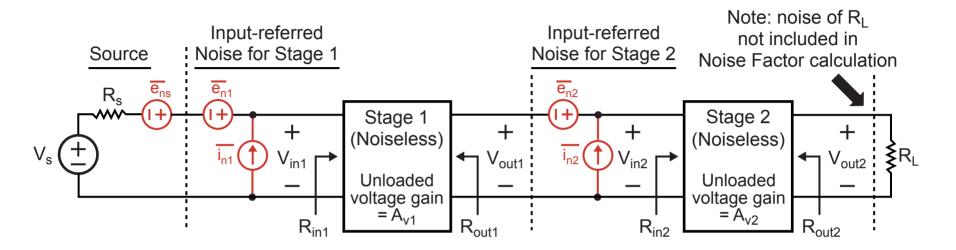


$$dBm(P_{in,min}) = -174 + 10\log(B) + dB(NF) + dB(SNR_{out,min})$$

- Suppose that a receiver has a noise figure of 8 dB, channel bandwidth is 1 MHz, and the minimum SNR at the receiver output is 12 dB to achieve a BER of 1e-3
  - Receiver sensitivity (for BER of 1e-3) is

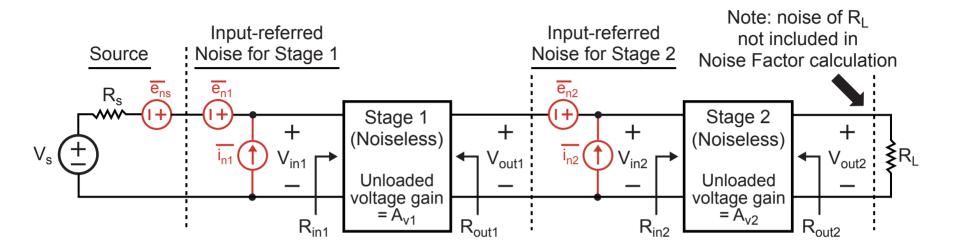
$$dBm(P_{in,min}) = -174 + 60 + 8 + 12 = -94 dBm$$

# Calculation of Noise Figure of Cascaded Stages

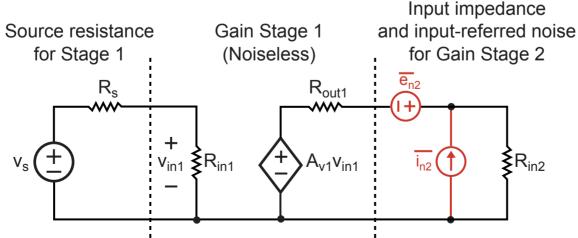


- Want to calculate overall noise figure of above system
- Assumptions
  - Input refer the noise sources of each stage
  - Model amplification (or attenuation) of each stage as a noiseless voltage controlled voltage source with an unloaded gain equal to A<sub>v</sub>
  - Ignore noise of final load resistor (or could input refer to previous stage)

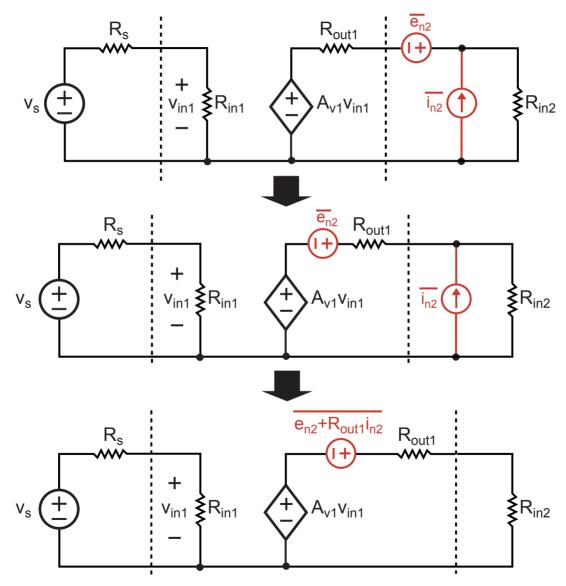
# Method: Refer All Noise to Input of First Stage



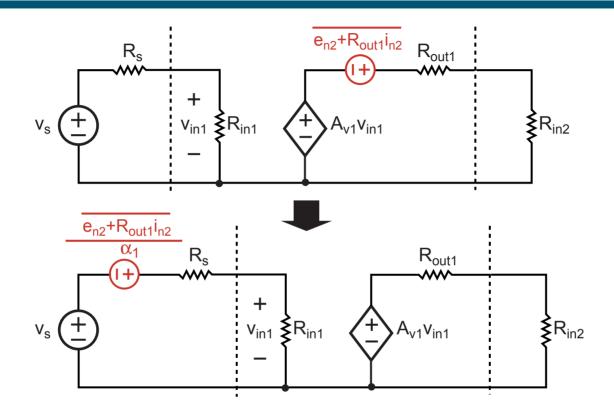
#### Model for referring stage 2 noise to input of stage 1



