Lecture 3: Electrochemical Energy Storage

Systems for electrochemical energy storage and conversion include full cells, batteries and electrochemical capacitors. In this lecture, we will learn some examples of electrochemical energy storage. A schematic illustration of typical electrochemical energy storage system is shown in Figure 1.

Charge process: When the electrochemical energy system is connected to an external source (connect OB in Figure 1), it is charged by the source and a finite charge Q is stored. So the system converts the electric energy into the stored chemical energy in charging process.

Discharge process: When the system is connected to an external resistive circuit (connect OA in Figure 1), it releases the stored charge Q and generates a current through the external circuit. The system converts the stored chemical energy into electric energy in discharging process.

![Fig1. Schematic illustration of typical electrochemical energy storage system](image)

A simple example of energy storage system is capacitor. Figure 2(a) shows the basic circuit for capacitor discharge. Here we talk about the integral capacitance. The capacitance is defined as a constant,
The current is

\[ I = -\frac{dQ}{dt} = -C \frac{dV_c}{dt} \]  

(2)

The voltage applied to the external resistance is

\[ V = \frac{Q}{V_c} - IR_{\text{int}} = IR_{\text{ext}} \]  

(3)

Total resistance \( R = R_{\text{int}} + R_{\text{ext}} \)  

(4)

Plug(1), (2), (4) into (3), then we get

\[ Q = -RC \frac{dQ}{dt} \]

Apply the initial condition \( Q(t=0) = Q_0 \), we can solve the equation,

\[ Q = Q_0 e^{-\frac{t}{\tau}} \]

The relation between stored charge and time is shown in Figure 2(b), where \( \tau = RC \) is called decay time.

Fig 2. (a) Circuit for capacitor discharge  (b) Relation between stored charge and time during capacitor discharge

If we just consider the simplest linear circuit model,
\[ V = V_0 - IR_{\text{int}} - \frac{Q}{C} = V_0(Q) - IR_{\text{int}} \]

where \[ V_0(Q) = V_0 - \frac{Q}{C} \]

The relation between the voltage and stage of charge is shown in Figure 3,

Fig3. Relation between open circuit voltage and stage of charge in a linear circuit model
In the following sections, we will introduce some practical examples of electrochemical energy storage.

1. Supercapacitor

A supercapacitor is an electrochemical capacitor that has an unusually high energy density compared to common capacitors, typically on the order of thousands of times greater than a high capacity electrolytic capacitor. In general, supercapacitors improve storage density through the appliance of nano porous materials, as shown in Figure 4. Two porous electrodes with ultrahigh surface area are soaked in the electrolyte. The electrical energy is stored in the electrical double layer that forms at the interface between an electrolytic solution and an electronic conductor.

A supercapacitor can be modeled as an RC transmission line, shown in Figure 4. Assume a symmetric situation of two identical porous electrodes of thickness $L$, and thus focus on only one, in the region $0 < x < L$. The electrolyte-filled pore space has a
constant volume-averaged resistance per length $r$ and constant capacitance per unit length $c$. Neglect any resistance in the porous electrode or the thin gap between the electrodes. The mean potential in the pores satisfies a linear diffusion equation

$$rC \frac{\partial \phi}{\partial t} = \frac{\partial^2 \phi}{\partial x^2}$$

If we apply a sudden change of voltage $V$ for $t>0$ at $x=0$, the current response can be estimated as

$$I \sim \begin{cases} V \sqrt{\frac{c}{rL}} & , t << rcL^2 \\ \frac{V}{rL} e^{-\frac{t}{rcL}} & , t >> rcL^2 \end{cases}$$

2. Primary Battery

A primary cell is any kind of battery in which the electrochemical reaction is not reversible. Primary batteries can produce current immediately on assembly. A primary cell is not rechargeable because the chemical reactions are not reversible and active materials may not return to their original forms. Primary batteries are assembled in the charged state; discharge is the primary process during operation.

2.1 Alkaline Leclanché cell

Leclanché cell is a typical primary battery. The modern commercial Leclanché cell packaging and the basic structure are shown in Figure 5. The detailed reactions are

Anode (oxidation reaction, produces electrons):

$$\text{Zn} + 2\text{OH}^- \rightarrow \text{ZnO} + \text{H}_2\text{O}(l) + 2e^-$$

Cathode (reduction reaction, consumes electrons):

$$2\text{MnO}_2 + \text{H}_2\text{O}(l) + 2e^- \rightarrow \text{Mn}_2\text{O}_3 + 2\text{OH}^-$$

Net reaction:

$$\text{Zn} + 2\text{MnO}_2 \rightarrow \text{Mn}_2\text{O}_3 + \text{ZnO}$$
2.2 Primary Lithium battery Li-MnO$_2$

Primary Li-MnO$_2$ batteries use metallic lithium as anode and manganese dioxide as cathode, with a salt of lithium dissolved in an organic solvent. Due to the strong negative potential of metallic lithium, it’s possible to obtain high cell voltage (3.7V). 

Anode reaction:

$$\text{Li} \rightarrow \text{Li}^+ + e^-$$

Cathode reaction:

$$\text{Li}^+ + e^- + \text{MnO}_2 \rightarrow \text{LiMnO}_2$$

3. Secondary Battery

Secondary batteries are also known as rechargeable batteries because their electrochemical reactions are electrically reversible. Li-ion battery is a typical example of secondary battery. Li-ion batteries use intercalated lithium compounds as electrode materials. Cathode materials, such as LiCoO$_2$, LiMn$_2$O$_4$ and LiFePO$_4$, have been used in commercially available batteries. And the dominant anode material used in Li-ion batteries is graphite.
As shown in Figure 6, during discharge, Li ions move from the negative electrode and intercalate into the positive electrode. And the reverse reaction occurs when the cell is charging. The process that involves the transfer of Li ions back and forth between the two electrodes is sometimes called “rocking chair” effect.


Cathode half-reaction is:

\[ \text{LiCoO}_2 = \text{Li}_{1-x}\text{CoO}_2 + x \text{Li} + x e^- \]

Anode half-reaction is:

\[ x \text{Li} + x e^- + x \text{C}_6 = x \text{LiC}_6 \]

References
