

Let's think about calculating torque.

I have a force,  $F$ , being applied to an object.

And that object is pivoted at a point,  $Q$ . I'll define  $R$  as the vector from the pivot point,  $Q$ , to the point of the application of the force.

Torque is defined as the cross product,  $R$  cross  $F$ , which we can also write as  $R$  times  $F$  times the sine of  $\theta$ .

But what does that mean?

I'll introduce two different intuitive ways of understanding this mathematical expression.

First, we can think about this as the magnitude of  $F$  times the quantity,  $R$  sine  $\theta$ .

If we look at the direction of the force, then it is easy to see there  $R$  sine  $\theta$  is just the part of  $R$  that is perpendicular to the force.

So here the torque is equal to the magnitude of the force, times the magnitude of this perpendicular part of the vector  $R$ .

This perpendicular portion of the distance vector  $R$  is often referred to as the moment arm.

We can instead group  $F$  with sine  $\theta$ .

So this means that we're thinking of the cross-product as the distance  $R$  multiplied by  $F$  sine  $\theta$ .

The component of the force  $F$ , that's perpendicular to the position vector  $R$ .

Here I'm calculating torque as the distance between the pivot point, and where the force is applied, times the perpendicular part of the force.

Be very careful about the sine  $\theta$  term.

In many cases the angle  $\theta$  that is given in the problem is not the angle that is used in the expression.

In this example,  $F$  times the sine of  $\theta$ , will actually give the parallel component of the force.

Therefore it is much better to remember to take the perpendicular component, rather than just memorizing sine of  $\theta$ .