# Step 1: Create an Equivalent Noise Voltage Source



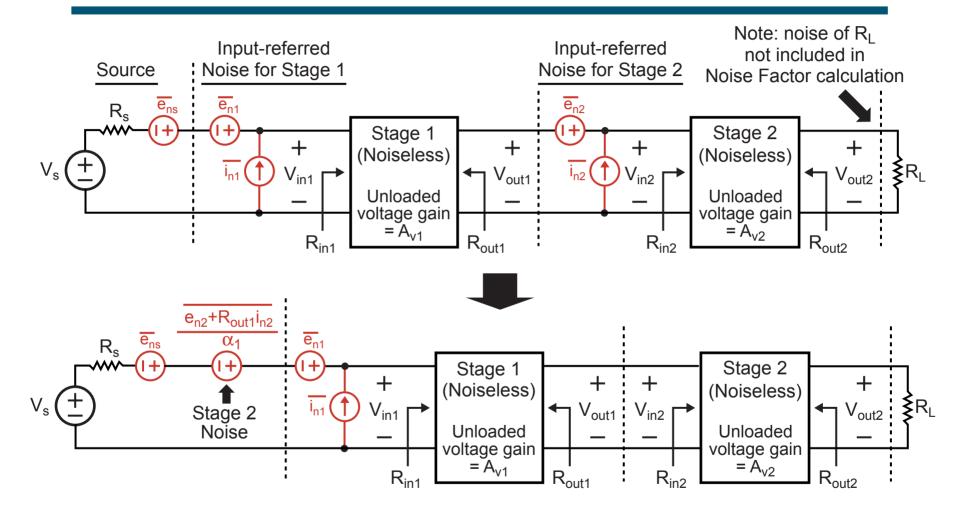
# Step 2: Input Refer Voltage Noise Source



• Scaling factor  $\alpha_1$  is a function of unloaded gain,  $A_v$ , and input voltage divider

$$\alpha_1 = \frac{R_{in}}{R_s + R_{in}} A_v$$

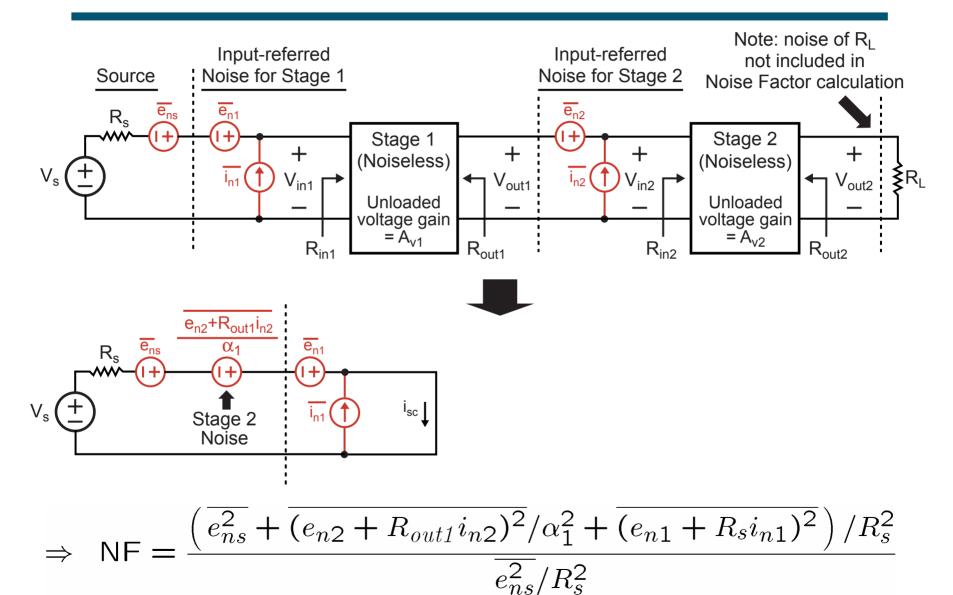
# Input Referral of Noise to First Stage



• Where 
$$lpha_1 = rac{R_{in}}{R_s + R_{in}} A_{vi}$$

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#### **Noise Factor Calculation**



# Alternate Noise Factor Expression

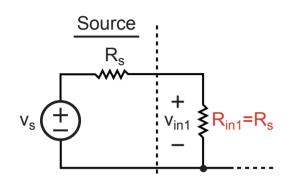
$$\begin{aligned} &\mathsf{NF} = \frac{\left(\overline{e_{ns}^2} + \overline{(e_{n2} + R_{out1}i_{n2})^2}/\alpha_1^2 + \overline{(e_{n1} + R_si_{n1})^2}\right)/R_s^2}{\overline{e_{ns}^2}/R_s^2} \\ &= \frac{\overline{e_{ns}^2} + \overline{(e_{n1} + R_si_{n1})^2} + \overline{(e_{n2} + R_{out1}i_{n2})^2}/\alpha_1^2}{\overline{e_{ns}^2}} \\ &= 1 + \frac{\overline{(e_{n1} + R_si_{n1})^2}}{\overline{e_{ns}^2}} + \frac{1}{\alpha_1^2} \frac{\overline{(e_{n2} + R_{out1}i_{n2})^2}}{\overline{e_{ns}^2}} \\ &= 1 + \frac{\overline{(e_{n1} + R_si_{n1})^2}}{4kTR_s} + \frac{1}{\alpha_1^2} \frac{R_{out1}}{R_s} \frac{\overline{(e_{n2} + R_{out1}i_{n2})^2}}{4kTR_{out1}} \\ &= 1 + (\mathsf{NF}_1 - 1) + \frac{1}{\alpha_1^2} \frac{R_{out1}}{R_s} (\mathsf{NF}_2 - 1) \\ &= 1 + (\mathsf{NF}_1 - 1) + \frac{(\mathsf{NF}_2 - 1)}{A_{p1}}, \quad A_{p1} = \alpha_1^2 \frac{R_s}{R_{out1}} \end{aligned}$$

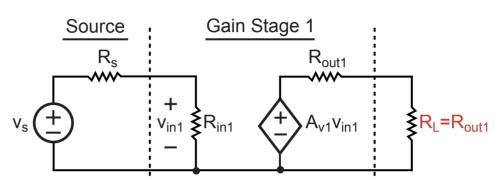
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#### Define "Available Power Gain"

