## Problem set \#5

1. $(20 \mathrm{pts})$

A kind of triangular molecules form a 1D lattice as shown below. The mass of the molecule is $m$ and the separation between the molecules is $a$. The interaction between the molecules can be modeled by two kind of springs with spring constants $C_{1}$ and $C_{2}$ (see the figure below)

(a) Find the fundamental translation vector of the 1D lattice. Find the fundamental translation vector the reciprocal lattice.
(b) Calculate the dispersion relation $\omega_{k}$ of the two branches of sound waves.
(c) Plot the dispersion relations.
(d) Describe how molecules vibrate in the two branches of sound waves at wave vector $k=0$.
(e) Discuss the $C_{1} \rightarrow \infty$ and $C_{1}=C_{2}$ limits of your result.
2. Problem 6 on page 103 in Kittel.
3. Problem 1 on page 128 in Kittel.
4. Problem 3 on page 128 in Kittel.

