#### Class 15: Outline

#### Hour 1:

Magnetic Force Expt. 6: Magnetic Force

Hour 2: Creating B Fields: Biot-Savart Last Time: Magnetic Fields & Magnetic Dipoles

## **Magnetic Fields**

Magnetic Dipoles Create and Feel B Fields:

Also saw that moving charges feel a force:  $\vec{\mathbf{F}}_B = q \, \vec{\mathbf{v}} \times \vec{\mathbf{B}}$ 



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# What Kind of Motion Does this Lead to?

# **Cyclotron Motion**



(1) r : radius of the circle  $qvB = \frac{mv^2}{r} \Rightarrow r = \frac{mv}{qB}$ (2) T : period of the motion

$$T = \frac{2\pi r}{v} = \frac{2\pi m}{qB}$$

(3)  $\omega$ : cyclotron frequency

$$\omega = 2\pi f = \frac{v}{r} = \frac{qB}{m}$$

# **Current Carrying Wires**

Magnetic Force on Current-Carrying Wire

B

 $\mathbf{F}_{B}$ 

V<sub>d</sub>

q



$$\vec{\mathbf{F}}_B = I\left(\vec{\mathbf{L}}\times\vec{\mathbf{B}}\right)$$

Demonstration: Jumping Wire

#### Magnetic Force on Current-Carrying Wire



Current is moving charges, and we know that moving charges **feel** a force in a magnetic field

#### PRS Questions: 5 Predictions For Experiment 6

# **Experiment 6: Magnetic Force**

#### **Mid-term Course Evaluation**

# Lab Summary: Currents FEEL Forces in Magnetic Fields

Question: What happens if currents are next to each other?

#### Demonstration: Parallel & Anti-Parallel Currents

#### **How Do They Interact?**

Moving charges also create magnetic fields!

- The current in one wire *creates* a magnetic field that is *felt* by the other wire.
- This is the rest of today's focus





(http://ocw.mit.edu/ans7870/8/8.02T/f04/vis ualizations/magnetostatics/13-ParallelWires/13-Parallel\_Wires\_320\_f185.html)

(http://ocw.mit.edu/ans7870/8/8.02T/f04 /visualizations/magnetostatics/14-SeriesWires/14-Series\_320.html)

#### Sources of Magnetic Fields: Biot-Savart

## **Electric Field Of Point Charge**

An electric charge produces an electric field:



 $\hat{\mathbf{r}}$ : unit vector directed from q to P

# **Magnetic Field Of Moving Charge**

Moving charge with velocity v produces magnetic field:



 $\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$  permeability of free space

#### **The Biot-Savart Law**

Current element of length ds carrying current I produces a magnetic field:



(<u>http://ocw.mit.edu/ans7870/8/8.02T/f04/visualizations/magn</u>etostatics/03-CurrentElement3d/03-cElement320.html)

# The Right-Hand Rule #2



#### Animation: Field Generated by a Moving Charge

(http://ocw.mit.edu/ans7870/8/8.02T/f04/visualizations/magnetostatics/01-MovingChargePosMag/01-

MovChrgMagPos\_f223\_320.html)



#### Demonstration: Field Generated by Wire

Consider a coil with radius R and current I



#### Find the magnetic field B at the center (P)

Consider a coil with radius R and current I



- 1) Think about it:
  - Legs contribute nothing / parallel to r
  - Ring makes field into page
- 2) Choose a ds
- 3) Pick your coordinates
- 4) Write Biot-Savart

In the circular part of the coil...

$$d \vec{\mathbf{s}} \perp \hat{\mathbf{r}} \rightarrow /d \vec{\mathbf{s}} \times \hat{\mathbf{r}} = ds$$



Biot-Savart:  

$$dB = \frac{\mu_0 I}{4\pi} \frac{|d\vec{s} \times \hat{r}|}{r^2} = \frac{\mu_0 I}{4\pi} \frac{ds}{r^2}$$

$$= \frac{\mu_0 I}{4\pi} \frac{R d\theta}{R^2}$$

$$= \frac{\mu_0 I}{4\pi} \frac{d\theta}{R}$$

Consider a coil with radius *R* and current *I* 

 $dB = \frac{\mu_0 I}{4\pi} \frac{d\theta}{R}$  $B = \int dB = \int_{0}^{2\pi} \frac{\mu_0 I}{4\pi} \frac{d\theta}{R}$  $=\frac{\mu_0 I}{4\pi R}\int_{0}^{2\pi} d\theta = \frac{\mu_0 I}{4\pi R} (2\pi)$  $\vec{\mathbf{B}} = \frac{\mu_0 I}{2R}$  into page P15-26



Notes:

- •This is an EASY Biot-Savart problem:
  - No vectors involved
- •This is what I would expect on exam

#### PRS Questions: B fields Generated by Currents

# Group Problem: B Field from Coil of Radius R

Consider a coil with radius R and carrying a current I



WARNING: This is much harder than what I just did! Why??

# Field Pressures and Tensions: A Way To Understand the qVxB Magnetic Force

Tension and Pressures Transmitted by E and B

#### Fields (E or B):

- Transmit tension along field direction (Field lines want to pull straight)
- Exert pressure perpendicular to field (Field lines repel)

# **Example of E Pressure/Tension**



(http://ocw.mit.edu/ans7870/ 8/8.02T/f04/visualizations/ele ctrostatics/11-forceq/11-ForceQ\_f0\_320.html)

Positive charge in uniform (downward) E field Electric force on the charge is combination of

- 1. Pressure pushing down from top
- 2. Tension pulling down towards bottom

# **Example of B Pressure/Tension**



(http://ocw.mit.edu/ans7870/8/8 .02T/f04/visualizations/magneto statics/10-forcemovingq/10-ForceMovingQ\_f0\_320.html)

Positive charge moving out of page in uniform (downwards) B field. Magnetic force combines:

- 1. Pressure pushing from left
- 2. Tension pulling to right