#### **Available Source Power**

#### **Available Power at Output**





Available power gain for stage 1 defined as

Available power at output

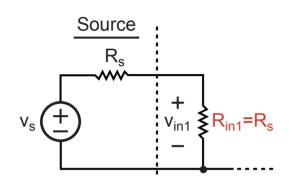
$$\left(v_s \frac{R_{in1}}{R_s + R_{in1}} A_{v1} \frac{R_{out1}}{R_{out1} + R_{out1}}\right)^2 / R_{out1} = \frac{v_s^2 \alpha_1^2}{4R_{out1}}$$

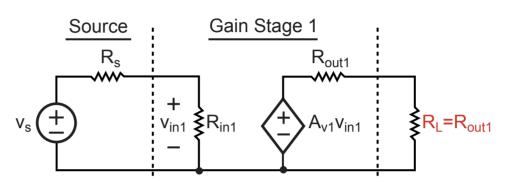
Available source power 
$$\left(v_s \frac{R_s}{R_s + R_s}\right)^2 / R_s = \frac{v_s^2}{4R_s}$$

# Available Power Gain Versus Loaded Voltage Gain

#### **Available Source Power**

#### **Available Power at Output**





Available power gain for stage 1

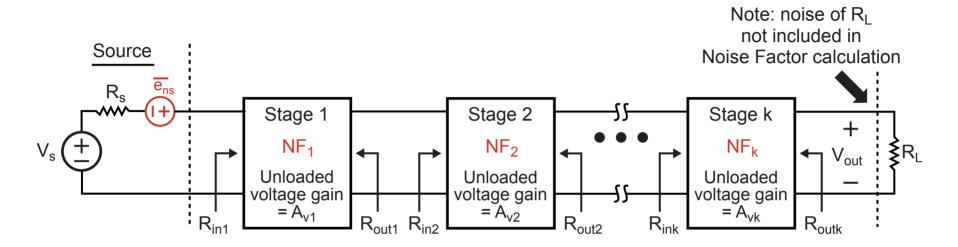
$$A_{p1} = \frac{v_s^2 \alpha_1^2}{4R_{out1}} \frac{4R_s}{v_s^2} = \alpha_1^2 \frac{R_s}{R_{out1}} \quad \text{where } \alpha_1 = \frac{R_{in1}}{R_s + R_{in1}} A_{v1}$$

If  $R_{in1} = R_{out1} = R_s$ 

$$\alpha_1 = \frac{1}{2} A_{v1} \implies A_{p1} = \frac{1}{4} A_{v1}^2 = A_{v1\_l}^2$$

Where A<sub>v1 I</sub> is defined as the "loaded gain" of stage 1

# Final Expressions for Cascaded Noise Factor Calculation



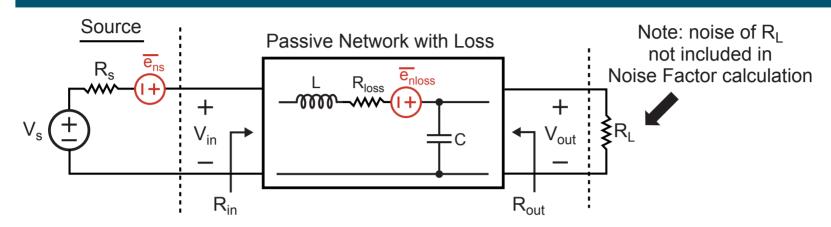
Overall Noise Factor (general expression)

$$NF = 1 + (NF_1 - 1) + \frac{(NF_2 - 1)}{A_{p1}} + \dots + \frac{(NF_k - 1)}{A_{p1} \cdot \dots \cdot A_{pk}}$$

Overall Noise Factor when all input and output impedances equal R<sub>s</sub>:

$$NF = 1 + (NF_1 - 1) + \frac{(NF_2 - 1)}{A_{v_1 l}^2} + \dots + \frac{(NF_k - 1)}{A_{v_1 l}^2 \dots A_{v_k l}^2}$$

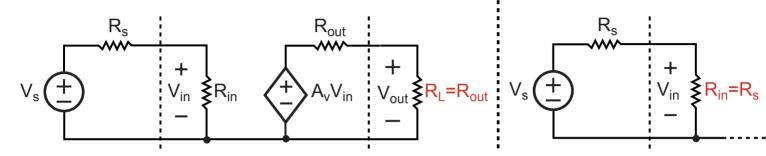
#### Calculation of Noise Factor for Lossy Passive Networks



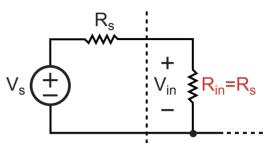
- RF systems often employ passive filters for band select and channel select operations
  - Achieve high dynamic range and excellent selectivity
- Practical filters have loss
  - Can model as resistance in equivalent RLC network
  - Such resistance adds thermal noise, thereby lowering noise factor of receiver
- We would like to calculate noise factor contribution of lossy passive networks in a straightforward manner
  - See pages 46-48 of Razavi book

#### Define "Available Power Gain" For Passive Networks

#### **Available Power at Output**



#### **Available Source Power**



Available power at output

$$V_s^2 \left(\frac{R_{in}}{R_s + R_{in}}\right)^2 A_v^2 \left(\frac{R_{out}}{R_{out} + R_{out}}\right)^2 / R_{out}$$

$$= \frac{V_s^2}{4R_{out}} \left(\frac{R_{in}}{R_s + R_{in}}\right)^2 A_v^2$$
Available source power

**Available source power** 

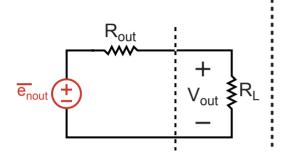
$$V_s^2 \left(\frac{R_s}{R_s + R_s}\right)^2 / R_{in} = \frac{V_s^2}{4R_s}$$

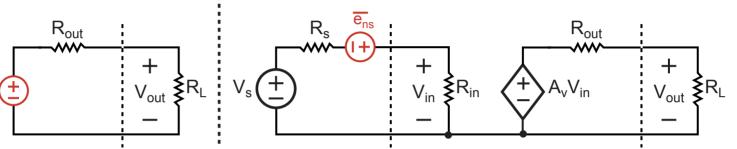
$$\Rightarrow A_p = \frac{R_s}{R_{out}} \left( \frac{R_{in}}{R_s + R_{in}} \right)^2 A_v^2 \quad (\leq 1 \text{ for passive networks})$$

# Equivalent Noise Model and Resulting NF Calculation

#### **Equivalent Model for Computing Total Noise**

#### **Equivalent Model for Computing Source Noise Contribution**





**Total noise at output** 

$$\overline{e_{nout}^2} \left( \frac{R_L}{R_L + R_{out}} \right)^2 = 4kTR_{out} \left( \frac{R_L}{R_L + R_{out}} \right)^2$$

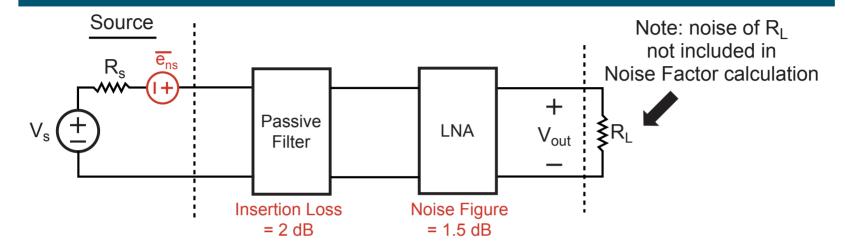
Noise due to source (referred to output)

$$4kTR_s \left(\frac{R_{in}}{R_s + R_{in}}\right)^2 A_v^2 \left(\frac{R_L}{R_L + R_{out}}\right)^2$$

**Noise factor** 

$$NF = \frac{R_{out}}{R_s} \left(\frac{R_s + R_{in}}{R_{in}}\right)^2 \frac{1}{A_v^2} = \boxed{1/A_p}$$

#### Example: Impact of Cascading Passive Filter with LNA



#### Noise Factor calculation

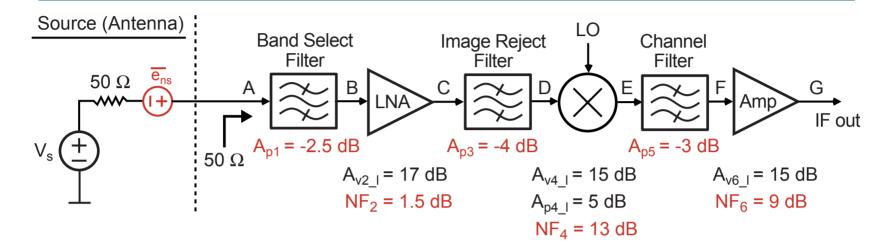
$$\begin{aligned} \text{NF} &= 1 + (\text{NF}_{\text{filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}} - 1) + \frac{\text{NF}_{\text{LNA}} - 1}{A_{\text{p\_filt}}} = \\ &= 1 + (1/A_{\text{p\_filt}$$

#### Noise Figure

$$10\log(NF) = -10\log(A_{p_filt}) + 10\log(NF_{LNA})$$

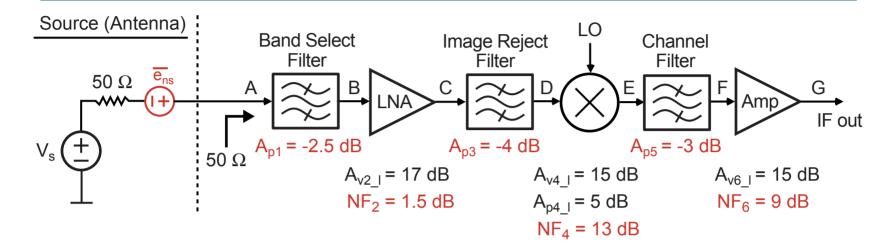
$$= 2 + 1.5 = 3.5 dB$$

#### Example: Noise Factor Calculation for RF Receiver



- Ports A, B, C, and D are conjugate-matched for an impedance of 50 Ohms
  - Noise figure of LNA and mixer are specified for source impedances of 50 Ohms
- Ports E and F and conjugate-matched for an impedance of 500 Ohms
  - Noise figure of rightmost amplifier is specified for a source impedance of 500 Ohms

# Methodology for Cascaded NF Calculation



- Perform Noise Figure calculations from right to left
- Calculation of cumulative Noise Factor at node k

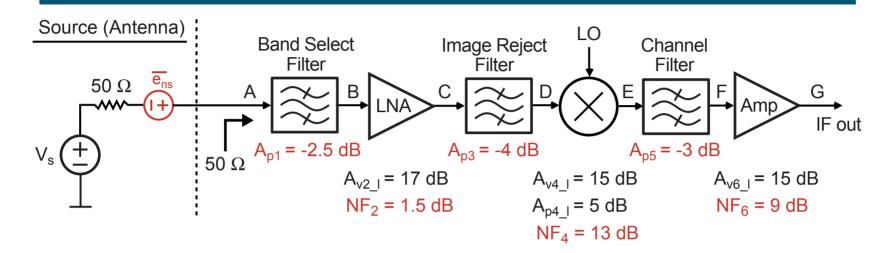
$$NF_{-}cum_{k} = NF_{k} + \frac{(NF_{k+1} - 1)}{A_{pk}}$$

If source and load impedances are equal

$$NF_{-}cum_{k} = NF_{k} + \frac{(NF_{k+1} - 1)}{A_{vk}^{2}}$$

True for all blocks except mixer above

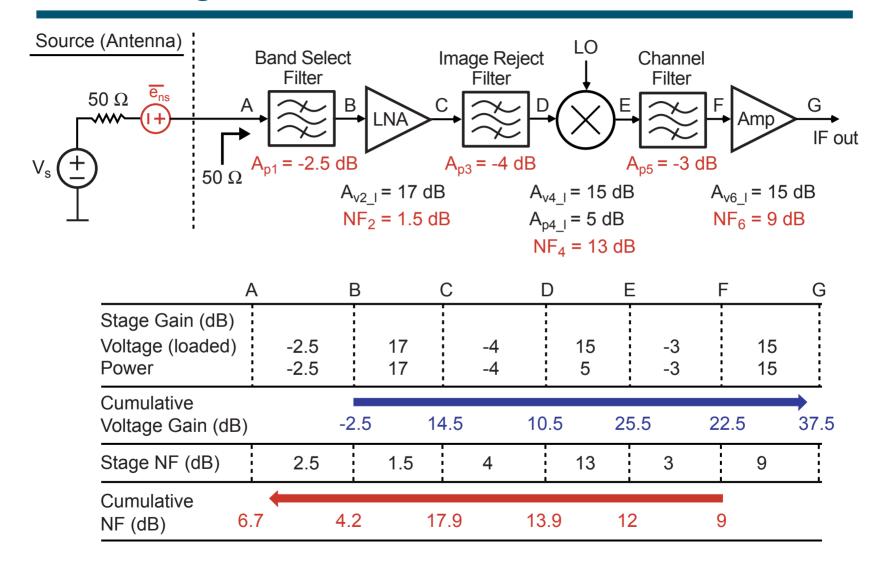
#### **Cumulative Noise Factor Calculations**



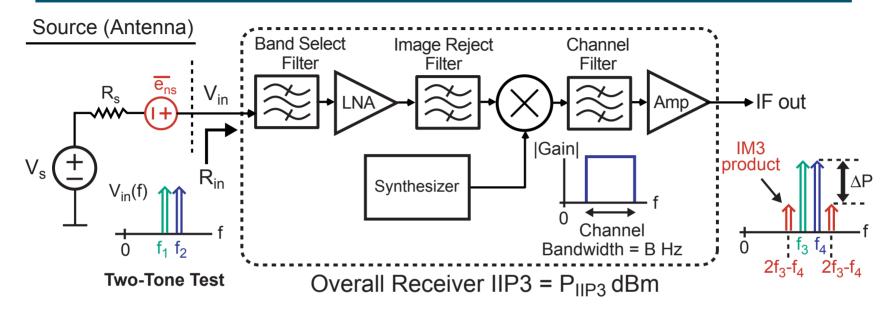
$$\begin{aligned} &\mathsf{NF}_E = 10^{(3+9)/10} = 15.85 \quad (12 \, \mathsf{dB}) \\ &\mathsf{NF}_D = 10^{(13)/10} + (15.85 - 1)/10^{(5/10)} = 24.65 \quad (13.9 \, \mathsf{dB}) \\ &\mathsf{NF}_C = 10^{(13.9 + 4)/10} = 61.7 \quad (17.9 \, \mathsf{dB}) \\ &\mathsf{NF}_B = 10^{1.5/10} + (61.7 - 1)/10^{17/10} = 2.62 \quad (4.2 \, \mathsf{dB}) \\ &\mathsf{NF}_A = 10^{(2.5 + 4.2)/10} = 4.68 \quad (6.7 \, \mathsf{dB}) \end{aligned}$$

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#### "Level Diagram" for Gain, NF Calculation



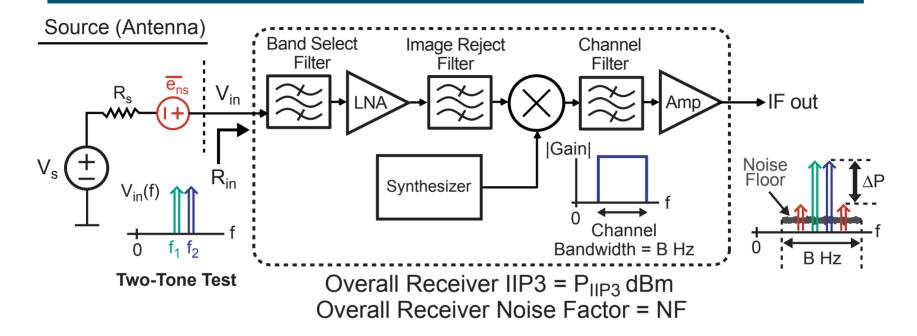
# The Issue of Receiver Nonlinearity



- Lower limit of input power into receiver is limited by sensitivity (i.e., required SNR, Noise Figure, etc.)
- Upper limit of input power into receiver is determined by nonlinear characteristics of receiver
  - High input power will lead to distortion that reduces SNR (even in the absence of blockers)
  - Nonlinear behavior often characterized by IIP3 performance of receiver

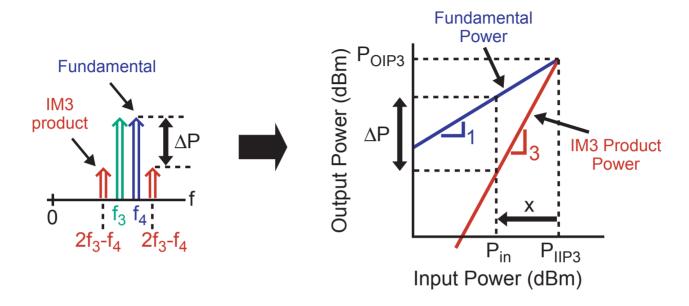
MIT OCW

#### Receiver Dynamic Range



- Defined as difference (in dB) between max and min input power levels to receiver
  - Min input power level set by receiver sensitivity
  - Max input power set by nonlinear characteristics of receiver
    - Often defined as max input power for which third order IM products do not exceed the noise floor in a two tone test

#### A Key IIP3 Expression



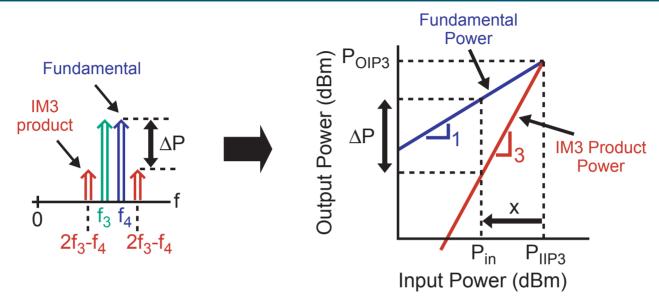
By inspection of the right figure

$$P_{IIP3} = P_{in} + x \qquad \Delta P = 3x - x = 2x$$

Combining the above expressions:

$$\Rightarrow P_{IIP3} = P_{in} + \frac{\Delta P}{2} = P_{in} + \frac{P_{out} - P_{IM3,out}}{2}$$

#### Refer All Signals to Input in Previous IIP3 Expression



- Difference between fundamental and IM3 products,  $\Delta P$ , is the same (in dB) when referred to input of amplifier
  - Both are scaled by the inverse of the amplifier gain

$$\Rightarrow P_{IIP3} = P_{in} + \frac{\Delta P}{2} = P_{in} + \frac{P_{in} - P_{IM3,in}}{2}$$

Applying algebra:

$$P_{in} = \frac{2P_{IIP3} + P_{IM3,in}}{3}$$

# Calculation of Spurious Free Dynamic Range (SFDR)

- Key expressions:
  - Minimum P<sub>in</sub> (dBm) set by SNR<sub>min</sub> and noise floor

$$P_{in,min} = F + SNR_{out,min}$$

Where F is the input referred noise floor of the receiver

$$F = -174 + 10\log(B) + dB(NF)$$

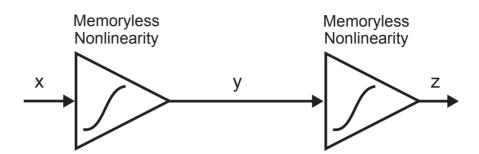
Max P<sub>in</sub> (dBm) occurs when IM3 products = noise floor

$$P_{in,max} = \frac{2P_{IIP3} + P_{IM3,in,max}}{3} \Rightarrow P_{in,max} = \frac{2P_{IIP3} + F}{3}$$

Dynamic range: subtract min from max P<sub>in</sub> (in dB)

$$SFDR = \frac{2P_{IIP3} + F}{3} - (F + SNR_{out,min})$$

#### Calculation of Overall IIP3 for Cascaded Stages



Assume nonlinearity of each stage characterized as

$$y(t) = \alpha_1 x(t) + \alpha_2 x^2(t) + \alpha_3 x^3(t)$$
  
$$z(t) = \beta_1 y(t) + \beta_2 y^2(t) + \beta_3 y^3(t)$$

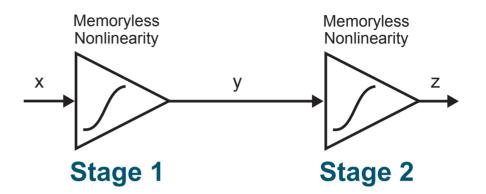
Multiply nonlinearity expressions and focus on first and third order terms

$$z(t) = \alpha_1 \beta_1 x(t) + (\alpha_3 \beta_1 + 2\alpha_1 \alpha_2 \beta_2 + \alpha_1^3 \beta_3) x^3(t) + \cdots$$

Resulting IIP3 expression

$$A_{IP3} = \sqrt{\frac{4}{3} \left| \frac{\alpha_1 \beta_1}{\alpha_3 \beta_1 + 2\alpha_1 \alpha_2 \beta_2 + \alpha_1^3 \beta_3} \right|}$$

#### Alternate Expression for Overall IIP3



Worst case IIP3 estimate – take absolute values of terms

$$A_{IP3} \approx \sqrt{\frac{4}{3} \frac{|\alpha_1 \beta_1|}{|\alpha_3 \beta_1| + |2\alpha_1 \alpha_2 \beta_2| + |\alpha_1^3 \beta_3|}}$$

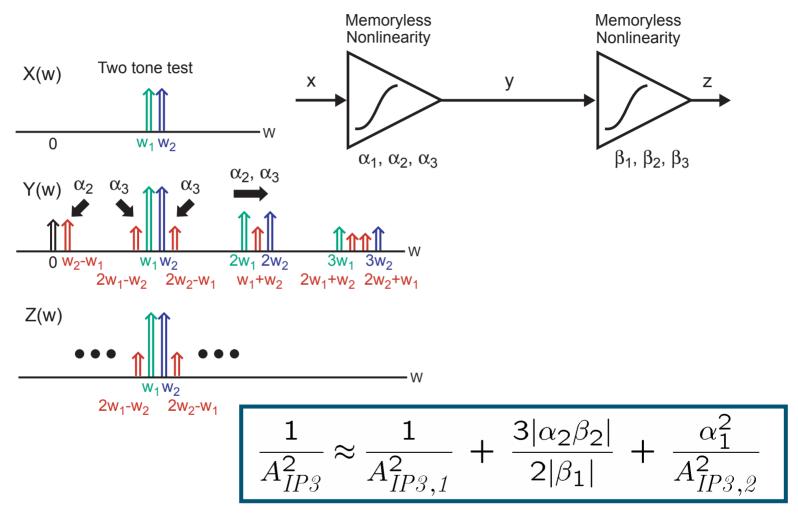
Square and invert the above expression

$$\frac{1}{A_{IP3}^2} \approx \frac{3|\alpha_3\beta_1| + |2\alpha_1\alpha_2\beta_2| + |\alpha_1^3\beta_3|}{|\alpha_1\beta_1|}$$

Express formulation in terms of IIP3 of stage 1 and stage 2

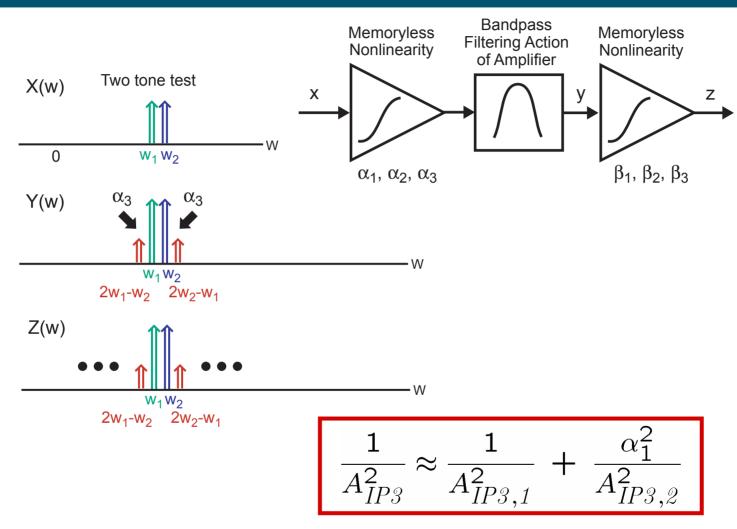
$$\frac{1}{A_{IP3}^2} \approx \frac{1}{A_{IP3,1}^2} + \frac{3|\alpha_2\beta_2|}{2|\beta_1|} + \frac{\alpha_1^2}{A_{IP3,2}^2}$$

# A Closer Look at Impact of Second Order Nonlinearity



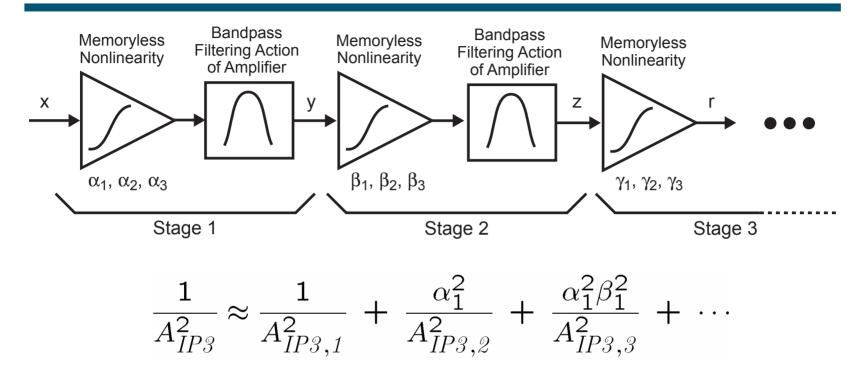
Influence of  $\alpha_2$  of Stage 1 produces tones that are at frequencies far away from two tone input

# Impact of Having Narrowband Amplification



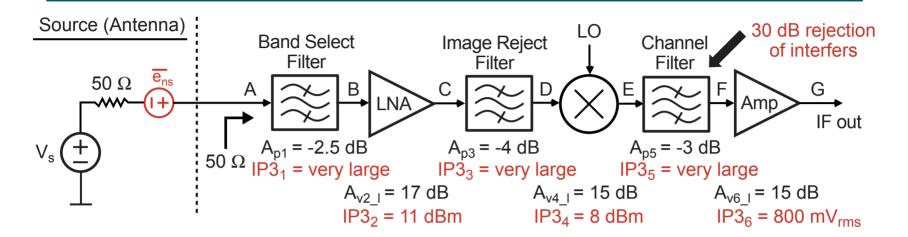
 Removal of outside frequencies dramatically simplifies overall IIP3 calculation

# Cascaded IIP3 Calculation with Narrowband Stages



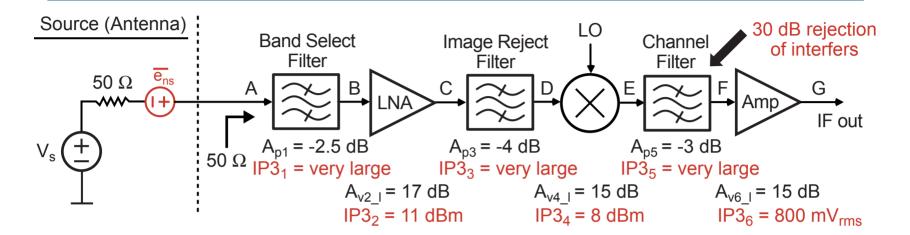
Note that  $\alpha_1$  and  $\beta_1$  correspond to the loaded voltage gain values for Stage 1 and 2, respectively

#### Example: IIP3 Calculation for RF Receiver



- Ports A, B, C, and D are conjugate-matched for an impedance of 50 Ohms
  - IIP3 of LNA and mixer are specified for source impedances of 50 Ohms
- Ports E and F and conjugate-matched for an impedance of 500 Ohms
  - IIP3 of rightmost amplifier is specified for a source impedance of 500 Ohms

# Key Formulas for IIP3 Calculation



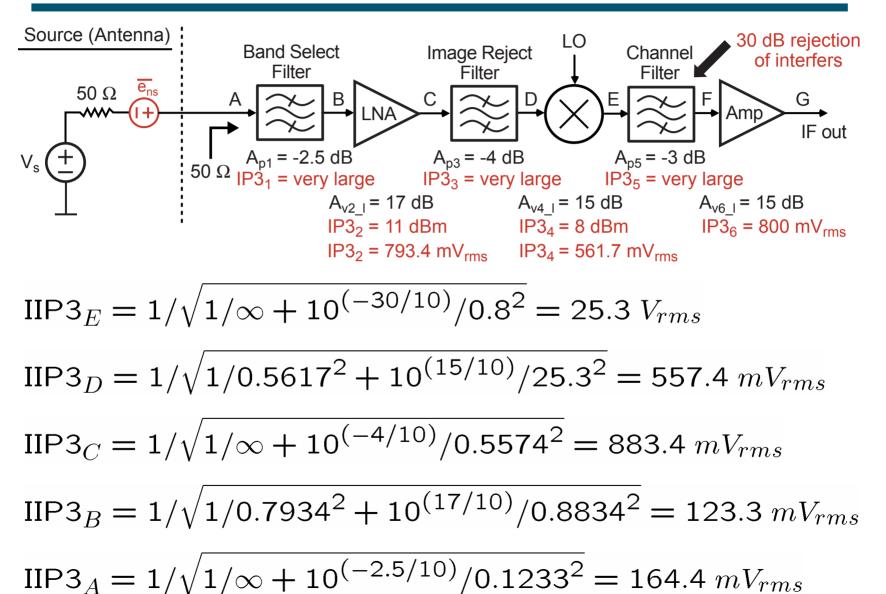
- Perform IIP3 calculations from right to left
- Calculation of cumulative IIP3 at node k (IIP3 in units of rms voltage)

$${\rm IIP3\_cum}_k = 1/\sqrt{1/{\rm IIP3}_k^2 + A_{vk_l}^2/{\rm IIP3}_{k-1}^2}$$

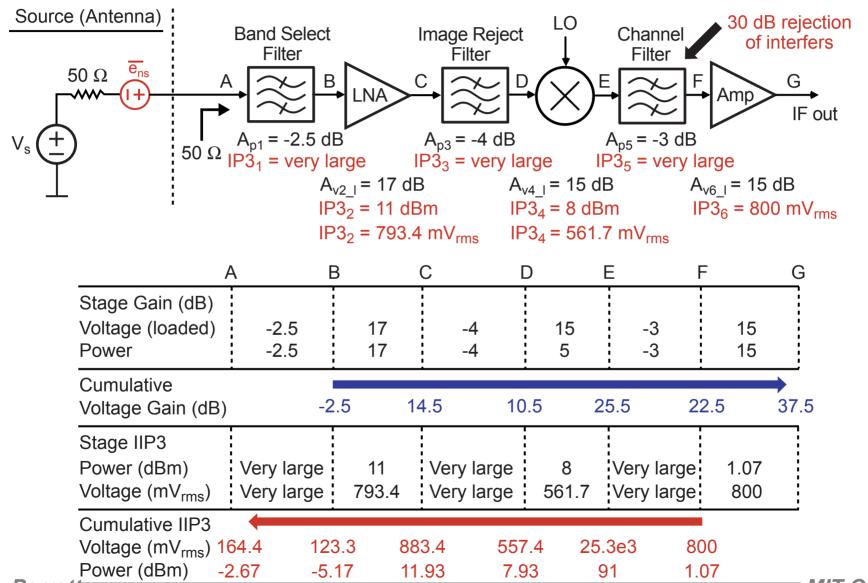
Conversion from rms voltage to dBm

$$dBm = 10\log(1e3 \cdot V_{rms}^2/R)$$

#### **Cumulative IIP3 Calculations**



#### "Level Diagram" for Gain, IIP3 Calculations



M.H. Perrott

# Final Comments on IIP3 and Dynamic Range

- Calculations we have presented assume
  - Narrowband stages
    - Influence of second order nonlinearity removed
  - IM3 products are the most important in determining maximum input power
- Practical issues
  - Narrowband operation cannot always be assumed
  - Direct conversion architectures are also sensitive to IM2 products (i.e., second order distortion)
  - Filtering action of channel filter will not reduce in-band IM3 components of blockers (as assumed in the previous example in node E calculation)

Must perform simulations to accurately characterize IIP3 (and IIP2) and dynamic range of RF receiver